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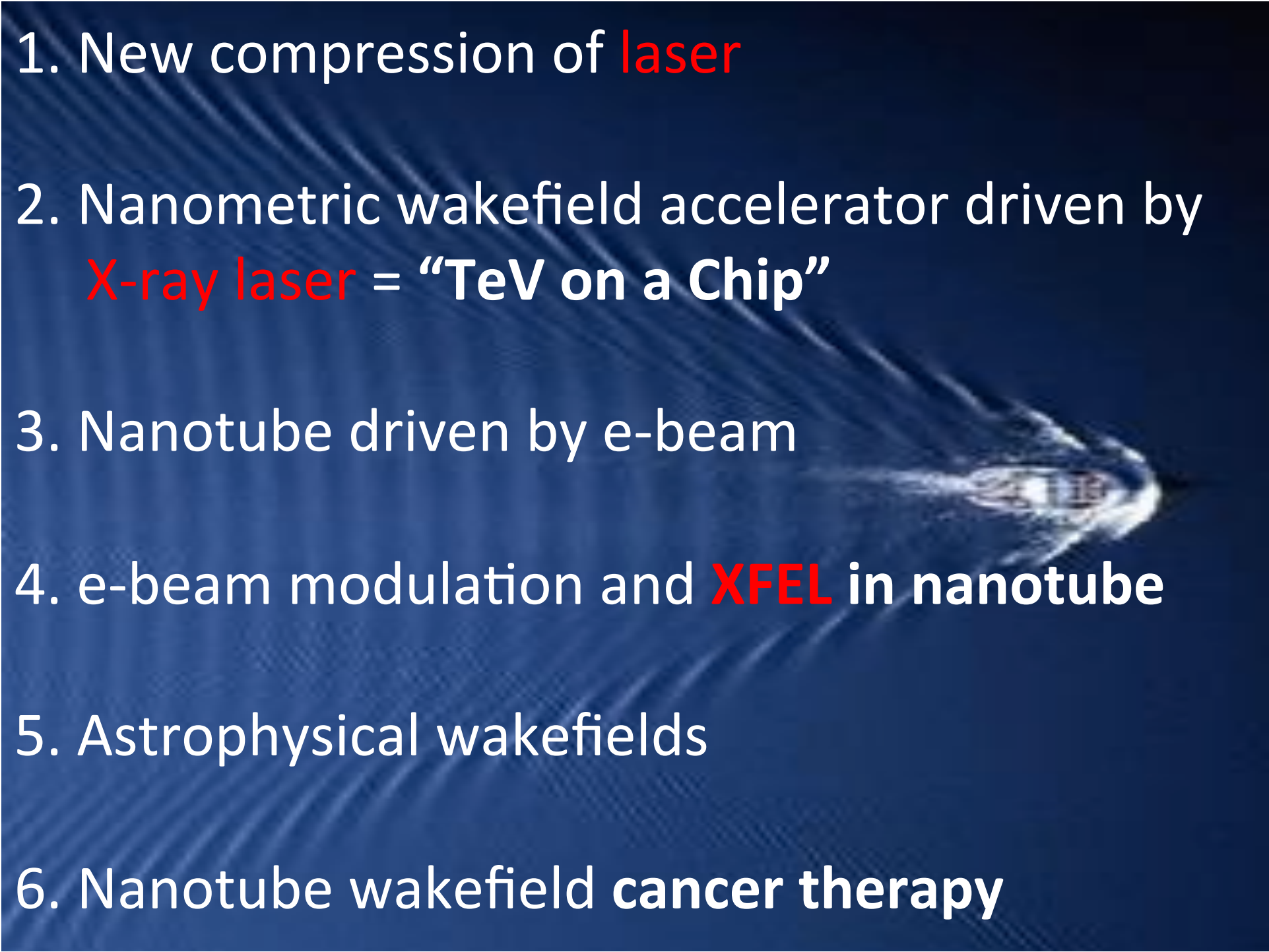
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Geneva, Feb. 13, 2020

# “TeV on a Chip”: A New Perspective of Wakefield Acceleration

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Collaboration: V. Shiltsev, A. Sahai, S. Hakimi, G. Mourou, Y.M. Shin, P. Taborek, K. Nakajima, T. Ebisuzaki, X. Yan, A. Chao, B. Barish, K. Abazajian, S. Barwick, X. M. Zhang, J. Wheeler, W. J. Sha, S. Nicks, D. Roa, T. Juhasz, D. Strickland, D. Farinella, A. Necas, F. Tamanoi, G. Szabo, F. Zimmermann

- 
1. New compression of **laser**
  2. Nanometric wakefield accelerator driven by **X-ray laser** = “TeV on a Chip”
  3. Nanotube driven by e-beam
  4. e-beam modulation and **XFEL** in nanotube
  5. Astrophysical wakefields
  6. Nanotube wakefield **cancer therapy**

# Motivation:

1. Invention of **Thin Film Compression** (TFC, 2013) opened up **Laser Wakefield Acceleration** (LWFA, 1979) in **X-ray** regime,

$$E_{TD} = m\omega_{pe} c / e; \quad \Delta\varepsilon = 2mc^2 a_0^2 (n_{cr} / n)$$

compactifying further by  $10^3$  over the gas plasma LWFA

2. X-ray frequency exceeds the nanomaterial's plasma frequency  $\omega_{pe}$

→ **carbon-nanotubes**

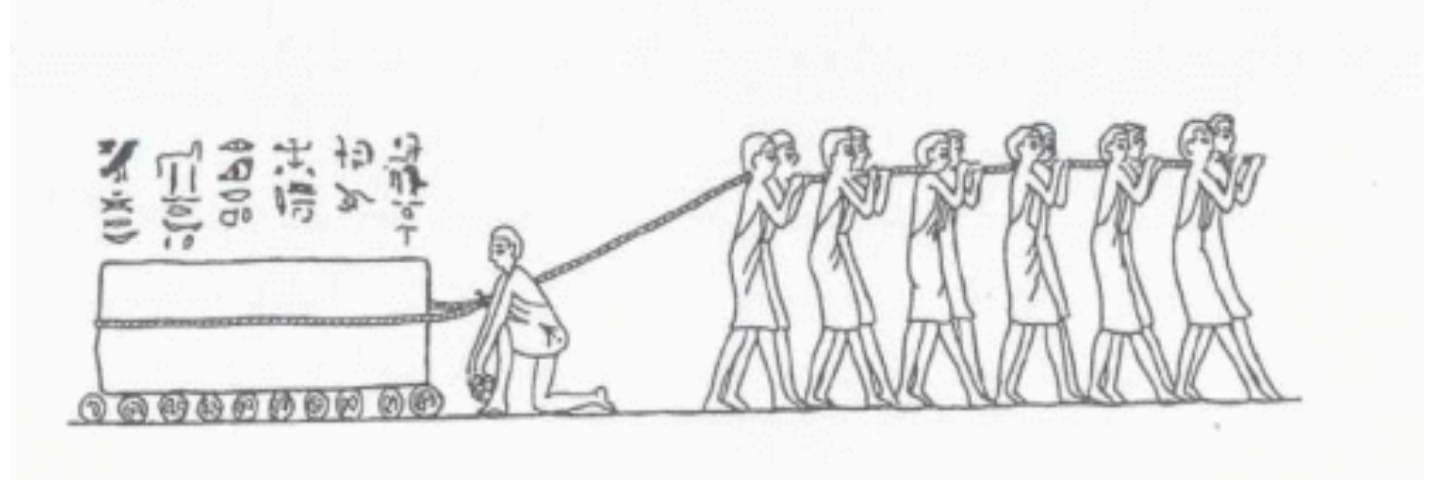
higher than 10TV/m wakefield (2014)

→ Explore **X-ray** wakefield accelerator in nanotube = “TeV on a Chip”

# Plasma (nanomaterial) accelerator driven by beam/pulse

Collective force  $\sim N^2$  (nonlinear  $\leftarrow$  linear force  $\sim N$ )

Coherent and smooth structure (not stochastic)



Plasma (nanomatter) accelerator driven by **laser** (coherent photons)

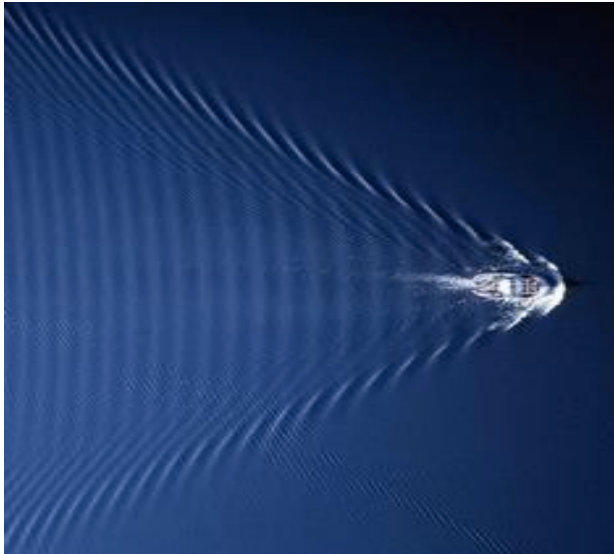
compactification by  $10^3 - 10^4$  (now even by  $10^6$ )  $\gg$  conventional accelerators

enabled by **laser** technology (laser compression (Mourou et al.1985))



# Laser Wakefield (LWFA):

Wake phase velocity  $\gg$  water movement speed  
maintains **coherent** and **smooth** structure



Tsunami phase velocity becomes  $\sim 0$ ,  
causes **wavebreak** and **turbulence**

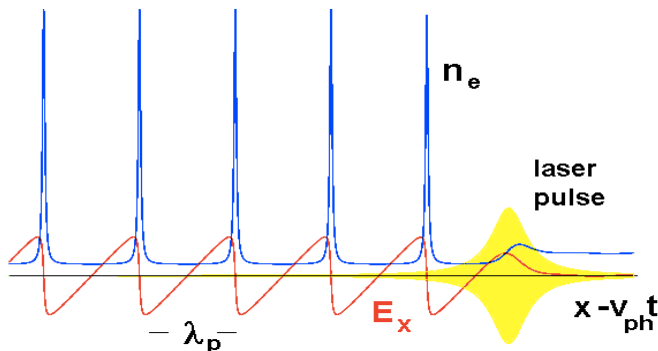


VS

Strong beam (of **laser** / particles) drives plasma waves to saturation amplitude:  $E = m\omega v_{ph} / e$

No wave breaks and wake **peaks** at  $v \approx c$

Wave **breaks** at  $v < c$



← relativity  
regularizes  
(*relativistic coherence*)



**Relativistic coherence** enhances beyond the Tajima-Dawson field  $E = m\omega_p c / e$  ( $\sim$  GeV/cm)

# The late Prof. Abdus Salam



At ICTP Summer School (1981), Prof. Salam summoned me and discussed about **laser wakefield** acceleration.

