

# Neuro-Cognitive Science Inspired Directions in Learning for Control

## Workshop on Cognition and Control ACC 2021

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This presentation contains numerous hyperlinks (in blue) as pointers for further study and exploration.

# Outline

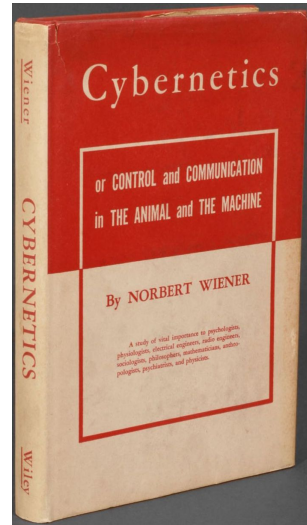
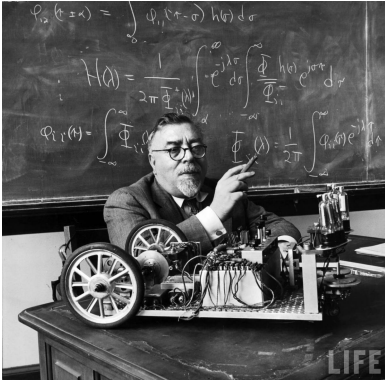
1. Context and Vision
2. Cognitive Cyber-Physical Systems
3. Technical Directions
4. Our Recent Work

Dedicated to the Memory of Dr. Kishan Baheti



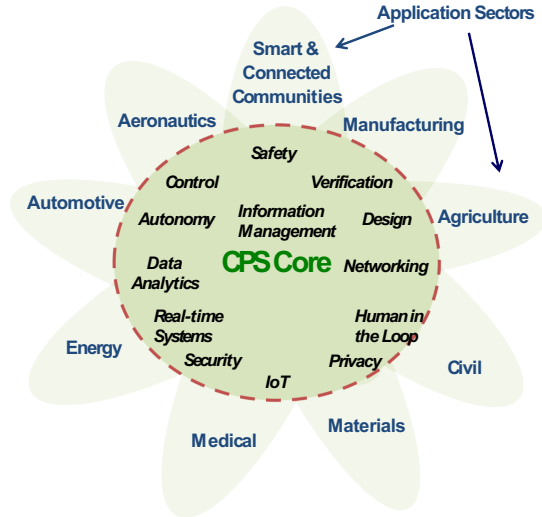
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# Wiener, Cybernetics, and Macy Conferences



How would the pioneers of cybernetics and AI envision the future of CPS?

# Cyber-Physical Systems



## Application Domains

### Transportation



- Faster and safer vehicles (airplanes, cars, etc)
- Improved use of airspace and roadways
- Energy efficiency
- Manned and un-manned

### Energy and Industrial Automation



- Homes and offices that are more energy efficient and cheaper to operate
- Distributed micro-generation for the grid

### Healthcare and Biomedical



- Increased use of effective in-home care
- More capable devices for diagnosis
- New internal and external prosthetics

### Critical Infrastructure



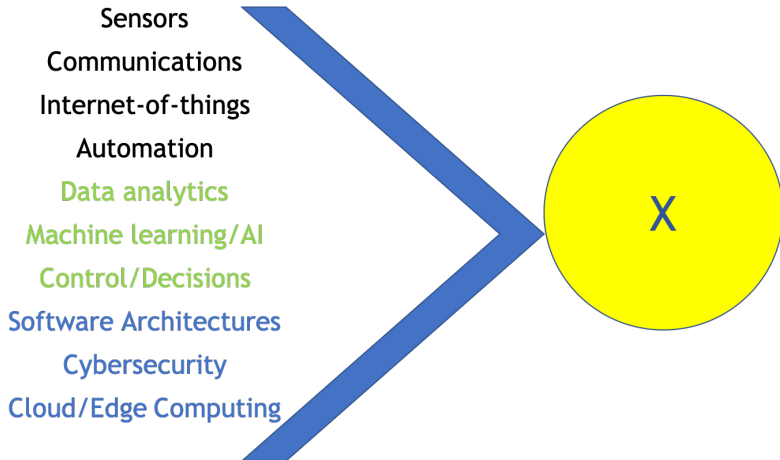
- More reliable power grid
- Highways that allow denser traffic with increased safety