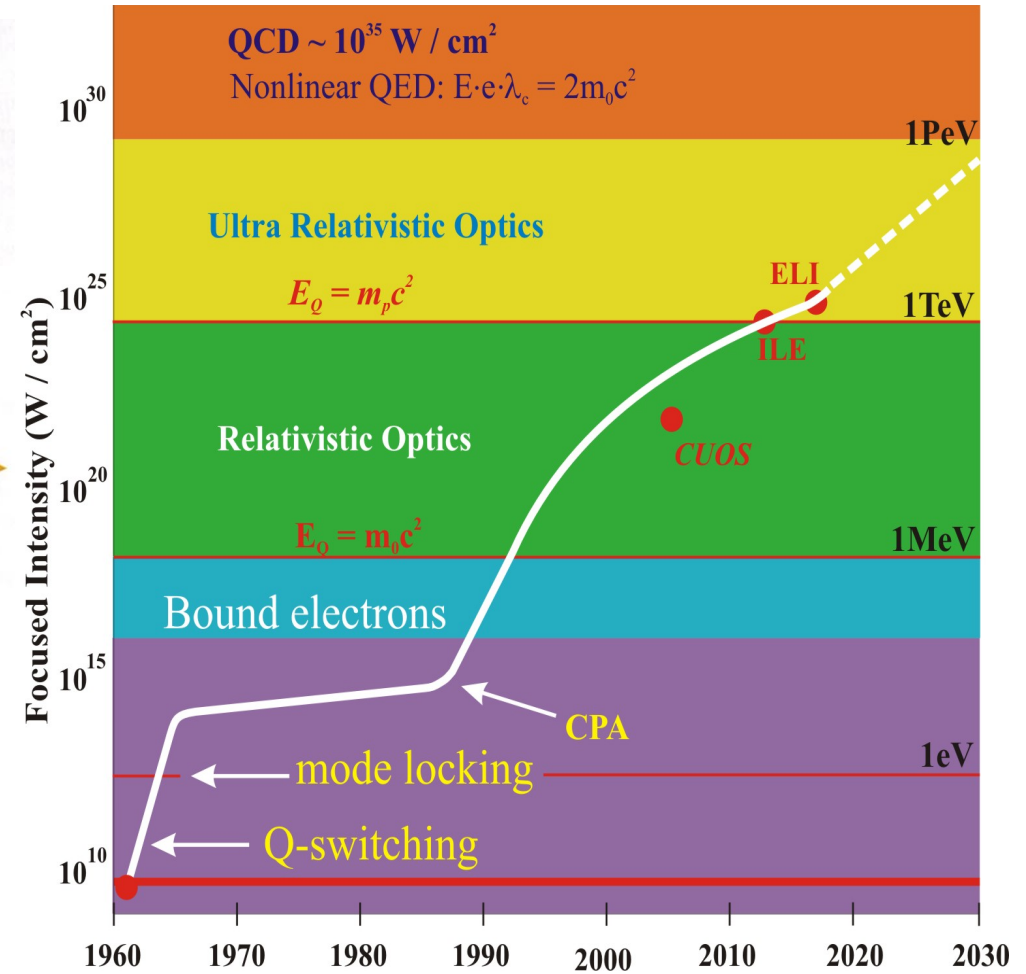
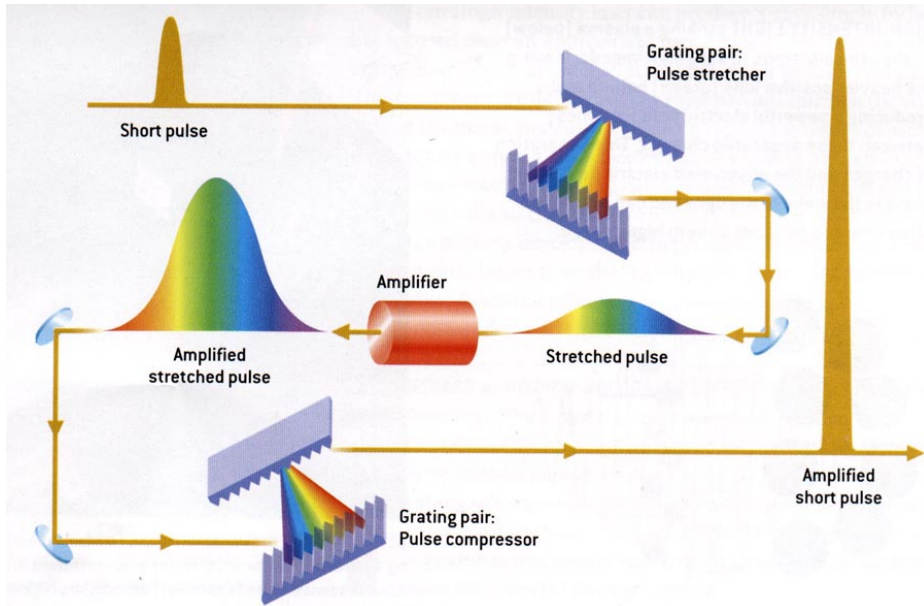
Salam: *'Scientists like me began feeling that we had less means to test our theory. However, with your laser acceleration, I am encouraged'*. (1981)

He organized the Oxford Workshop on **laser wakefield** accelerator in 1982.

Effort: many scientists over many years to realize his vision / dream  
High field science: spawned

(NB: Prof. C. Rubbia et al.  
discovered his bosons at CERN, 1983)

# Enabling technology: **laser** revolution



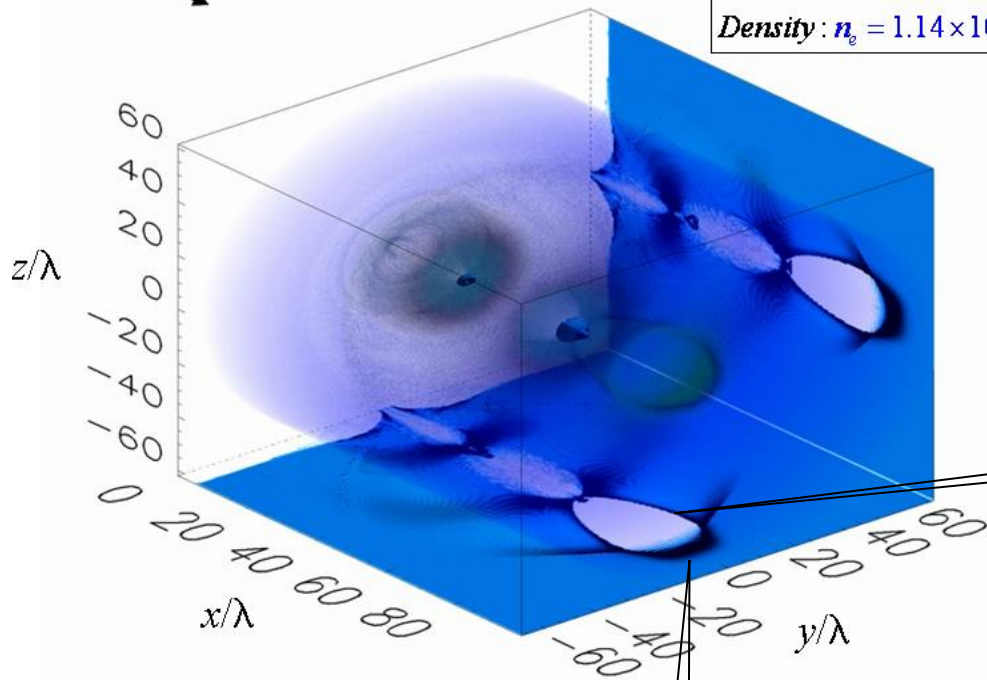
G. Mourou invented **Chirped Pulse Amplification** (1985)

**Laser** intensity exponentiated since,

to match the required intensity for Tajima-Dawson's **LWFA** (1979)

# Laser-driven Bow and Wake

Density:  $n_e = 1.14 \times 10^{18} \text{ cm}^{-3}$



Wakefield acceleration

Wake Wave



(Bulanov, Esirkepov)

Bow Wave

Ponderomotive acceleration

# Theory of **wakefield** toward extreme energy

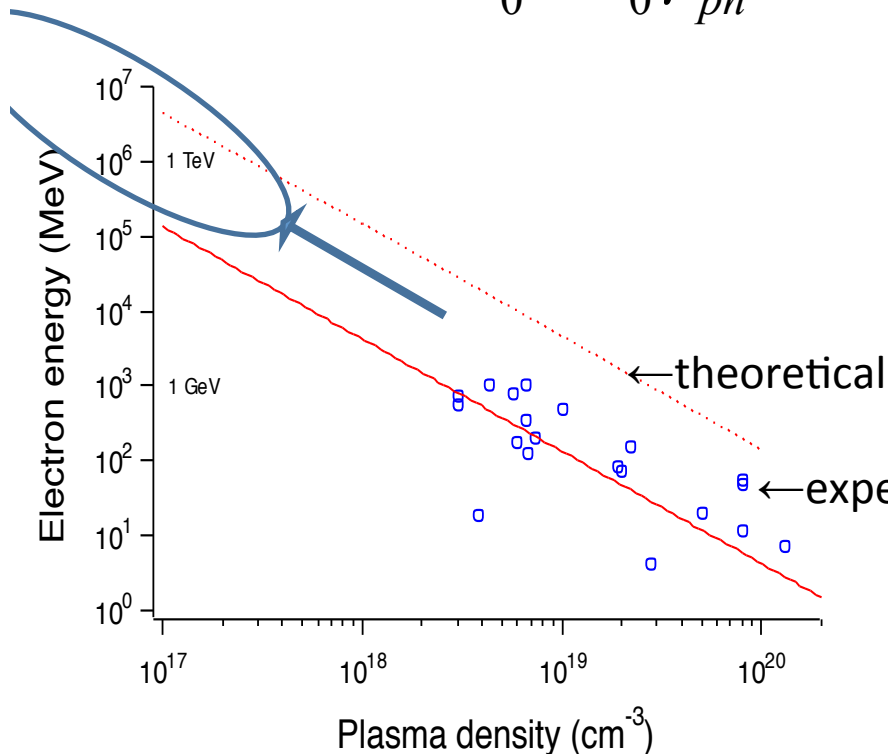
$$\Delta E \approx 2m_0c^2 a_0^2 \gamma_{ph}^2 = 2m_0c^2 a_0^2 \left( \frac{n_{cr}}{n_e} \right), \quad (\text{when 1D theory applies})$$

In order to avoid wavebreak,

$$a_0 < \gamma_{ph}^{1/2},$$

where

$$\gamma_{ph} = [n_{cr}(\omega) / n_e]^{1/2}$$



$$n_{cr} = 10^{21} / \text{cc} \text{ (1eV photon)}$$

$$\rightarrow 10^{29} \text{ (10keV photon)}$$

$$n_e = 10^{16} \text{ (gas)} \rightarrow 10^{23} / \text{cc} \text{ (solid)}$$

$$L_d = \frac{2}{\pi} \lambda_p a_0^2 \left( \frac{n_{cr}}{n_e} \right), \quad L_p = \frac{1}{3\pi} \lambda_p a_0 \left( \frac{n_{cr}}{n_e} \right),$$

dephasing length

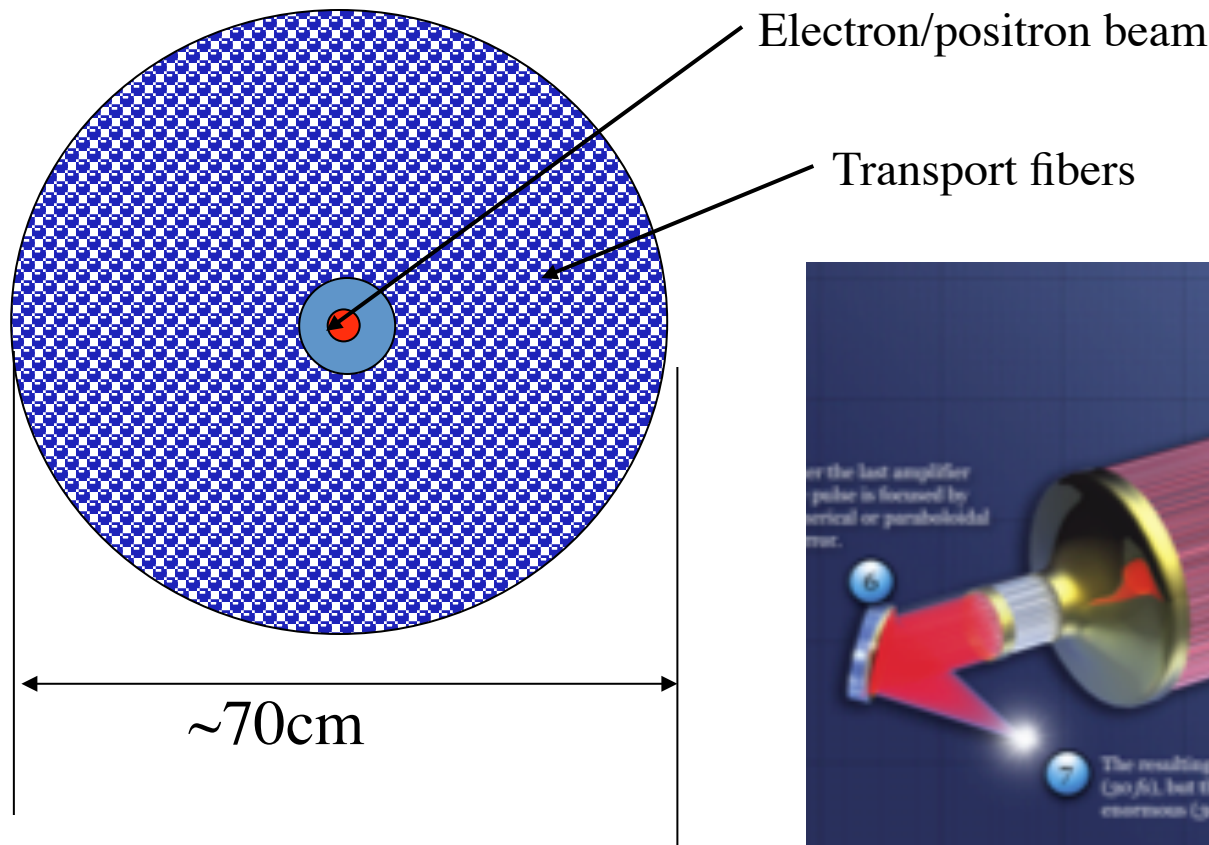
pump depletion length



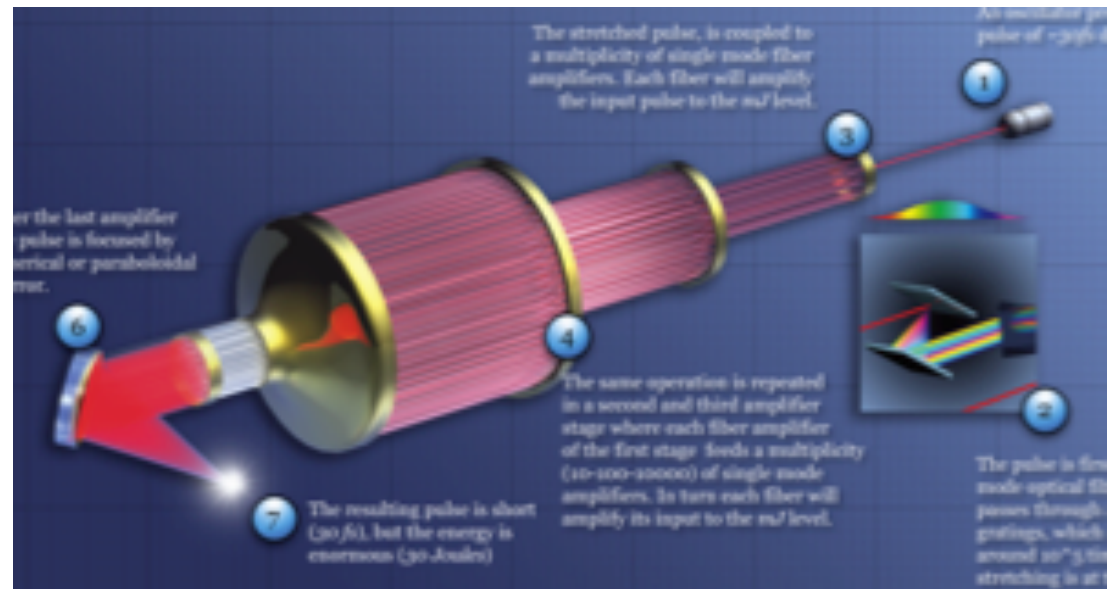
# CAN Laser:

Need to Phase

32 J/1mJ/fiber ~  $3 \times 10^4$  Phased Fibers!



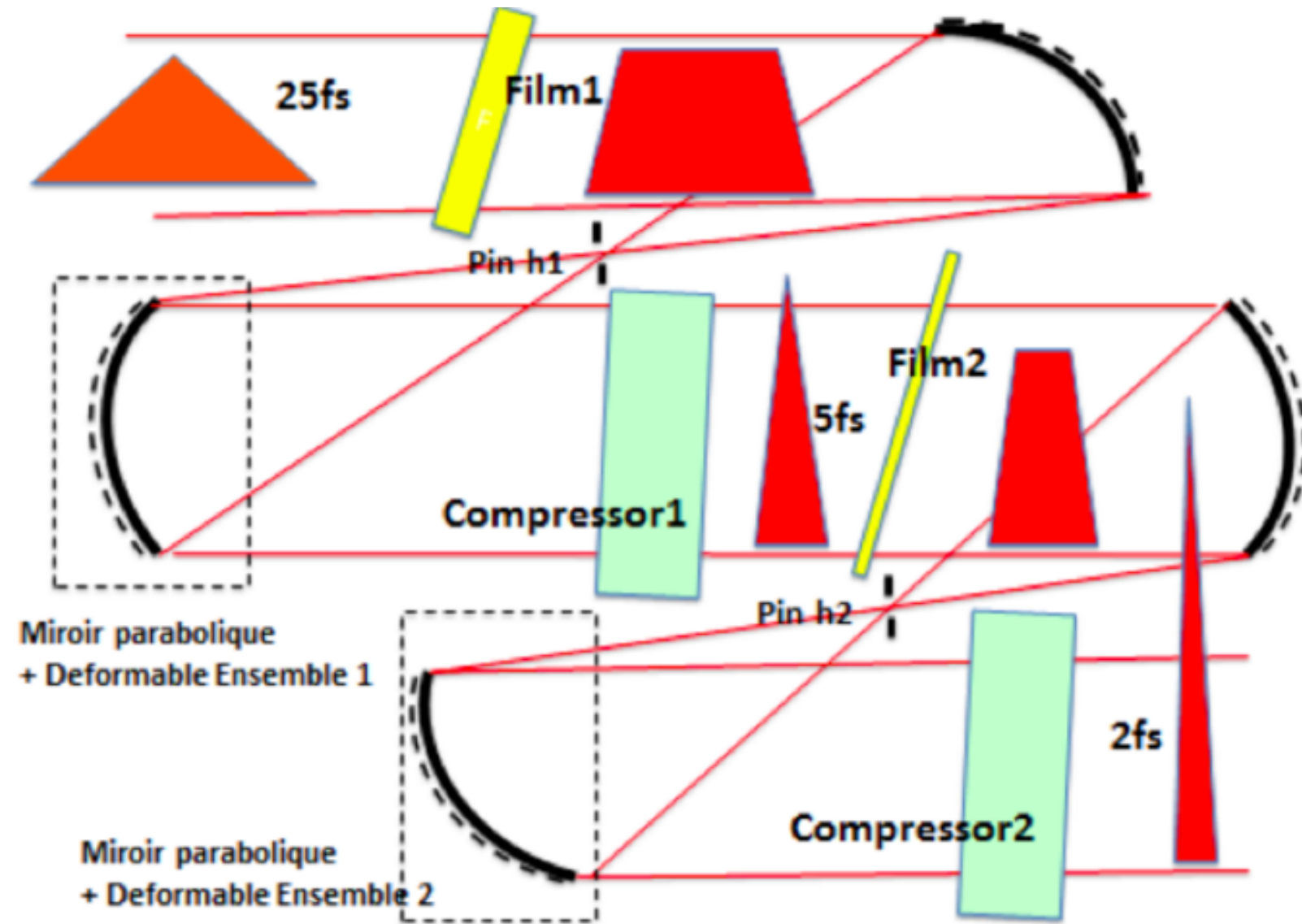
Mourou, Brookesby, Tajima, Limpert (2013)



Length of a fiber ~2m

Total fiber length ~  $5 \times 10^4$  km

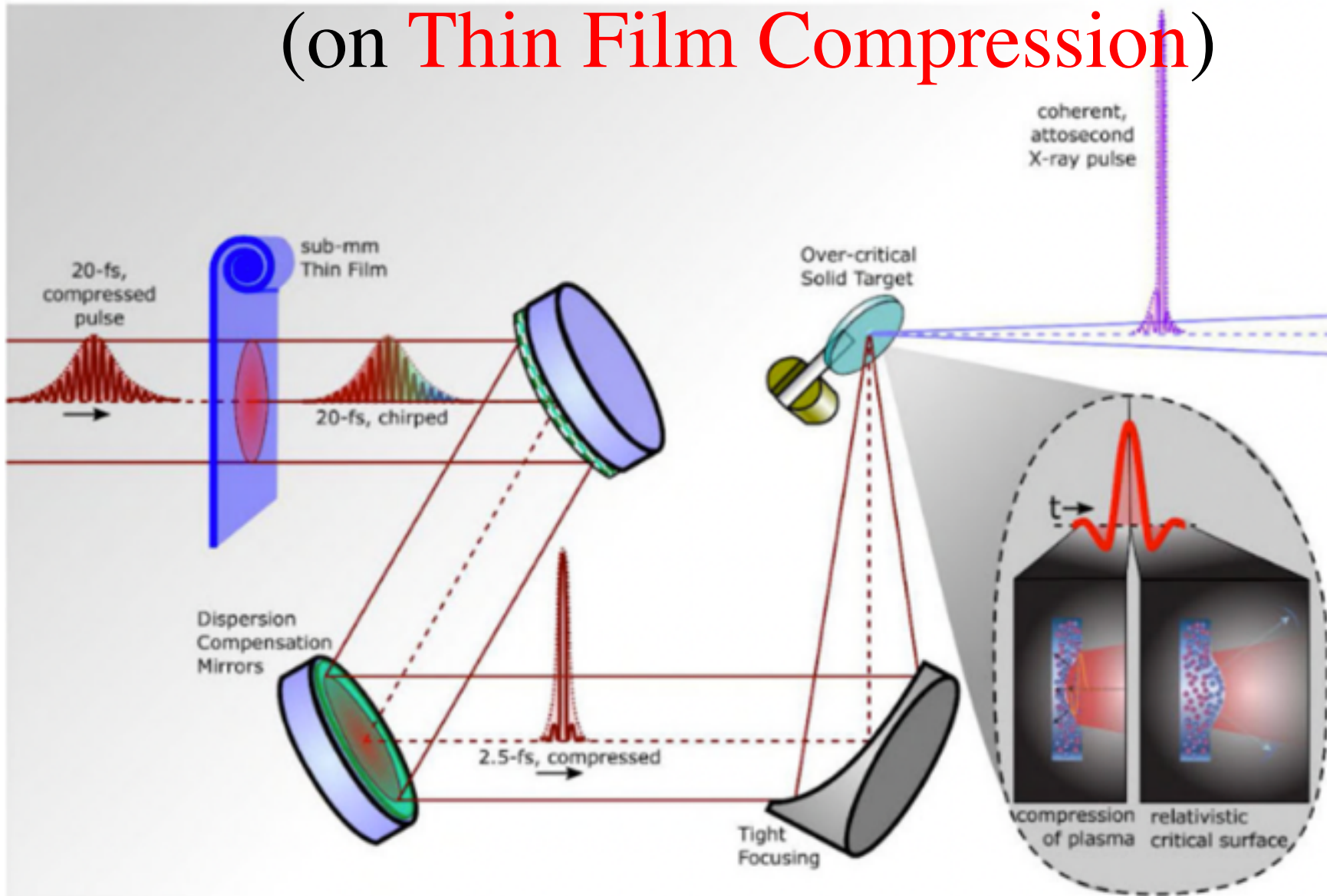
# Thin Film Compression



Single-cycled **laser** and “TeV on a chip”



# Next Generation X-ray Lasers (on Thin Film Compression)





# Earlier works of X-ray crystal acceleration

- X-ray optics and fields (Tajima et al. ,1987)
- Nanocrystal hole for particle propagation (Newberger, Tajima, et al. 1989)
- particle transport in the crystal (Tajima et al. 1990)