## Aspirational and Emerging Applications: Examples

- ▶ Smart-X
  1. Smart manufacturing
  2. Smart grid
  3. Smart transportation
  4. Smart cities
  5. Smart health
- ▶ Autonomous systems
  1. Unmanned air vehicles
  2. Self-driving cars
  3. Autonomous robots

Human individual and group behavior are central in many of these applications:  
*Smart Cyber-Physical-Human Systems (CPHS).*

## Smart-X: Conceptual View



# Cognitive Cyber-Physical Systems



# Marr's 3 Levels of Analysis and Cognitive Science

Goal/Function (Computational)

Algorithm and Architecture

Implementation

# Cognition - Definitions and Characteristics

- ▶ “All processes by which the sensory input is transformed, reduced, elaborated, stored, recovered, and used.” — Neisser, Cognitive Psychology, 1967.
- ▶ Important role of in-built capacity in the brain from genetics and evolution, e. g., symmetry, intuitive physics.
- ▶ Key Cognitive Functions
  1. Perception
  2. Attention
  3. Memory
  4. Reasoning
  5. Problem solving
  6. Knowledge representation

Cognitive Psychology, Neisser (1967)

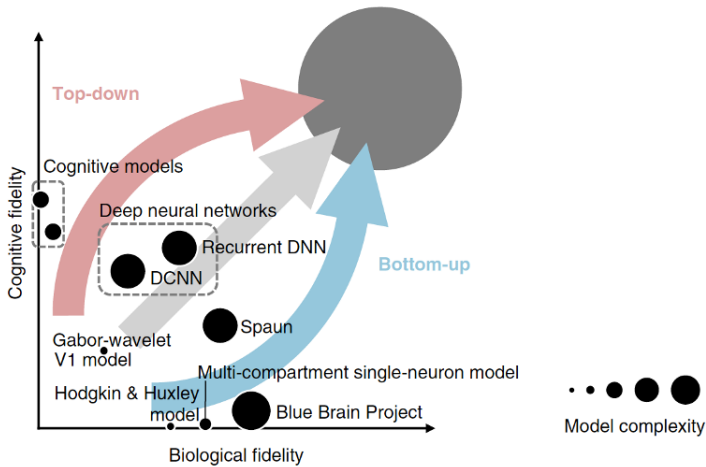
Mind as Machine: A History of Cognitive Science, Boden (2006)

## Cognitive CPS - Key Principles

- ▶ Working Definition: CPS that have *cognitive functions and capabilities*.
- ▶ CPS can be explicitly designed and/or can learn to possess cognitive functions.
- ▶ Need for specific cognitive functions and capabilities will depend on the problem.
- ▶ Cognitive CPS's may learn from each other, from humans, and also form collaborative networks.
- ▶ Hypothesis: Cognitive CPS will be better able to augment humans and lead to human flourishing.

**Cognitive CPS concept offers the most expansive and ambitious program for integrating ML/AI with CPHS for realizing Smart-X Systems.**

# Cognitive Models and Biological Fidelity



# Symbolic vs. Neural Connectionist Approaches

- ▶ Historical and ongoing debate on the nature of human cognition and the structure of the brain.
- ▶ Key topic in cognitive science: neuroscience, ML/AI, psychology, linguistics.
- ▶ Three major components:
  - ▶ Computational logic systems
  - ▶ Connectionist neural network models
  - ▶ Models and tools for uncertainty
- ▶ Pragmatic approach: combine connectionist, logic and probabilistic approaches to achieve desired system goals and objectives.