## APPLICATION OF NOVEL MATERIAL IN CRYSTAL ACCELERATOR CONCEPTS

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which incorporate regular macroscopic features on the underlying crystal lattice are of potential application to crystal accelerators and coherent sources. We have recently begun an investigation of material, porous Si, in which pores of radii up to a lattice spacings are etched through finite volumes of crystal. The potential reduction of losses to particle transport in crystal accelerators for relativistic, positively charged particles in this context will be presented. The consequences of this transport will be discussed.

and  $k = v_0/m_I c^2$ ,  $v_0$ , is the "spring constant of the channel well. Its specific form depends on the material. To construct the continuum potential of a string of atoms for purposes it suffices to take a typical value of  $2 \times 10^4$  eV is the multiple scattering velocity space "diffusion" We have used<sup>10</sup>

$$D = z\pi r_e^2 N Z_{\text{val}} \left(\frac{m_e}{m_I}\right)^2 L_R,$$

where  $r_e$  is the classical electron radius,  $Z_{\text{val}}$  is the number of valence electrons, and  $N$  is the number density of atoms. Logarithmic dependencies on particle energy are neglected throughout:  $L_R$  is a constant with a value

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## BEAM TRANSPORT IN THE CRYSTAL X-RAY ACCELERATOR

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**Abstract** A Fokker-Planck model of charged particle transport in crystal channels which includes the effect of strong accelerating gradients has been developed<sup>1</sup> for application to

### Crystal X-Ray Accelerator

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 and

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 (Received 18 November 1986)

An ultimate linac structure is realized by an appropriate crystal lattice (superlattice) that serves as a "soft" irised waveguide for x rays. High-energy ( $\approx 40$  keV) x rays are injected into the crystal at the Bragg angle to cause Bornmann anomalous transmission, yielding slow-wave accelerating fields. Particles (e.g., muons) are channeled along the crystal axis.

PACS numbers: 52.75.Dr, 41.80.-y, 61.80.Mk

An approach to the attainment of ever higher energies by extrapolating the linac to higher accelerating fields, higher frequencies, and finer structures is prompted by several considerations, including the luminosity requirement which demands the radius of the colliding-beam spot be proportionately small at high energies:  $a_0 = \pi^{-1/2} h c (f/N)^{-1/2} P e^{-2}$ , where  $f$ ,  $N$ ,  $P$ , and  $e$  are the duty cycle, total number of events, beam power, and beam energy, respectively. This approach, however, encounters a physical barrier when the photon energy becomes of the order  $h\omega = h\omega_p = mc^2 a^2 = 30$  eV ( $a =$  the fine-structure constant), corresponding to wavelength (scale length)  $\lambda \approx 500$  Å. The metallic wall begins to absorb the photon strongly, where  $\omega_p$  is the plasma frequency corresponding to the crystal electron density. In addition, since the wall becomes not perfectly conducting for  $h\omega \geq mc^2 a^2$ , the longitudinal component of fields becomes small and the photon goes almost straight into the wall (a soft-wall regime). As the photon energy  $h\omega$  much exceeds  $mc^2 a^2$  and becomes  $\geq mc^2 a$ , however, the metal now ceases to be opaque. The mean free path of the photon is given by Bethe-Bloch theory as  $l = (3/2^3 \pi) \times a_B^{-2} a^{-1} n^{-1} (h\omega/Z_{\text{eff}}^2 R)^{3/2}$ , where  $a_B$  is the Bohr radius,  $n$  the electron density,  $Z_{\text{eff}}$  the effective charge of the lattice ion, and  $R$  the Rydberg energy.

In the present concept the photon energy is taken at the hard x-ray range of  $h\omega = mc^2 a$  and the linac structure is replaced by a crystal structure, e.g., silicon or GaAs-AlAs. (A similar bold endeavor was apparently undertaken by Hofstadter already in 1968.<sup>1</sup>) Here the crystal axis provides the channel through which accelerated particles propagate with minimum scattering (channeling<sup>2</sup>) and the x rays are transmitted via the Bornmann effect (anomalous transmission<sup>3,4</sup>) when the x rays (wavelength  $\lambda$ ) are injected in the  $xz$  plane with a

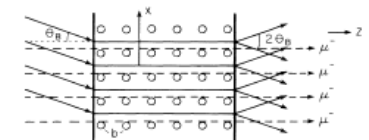
where  $b$  is the transverse lattice constant and later  $a$  the longitudinal lattice constant ( $a \approx b$ ) (see Fig. 1). The row of lattice ions (perhaps with inner-shell electrons) constitutes the "waveguide" wall for x rays, while they also act as periodic irises to generate slow waves. A superlattice<sup>5</sup> such as Ge<sub>2</sub>Si<sub>1-c</sub>S<sub>2</sub> (in which the relative concentration  $c$  ranges from 0 to 1 over 100 Å or longer in the longitudinal  $z$  direction) brings in an additional freedom in the crystal structure and provides a small Brillouin wave number  $k_z = 2\pi/s$  with  $s$  being the periodicity length. We demand that the x-ray light in the crystal channel walls becomes a slow wave and satisfies the high-energy acceleration condition

$$\omega/(k_z + k_x) = c, \quad (2)$$

where  $\omega$  and  $k_z$  are the light frequency and longitudinal wave number.

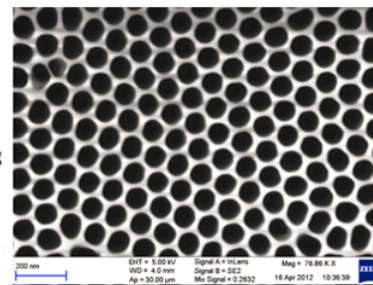
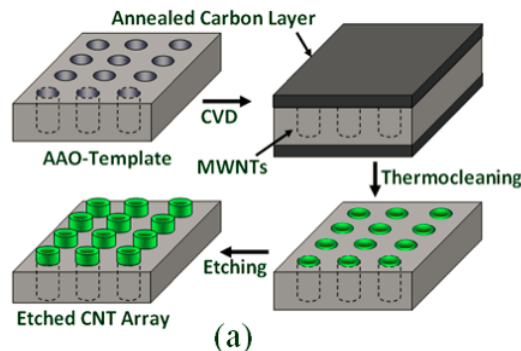
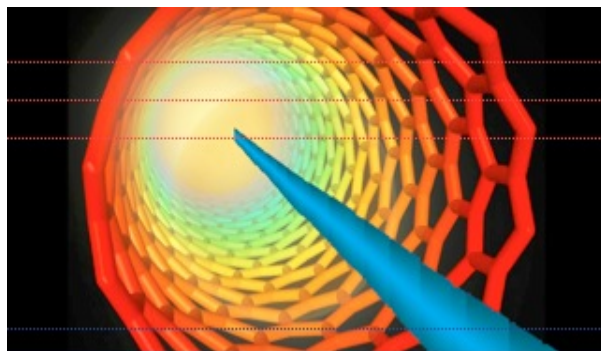
The energy loss of moving particles in matter is due to ionization, bremsstrahlung, and nuclear collisions. We can show<sup>6</sup> that a channeled high-energy particle moving fast in the  $z$  direction oscillates in the  $xy$  plane according to the Hamiltonian

$$H = \frac{1}{2m} (p_x^2 + p_y^2) + V(x, y), \quad (3)$$

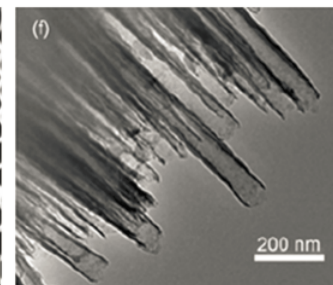




# Why Nanotubes



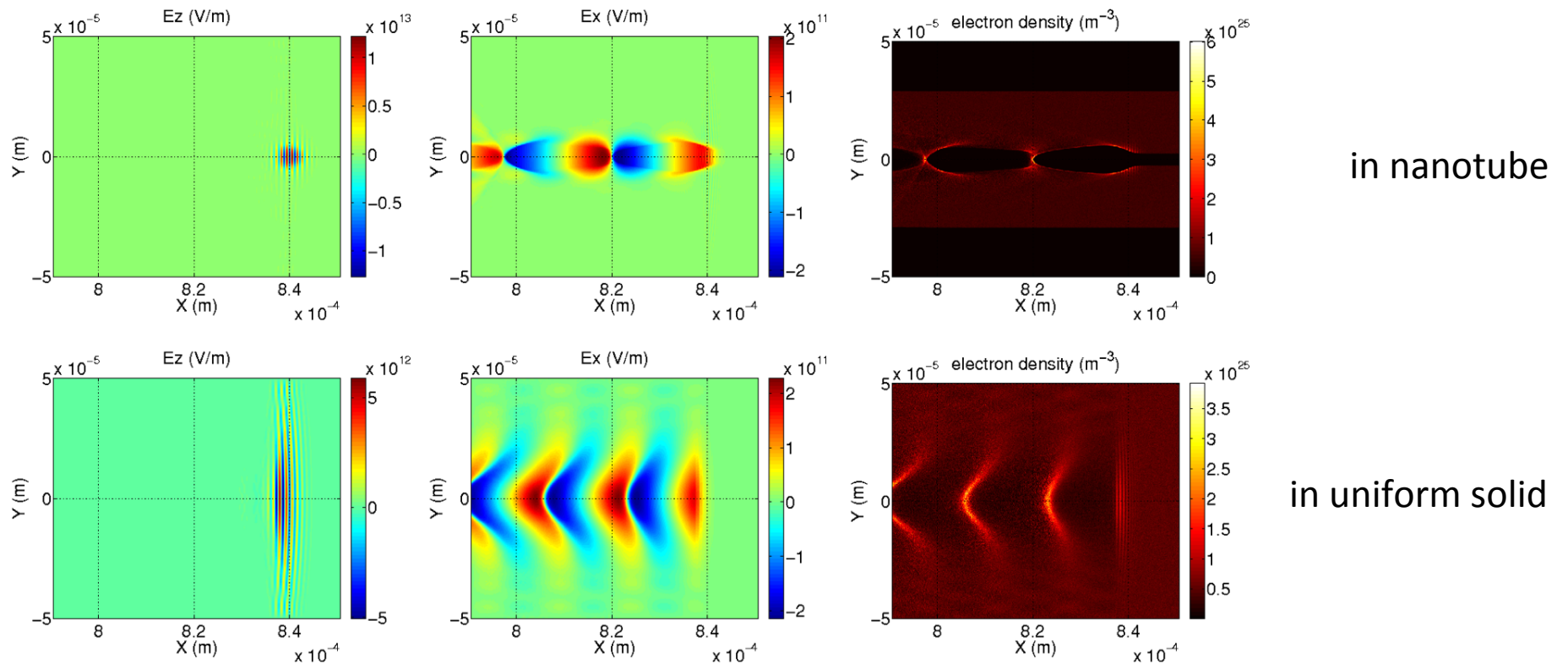
(b)