# Cognitive Models

- ▶ Production systems ([Newell and Simon](#)):
  1. If-then rules, logic, symbols
  2. Goals and subgoals, conflict resolution mechanisms
  3. Example: [ACT-R](#), [SOAR](#)
- ▶ Reinforcement learning based models
  1. Actions, states, rewards
  2. Perception and motor modules
  3. Value and policy based approaches
  4. Three modes: Model-free, model-based, and episodic
  5. [Brain combines all three of these modes but it is not known how this is done.](#)
- ▶ [Bayesian probabilistic models](#)

# Free Energy Principle

- ▶ A most ambitious **principle** for brain function due to K. Friston
- ▶ Brain seeks to minimize surprise
- ▶ Bayesian brain hypothesis: brain has an internal model that allows for computation of state estimate from sensory observations using Bayes rule
- ▶ Agent chooses action policy to maximize “information gain” (KL divergence or relative entropy)
- ▶ Free energy principle: minimize expected free energy under future observations and future states
- ▶ Connections to statistical mechanics, predictive coding, risk sensitive control, . . .

The free-energy principle: a unified brain theory?, Friston (2010)

# Perception in ML

- ▶ Deep learning is revolutionizing perception
- ▶ Compositionality is built-in
- ▶ Examples of very impressive progress in:
  - ▶ Computer vision
  - ▶ Speech recognition and processing
  - ▶ Language translation
- ▶ Architectures:
  - ▶ Convolutional neural networks
  - ▶ Long Short Term Memory (LSTM) recurrent neural networks



# Perception in CPS

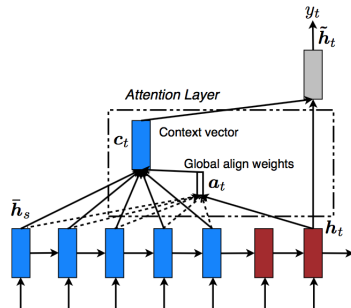
- ▶ CPS with multiple, distributed sources of sensed information
- ▶ Immediately possible to leverage DL advances
- ▶ Prior knowledge plays a very large role in cognitive theories of perception
- ▶ Neural network techniques could be combined with relational prior knowledge for improved context awareness in sensor rich CPS
- ▶ Potential tools and techniques for relational priors:
  1. Neural networks with symbolic front ends with priors to learn the symbolic front end
  2. Graph networks

# Computational Models of Attention

- ▶ Vision (human, robot, driving) has been a major focus for modeling of attention
- ▶ Feature integration theory, guided search model, CODE theory of visual attention, signal detection theory, ...
- ▶ Computational models:
  1. Itti's model: color, intensity, orientation
  2. Bayesian models of attention
  3. Decision theoretic models
  4. Information theoretic models
  5. Graphical models
  6. Spectrum analysis models

# Attention in ML

- ▶ Attention is the key to focusing on the most relevant information from multiple distributed sources of information
- ▶ Examples:
  - ▶ Recurrent Models of Visual Attention, Mnih et al. (2014)
  - ▶ Effective Approaches to Attention-based Neural Machine Translation, Luong et al. (2015)
  - ▶ Show, Attend and Tell: Neural Image Caption Generation with Visual Attention, Xu et al. (2015)
  - ▶ Self-attention Generative Adversarial Networks (GANs), Zhang et al (2019)



Attention based Machine Translator

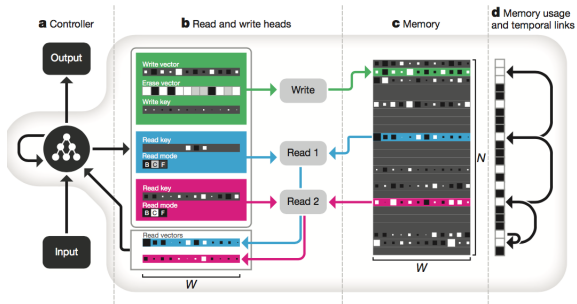
# Possible Routes to Attention in CPS

- ▶ Two levels of attention:
  - ▶ First level - selection and focus on a particular task
  - ▶ Second level - top-down search for relevant information
- ▶ Attention for detecting changing conditions and contexts.
- ▶ Attention for fault detection and/or resilience.
- ▶ Attention models that are hierarchical and programmable will be required for CPS
- ▶ Examples of programmable attention:
  1. Self-attention models of deep learning
  2. Non-local neural networks for image recognition
  3. Attentive meta learners

# Memory

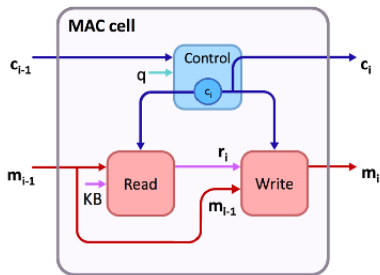
- ▶ Memory is central to intelligent behavior.
- ▶ Multiple memory mechanisms in human cognition:
  - ▶ short-term
  - ▶ long-term
  - ▶ episodic (content-addressable)
  - ▶ semantic
- ▶ **LSTM** - excellent example of use of memory in machine learning
- ▶ **Experience replay** - a key innovation in Deep RL breakthroughs
- ▶ Differentiable neural computer by [Graves et al. \(2016\)](#)
- ▶ Sparse distributed representations. Examples: [hierarchical temporal memory](#), [sparsey](#)

# Differentiable Neural Computer



Hybrid computing using a neural network with dynamic external memory, Graves et al. (2016)

# Memory, Attention, and Composition Cell Architecture



**Figure 3: The MAC cell architecture.** The MAC recurrent cell consists of a control unit, read unit, and write unit, that operate over dual **control** and **memory** hidden states. The **control unit** successively attends to different parts of the task description (question), updating the control state to represent at each timestep the reasoning operation the cell intends to perform. The **read unit** extracts information out of a knowledge base (here, image), guided by the control state. The **write unit** integrates the retrieved information into the memory state, yielding the new intermediate result that follows from applying the current reasoning operation.

## Example of Memory in CPS: Episodic Control

- ▶ Episodic control - re-enact successful episodes from memory storage.
- ▶ Episodic control has potential relevance to “small data” learning and control.
- ▶ Example: [Model-free episodic control, Blundell et al. \(2016\)](#)
- ▶ Model-free episodic control – recorded experiences are used as value function estimators.
- ▶ [Neural episodic control](#) – combining deep learning model and lookup tables of action values.
- ▶ Hierarchical episodic control – episodes as options.



## Selected Methodological Challenges

- ▶ There are numerous major challenges:
- ▶ Approaches for combining model-based and model-free techniques.
- ▶ Approaches to combine hierarchical and distributed architectures and algorithms.
- ▶ Reducing the need for large amounts of data: few-shot learning, one-shot learning
- ▶ Bringing meta learning paradigm for achieving autonomy: “learning to learn”.

## Combining Model-based and Model-free Approaches

- ▶ Model free ML based approaches for sensing, perception, memory and model-based for planning, safety and closing the loop
- ▶ Model predictive control and reinforcement learning – compute action sequence based on the model via MPC (model based), update the model via reinforcement learning and supervised learning
- ▶ **Guided policy search** – robust local policies are derived from local models; local policies used to guide a global policy

# Hierarchical Control

- ▶ Hierarchical structures appropriate and necessary for control and management of Smart-X
- ▶ Optimal behavioral hierarchy, Solway et al. (2014)
- ▶ Hierarchical control for sparse reward settings: meta controller sets the intermediate goal/sub-tasks and a lower level controller achieves the goal  
Example: Hierarchical DQN
- ▶ Hierarchical control provides scalable methods for large state-action spaces.  
Examples:
  - ▶ Options framework – temporally extended sequence of actions to simplify the learning process
  - ▶ Feudal RL – Higher level task is divided into a hierarchy of tasks
  - ▶ MAXQ framework: extension of the Q learning framework for the hierarchical setting

## Our Recent Work

- ▶ External memory architectures and algorithms for adaptive control
- ▶ Regret guarantees for online learning for control
- ▶ Reinforcement learning for matching markets with applications to smart grids
- ▶ Meta learning
- ▶ Smart-X applications:
  - ▶ Anomaly detection in smart grids and manufacturing
  - ▶ Graph network techniques for decision making in autonomous vehicles

# Meta Learning Paradigm

- ▶ **Meta Learning** as a paradigm for dealing with new environments by “learning to learn” approaches
- ▶ Learning from task properties, *transfer learning* from prior models, ...
- ▶ Meta learning principles and approaches could be leveraged for autonomy and control under uncertainty
- ▶ Central question: can the experience from learning in one setting to improve learning in another?
- ▶ Meta-learning is relevant in scenarios where the environment is different in each learning or control episode.
- ▶ Our Goals:
  - ▶ To provide a framework for meta-learning in a control setting
  - ▶ To provide a benchmark for finite episode meta-learning guarantees