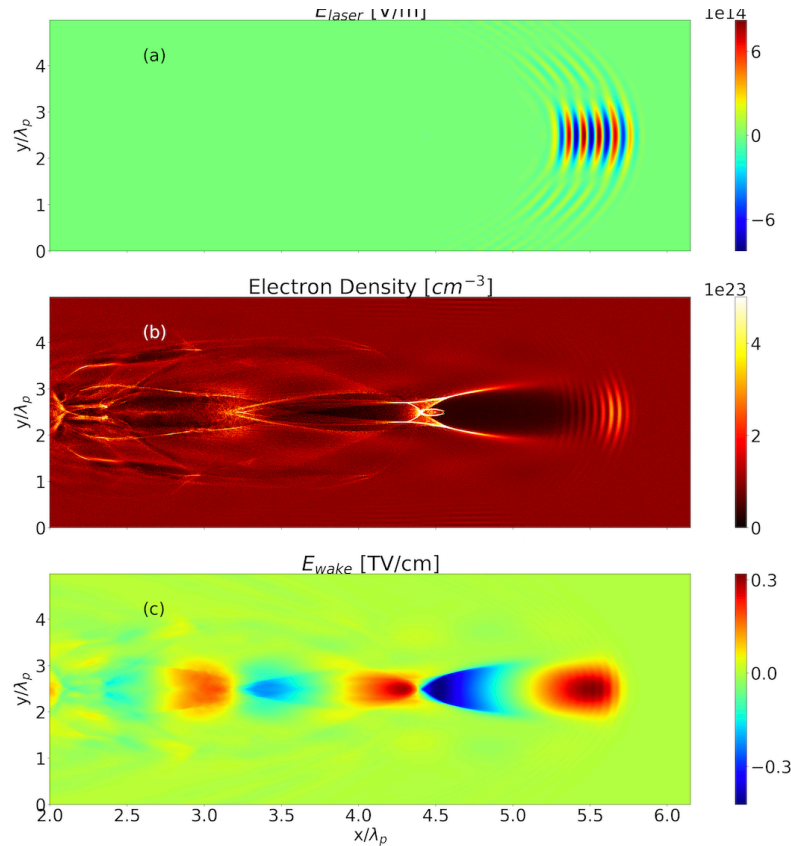
(c)

- High density ↔ Higher acceleration gradient ( $\sim \text{TeV} / \text{cm}$ )
- Provides external structure to guide laser and electron beam
- No slowdown of electrons by collisions
- Intact for time of ionization (fs)

# X-ray LWFA in a tube vs. uniform solid



A few-cycled 1keV X-ray pulse ( $a_0 \sim O(1)$ ), causing 10TeV/m wakefield in the tube  
more strongly confined in the tube  
cf: uniform solid



Ion lattice modes (s.a. polaritons) Included\*) :

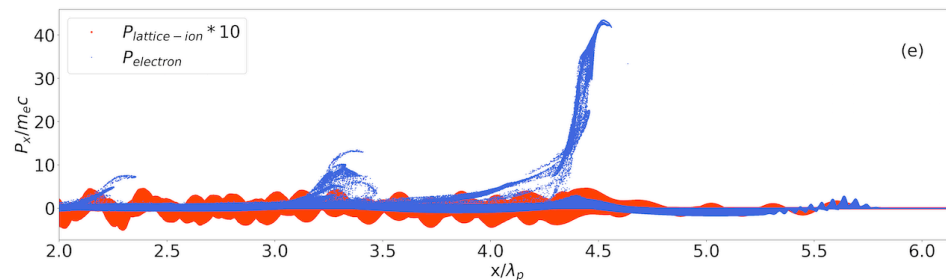
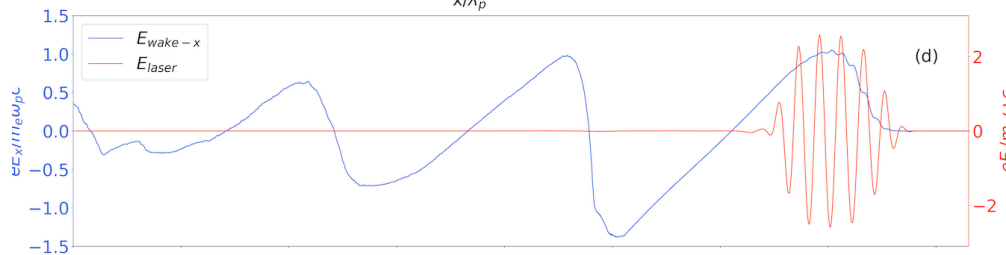
basically all actions via plasmons

(S. Hakimi et al. , 2019)

\*)

$$\epsilon(k, \omega) = 1 - \frac{\omega_{pi}^2}{\omega^2 - \omega_{TO}^2} - \frac{\omega_{pe}^2}{\omega^2 - k_x^2 v_e^2} .$$

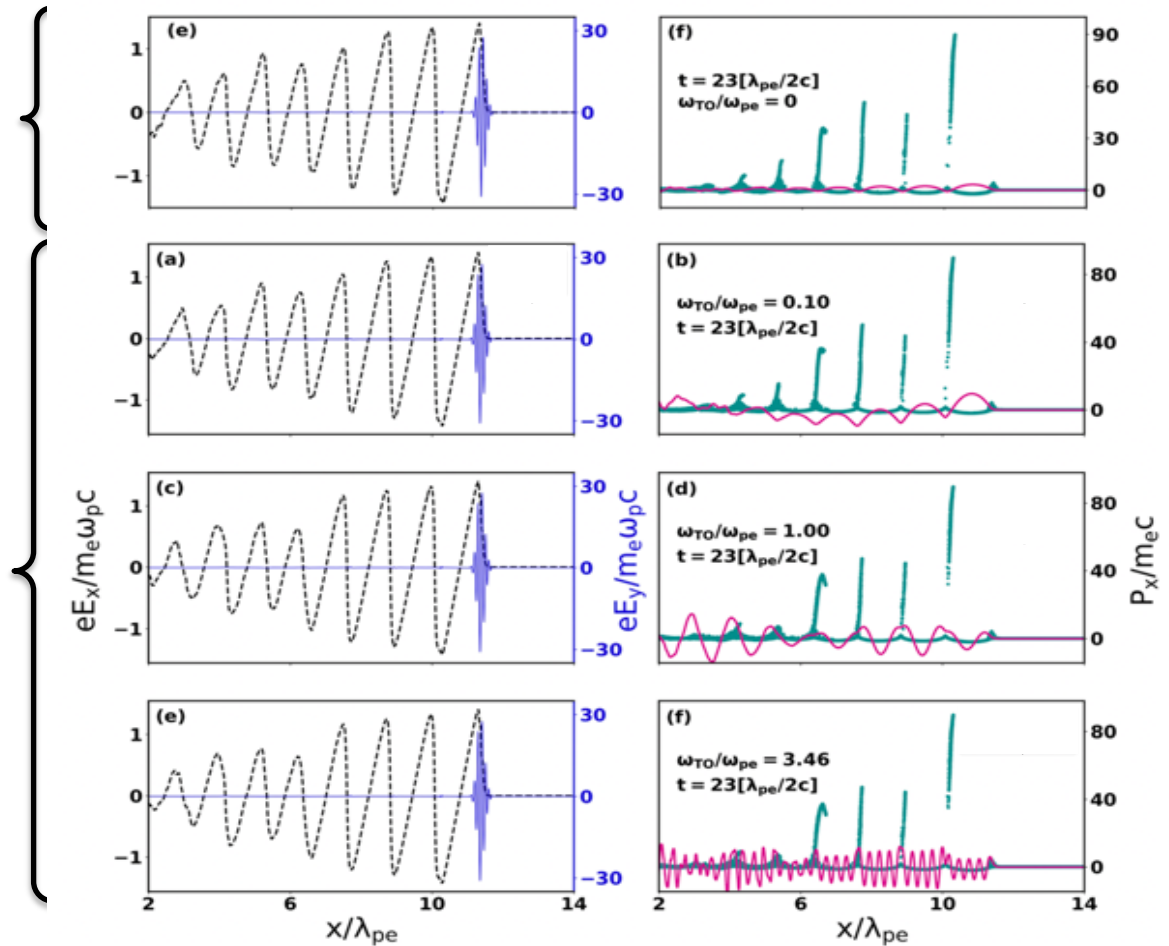
(Tajima and Ushioda, 1978)



# Effects of Optical Phonons

without  
optical phonon

with  
optical phonon



**X-ray** in nanotube  $\leftrightarrow$

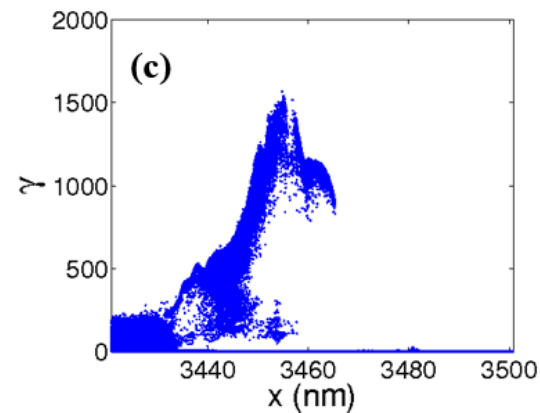
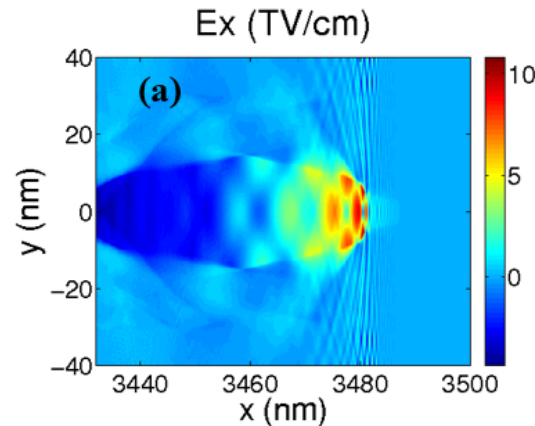
**optical laser** in mm plasma guide

Acceleration process are **self-similar**:

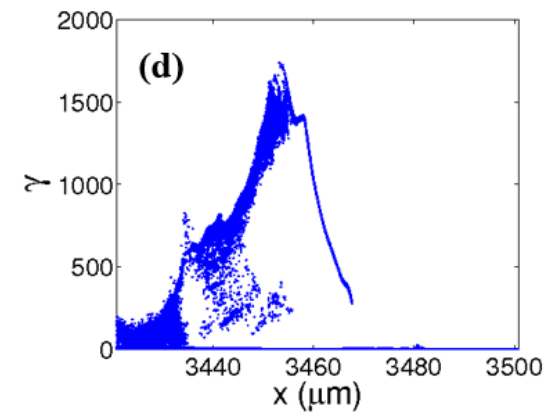
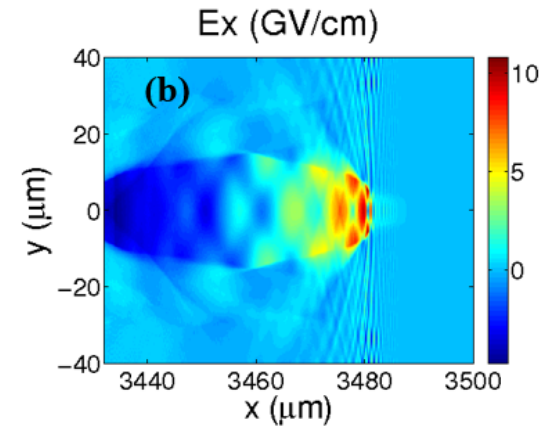
**Xray** in **micron** (short),  
while **optical laser** in **mm**  
(longer)

But **beam emittance** and  
**betatron radiation**: quite  
different (not self-similar)

X-ray laser



Optical laser

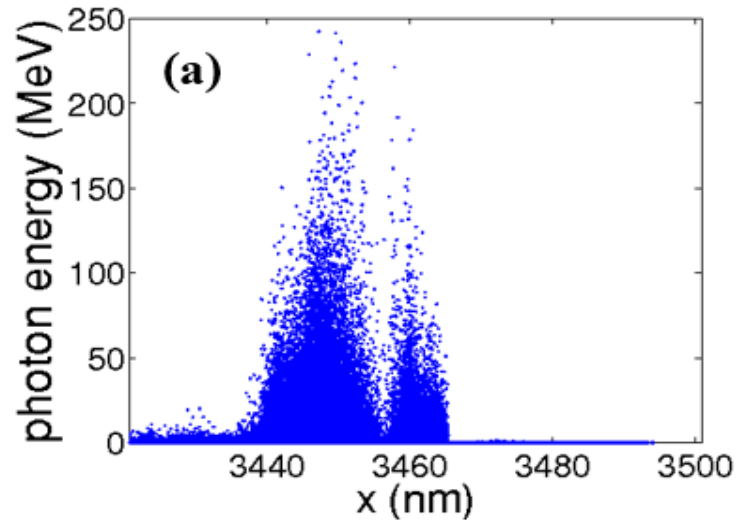


Distributions of (a)(b) **wakefield** and (c)(d) electron energy induced by (a)(c) the **X-ray laser** pulse and (b)(d) **optical laser** in a tube when  $a_0=10$