## Problem Setting

- ▶  $N$  episodes of length  $T$
- ▶ The environment draws an arbitrary  $\theta = [A, B] \in \Theta$  in each episode
- ▶ System dynamics within each episode:

$$x_{t+1} = Ax_t + Bu_t, \quad y_t = x_t + \epsilon_t, \quad x_1 = x_s, \quad \epsilon_t \text{ is noise.}$$

- ▶ Control input constraints:  $u_t \in \mathcal{U}, \forall t, \mathcal{U} = \{u | F_u u \leq b_u\}$  = a bounded polytope
- ▶ Control cost function:  $c_t(x_t, u_t)$ .
- ▶ Information:

Known	Observable
$\Theta,$ $\{c_s(., .)\}_{s \geq 1}$ (limited preview of future cost)	$\{y_s\}_{s \leq t}, \{u_s\}_{s \leq t-1}$

# Meta-Learning Architecture

superscript  $i$ : episode, subscript  $k$ : time index within an episode

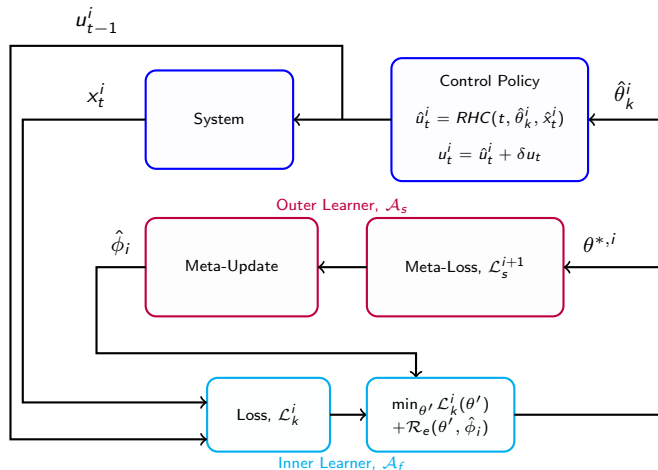
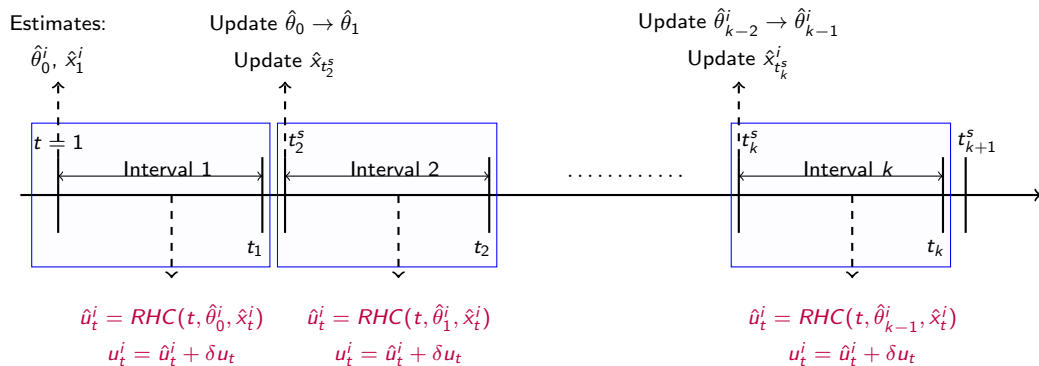


Figure: Online Model-based Meta-learning Control Architecture

# Online Control Algorithm



Length of interval  $k$ :  $t_k - t_k^s + 1 = 2^{k-1}H$ .