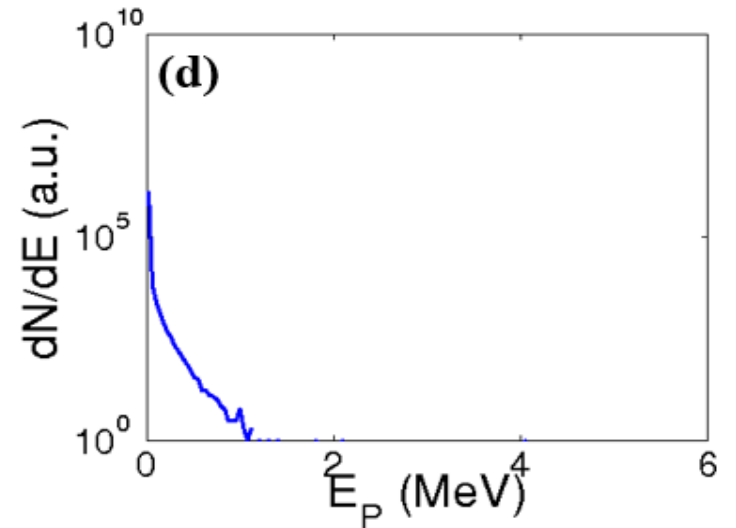
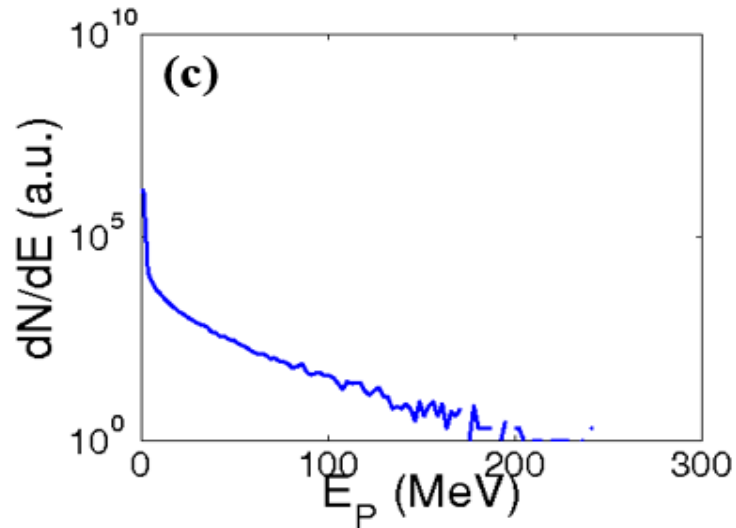
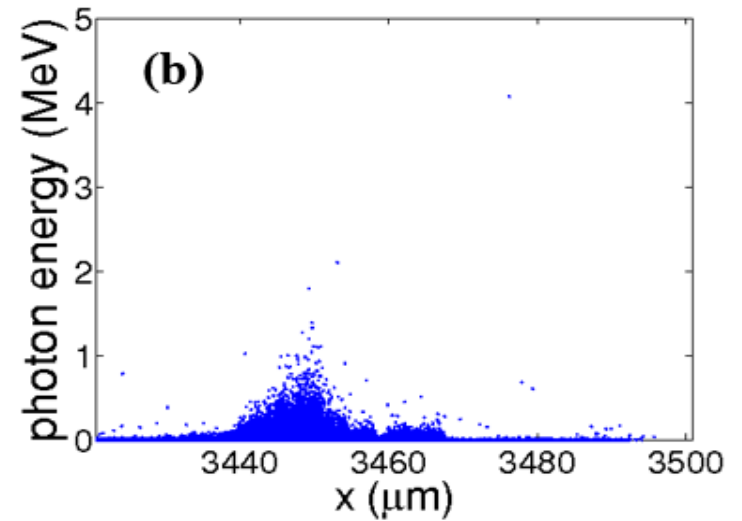


# Betatron radiation

X-ray laser



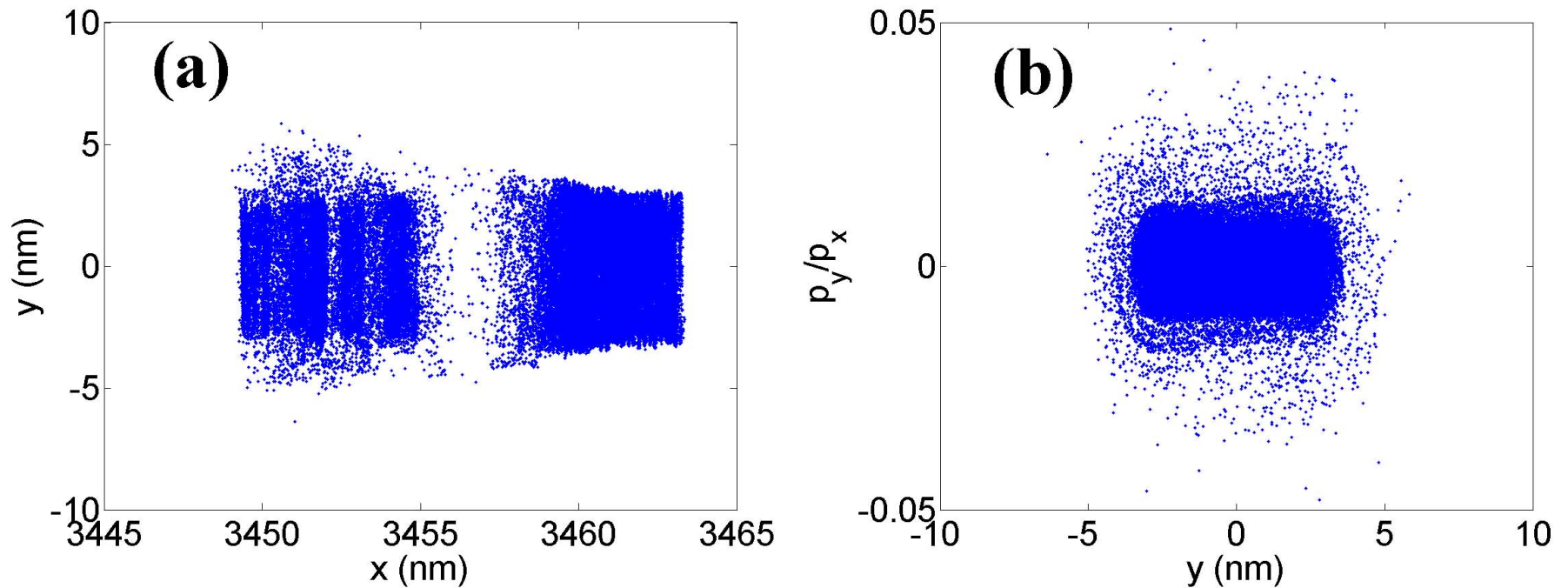
Optical laser



(a)(b) Photon energy distributions and (c)(d) photon energy spectrum in the (a)(c)X-ray driven case and (b)(d) 1eV optical laser driven case in a tube.

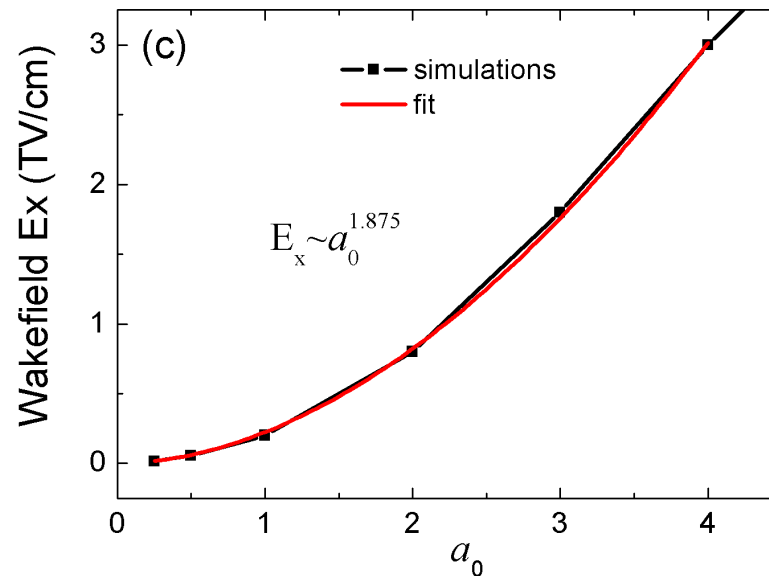
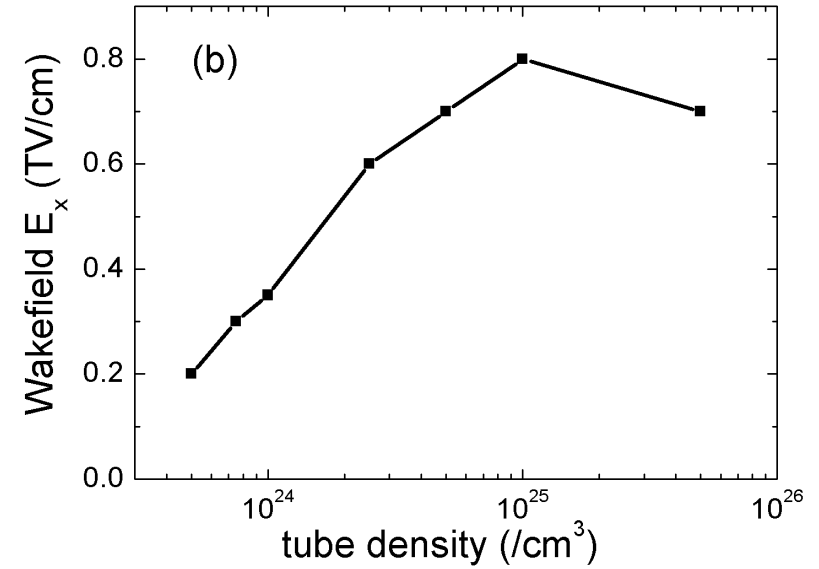
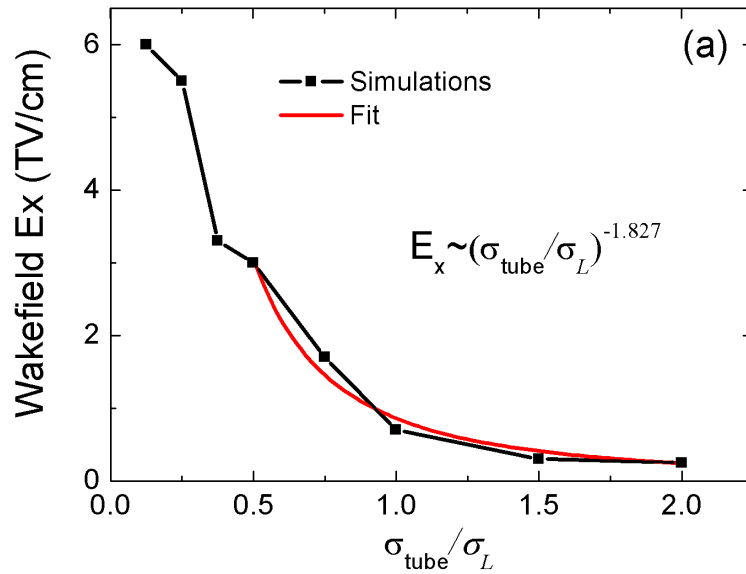
# Beam emittance reduction