## Inner Learner $\mathcal{A}_s$

- Loss  $\mathcal{L}_k^i$ ,

$$\mathcal{L}_k^i(\hat{\theta}) = \sum_{j=1}^{t_k} l_{\hat{\theta},j}^i, \quad l_{\hat{\theta},j}^i = \left\| y_{j+1}^i - \hat{\theta}[(y_j^i)^\top, (u_j^i)^\top]^\top \right\|_2^2.$$

- Least-squares estimate:

$$\hat{\theta}_{l,k}^i = \arg \min_{\hat{\theta}} \mathcal{L}_k^i(\hat{\theta}) + \mathcal{R}_e(\hat{\theta}, \hat{\phi}_i),$$

$$\mathcal{R}_e(\hat{\theta}, \hat{\phi}_i) = \lambda \left\| \hat{\theta} - \hat{\phi}_i \right\|_F^2.$$

## Control Policy: $RHC(t, \hat{\theta}_t^i, \hat{x}_t^i)$

- **Input:** Horizon  $M$ ,  $\{c_k\}_{t \leq k \leq t+M-1}$ , **Output:**  $\hat{u}_t^i$
- $RHC(t, \hat{\theta}_t^i, \hat{x}_t^i)$ : (Optimizes the cost-to-go for the estimated dynamics)
  1.  $U^* = \arg \min_U \sum_{k=0}^{M-1} c_{k+t}(\tilde{x}_k, w_k)$   
s.t.  $\tilde{x}_{k+1} = \hat{A}\tilde{x}_k + \hat{B}w_k$ ,  $\hat{\theta}_t^i = [\hat{A}, \hat{B}]$ ,  $w_k \in \mathcal{U}$ ,  $\tilde{x}_0 = \hat{x}$
  2.  $\hat{u}_t^i = w_0^*$  (current RHC control input)

# Perturbation

- ▶ The RHC approach requires persistence of excitation for parameter estimation. This requires perturbation along certain directions. One of the key contributions of this work: [balancing exploration and exploitation in online RHC](#).
- ▶ Perturbation may violate control input constraints. The control is designed so that while balancing exploration and exploitation constraint violation is bounded.

## Perturbation $\delta u_t$

- Perturbation by  $\delta u_t$  guarantees that

$$\sum_{j=1}^{t_k} \begin{bmatrix} x_j \\ u_j \end{bmatrix} \begin{bmatrix} x_j^\top & u_j^\top \end{bmatrix} \geq O(\sqrt{t_k}) \text{ (persistent excitation)}$$

(The specific rate of growth balances exploration and exploitation!)

## Outer Learner $\mathcal{A}_f$

► Outer learner update

$$\psi_{i+1} = \hat{\phi}_i - \eta_i \nabla l_i^o(\hat{\phi}_i), \quad \eta_i = \frac{1}{\sqrt{i}}, \quad l_i^o(\hat{\phi}) = \left\| \hat{\theta}^{*,i} - \hat{\phi} \right\|_F,$$

$\hat{\theta}^{*,i}$  = best inner learner estimate in episode  $i$

$$\hat{\phi}_{i+1} = \text{Proj}_{\Theta}(\psi_{i+1})$$

# Regret for Cost

- ▶ Regret

$$R_T^i = [\mathcal{C}^i(\mathcal{H}) - \mathcal{C}^{i,*}] , \text{ where } \mathcal{C}(\mathcal{H}) = \sum_{j=1}^T [c_j(x_j^i, u_j^i)],$$

$\mathcal{C}^{i,*}$  cost with complete knowledge of system and state

- ▶ Average regret across  $N$  episodes:

$$\bar{R} = \frac{1}{N} \sum_{i=1}^N R_T^i$$

## Performance for Constraint Violation

- Constraint violation in episode  $i$ ,

$$\mathcal{V}^i = \sum_{t=1}^T \left( \sum_s \{F_u u_t^i - b_u\}_{s,+} \right), \quad U_{1:T}^i = \{u_1^i, u_2^i, \dots, u_T^i\}$$

where  $\{.\}_l$  denotes the  $l$ -th component of a vector. The subscript  $\{.\}_+$  is a shorthand notation for  $\max\{., 0\}$