X-ray laser driven wakefield  
emittance reduction (much smaller transverse dimension)

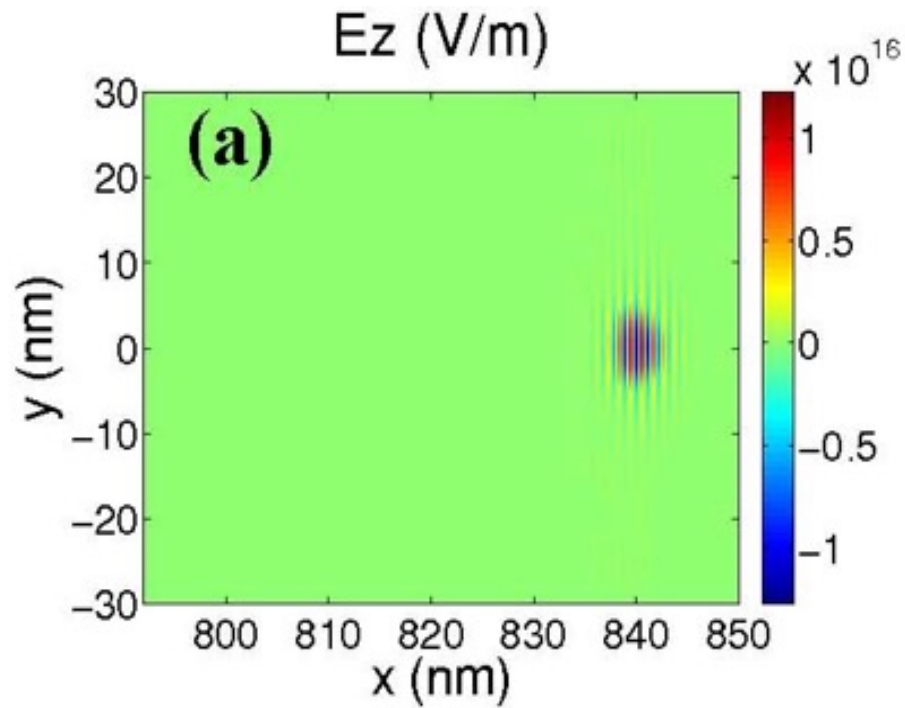


(a) The space distribution ( $x, y$ ) and (b) the transverse phase space ( $y, p_y/p_x$ )

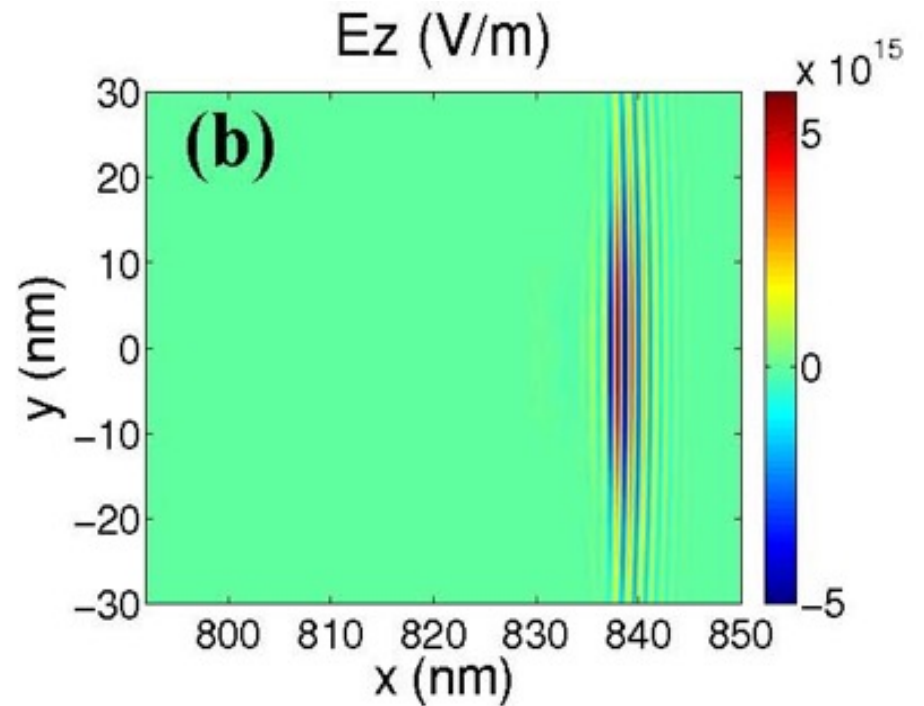
# Wakefield strength: tube size, wall density, laser intensity



# Nanotube $\leftrightarrow$ no hole

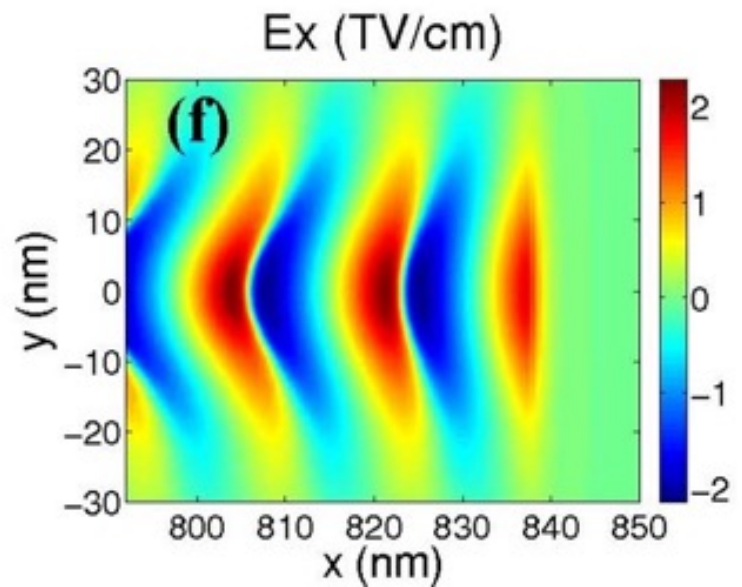
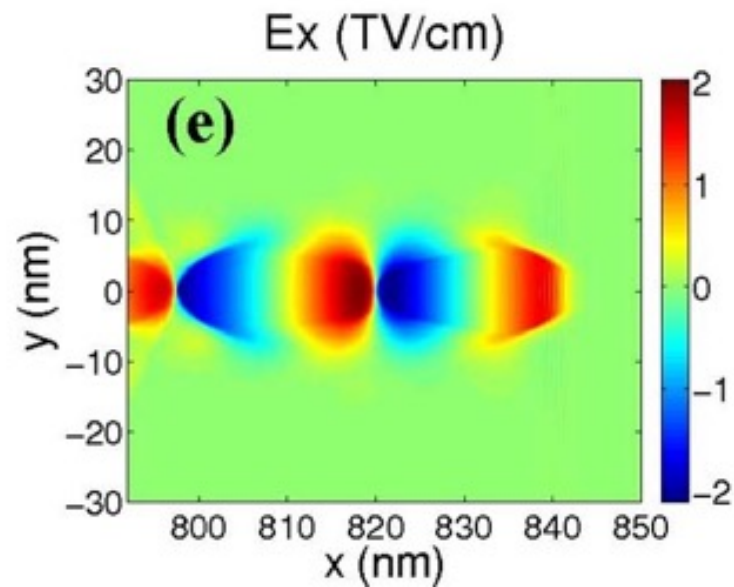
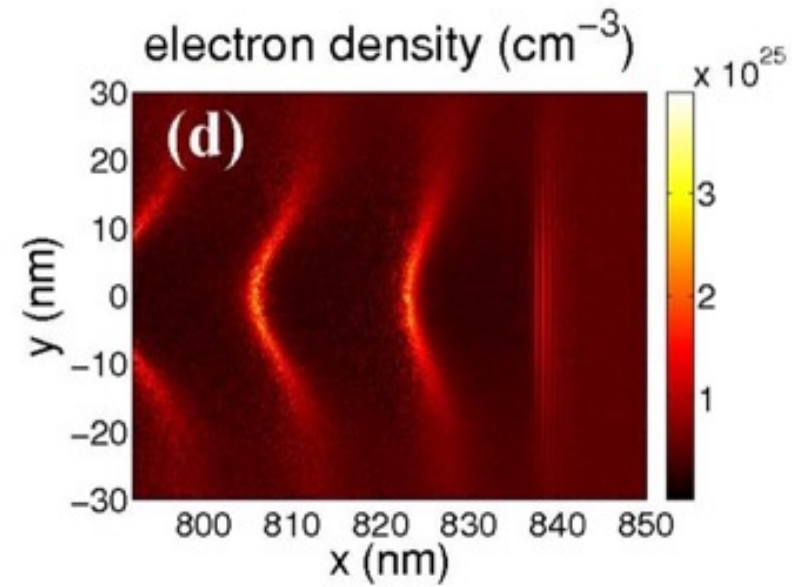
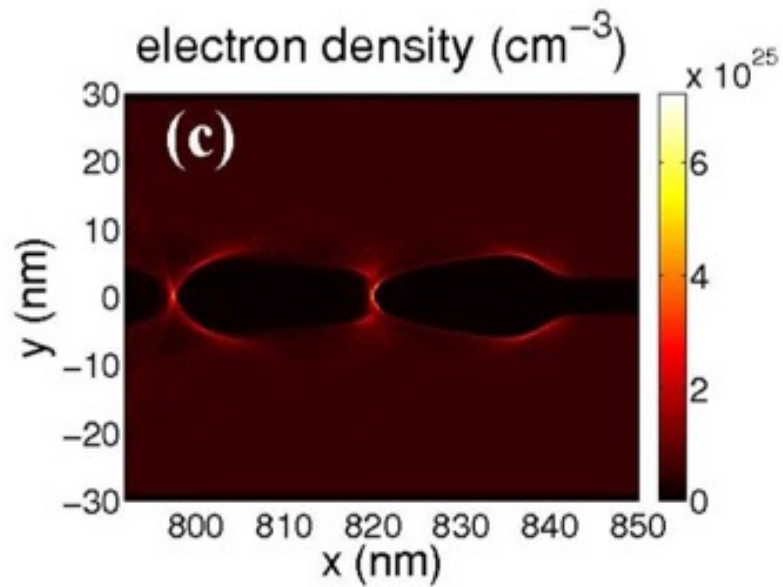


Nanotube (5 nm radius)