- Average constraint violation across  $N$  episodes:

$$\bar{\mathcal{V}} = \frac{1}{N} \sum_{i=1}^N \mathcal{V}^i(.)$$

## Key Results

- ▶ Per episode regret and constraint violation: Under suitable technical conditions, for  $\delta$  arbitrarily small, with probability greater than  $1 - \mathcal{O}(\delta)$ :

$$R_T \leq \tilde{\mathcal{O}}\left(T^{3/4}\right), \quad \nu \leq \tilde{\mathcal{O}}\left(T^{3/4}\right).$$

- ▶ Early result: Under the same technical conditions,  $N \geq T$ , for  $\delta$  arbitrarily small, with probability greater than  $1 - \mathcal{O}(\delta)$

$$\bar{R} \leq \tilde{\mathcal{O}}\left(\left(1 + \frac{1}{\sqrt{N}}\right) T^{3/4}\right), \quad \bar{\nu} \leq \tilde{\mathcal{O}}\left(\left(1 + \frac{1}{\sqrt{N}}\right) T^{3/4}\right).$$



# Contributions

- ▶ Key contribution: Comparison with respect to receding horizon controller with complete knowledge of system and state. Prior online control works analyse regret w.r.t linear feedback controllers.
- ▶ Novel approach to balance exploration and exploitation in online RHC
- ▶ First finite time regret guarantee for online RHC
- ▶ First finite-time guarantee for meta-learning in a control setting

## Publications for More Details I

1. D. Muthirayan and P. P. Khargonekar, "Working Memory Augmentation for Improved Learning in Neural Adaptive Control," IEEE Conference on Decision and Control, pp. 6785-6792, 2019.
2. D. Muthirayan, and P. P. Khargonekar, "Memory Augmented Neural Network Adaptive Controllers: Performance and Stability", arXiv preprint arXiv:1905.02832, 2019.
3. D. Muthirayan, and P. P. Khargonekar, "Memory Augmented Neural Network Adaptive Controller for Strict Feedback Nonlinear Systems," arXiv preprint arXiv:1906.05421, 2019.
4. D. Muthirayan, S. Nivison and P. P. Khargonekar, "Improved Attention Models for Memory Augmented Neural Network Adaptive Controllers," arXiv preprint arXiv:1910.01189, 2019, Proceedings of American Control Conference, pp. 639-646, 2020.
5. D. Muthirayan, J. Yuan and P. P. Khargonekar, "Regret Guarantees for Online Receding Horizon Learning Control," arXiv preprint arXiv:2010.07269, 2021.
6. D. Muthirayan, and P. P. Khargonekar, "Meta-Learning Guarantees for Online Receding Horizon Learning Control," arXiv preprint arXiv:2010.11327, 2021.
7. D. Muthirayan, J. Yuan, P. P. Khargonekar, "Adaptive Gradient Online Control", arXiv preprint arXiv:2103.08753, 2021.

## Publications for More Details II

8. M. Majidi\*, D. Muthirayan\*, M. Parvania, P. P. Khargonekar, "Dynamic Matching Markets in Power Grid: Concepts and Solution using Deep Reinforcement Learning", arXiv preprint arXiv:2104.05654, 2021.
9. D. Muthirayan, M. Parvania, P. P. Khargonekar, "[Online Algorithms for Dynamic Matching Markets in Power Distribution Systems](#)", IEEE Control Systems Letters, pp. 995-1000, 2020.
10. A. Barua, D. Muthirayan, P. P. Khargonekar, M. A. Al. Faruque, "[Hierarchical Temporal Memory based One-pass Learning for Real-Time Anomaly Detection and Simultaneous Data Prediction in Smart Grids](#)", IEEE Transactions on Dependable and Secure Computing, 2020
11. A. V. Malawade, N. D. Costa, D. Muthirayan, P. P. Khargonekar, M. A. Al. Faruque, "[Neuroscience-inspired algorithms for the predictive maintenance of manufacturing systems](#)", IEEE Transactions on Industrial Informatics, 2021, early access.
12. S. Y. Yu, A. V. Malawade, D. Muthirayan, P. P. Khargonekar, M. A. Al. Faruque, "[Scene-graph augmented data-driven risk assessment of autonomous vehicle decisions](#)", IEEE Transactions on Intelligent Transportation Systems, 2021, early access.

Thank you!

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