No nanotube

# Nanotube $\leftrightarrow$ No tube





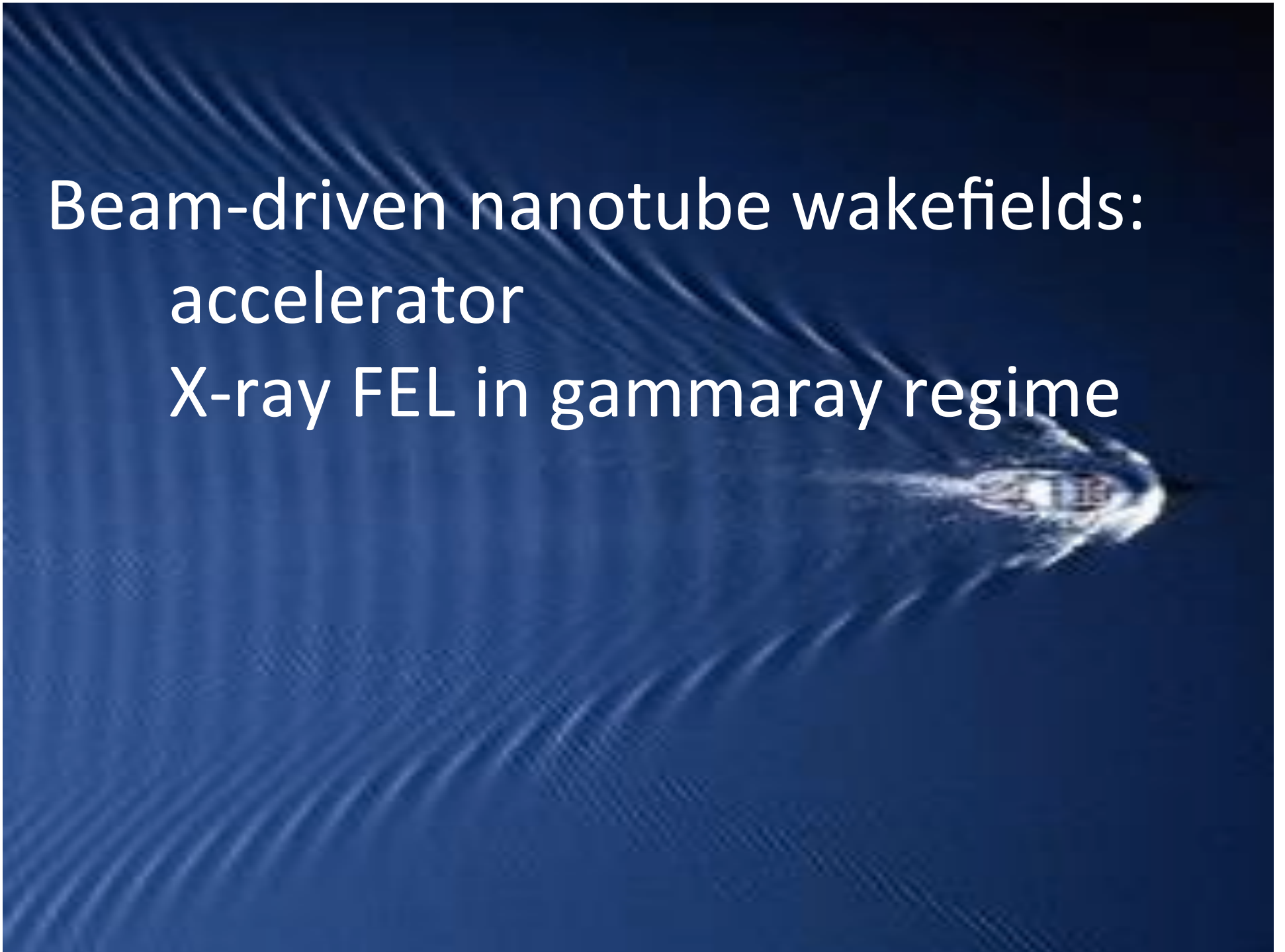
$$\alpha = \frac{\hbar^2}{ec}$$

# Fermi's PeV Accelerator

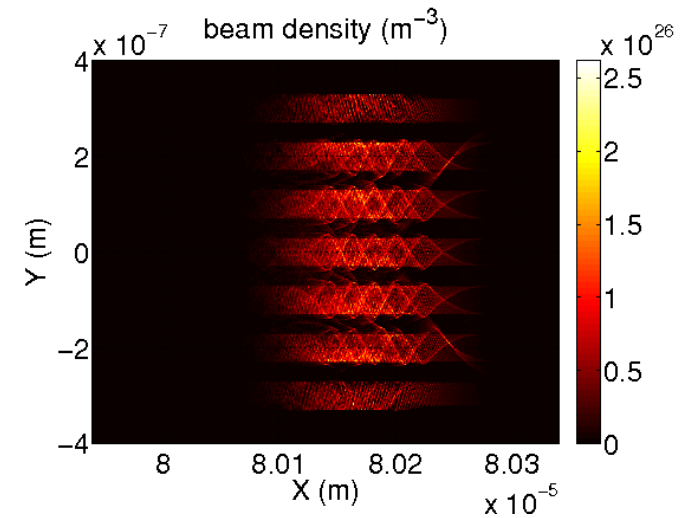
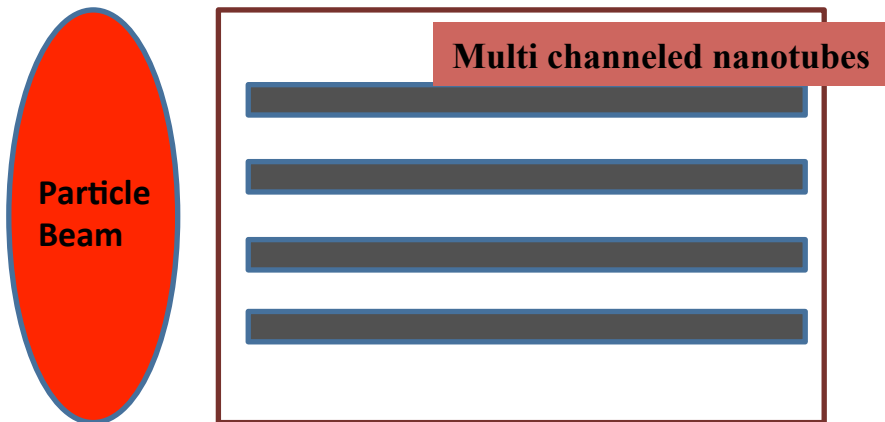
Now

TeV on a chip → PeV over 10m → check superstring theory?

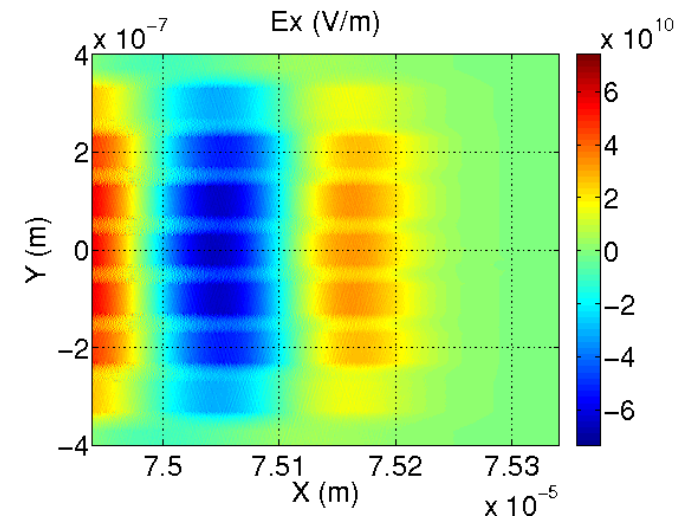
Beam-driven nanotube wakefields:  
accelerator  
X-ray FEL in gammaray regime



# E-Beam driven case



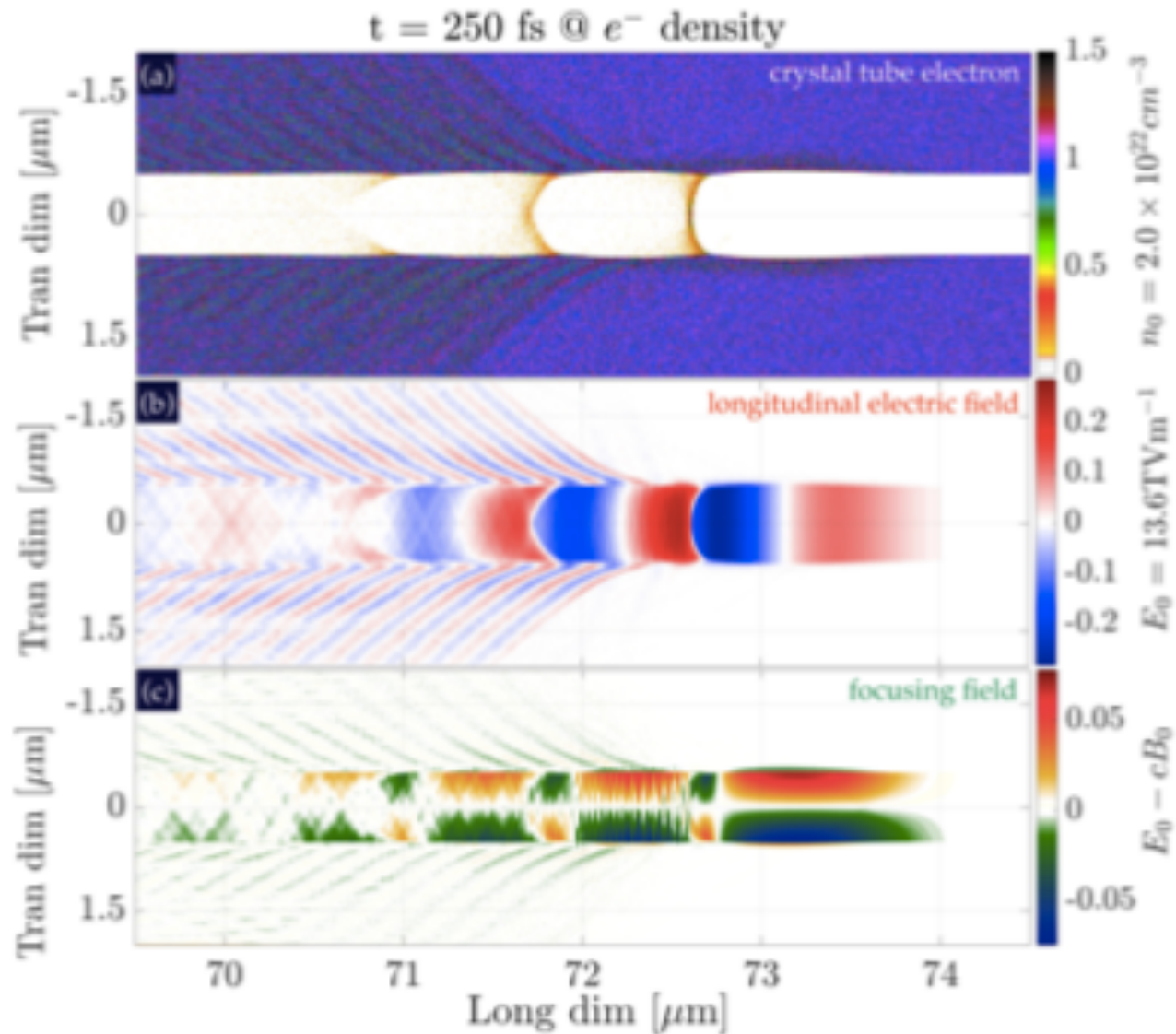
Beams in the tube



Beam-driven wakefield



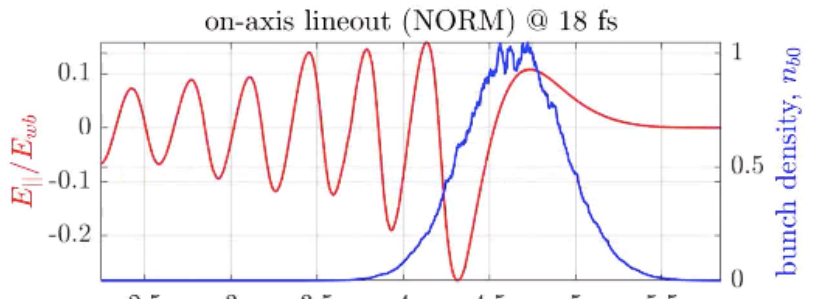
# E-beam driven wakefield in nanotube



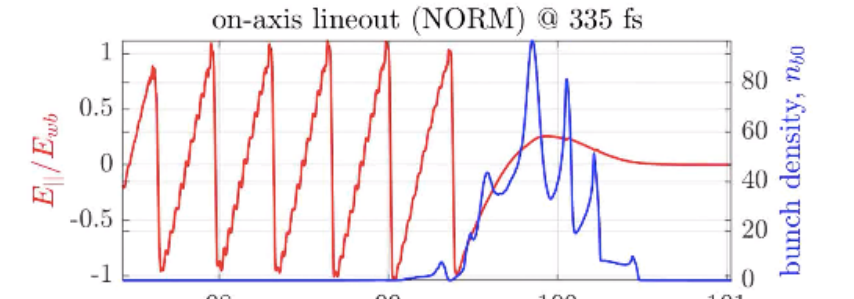
A. Sahai, (2020) supported by U. Colorado at Denver, Boulder RMACC

# Strong self-focus and self-modulation of electron beam in nanotube

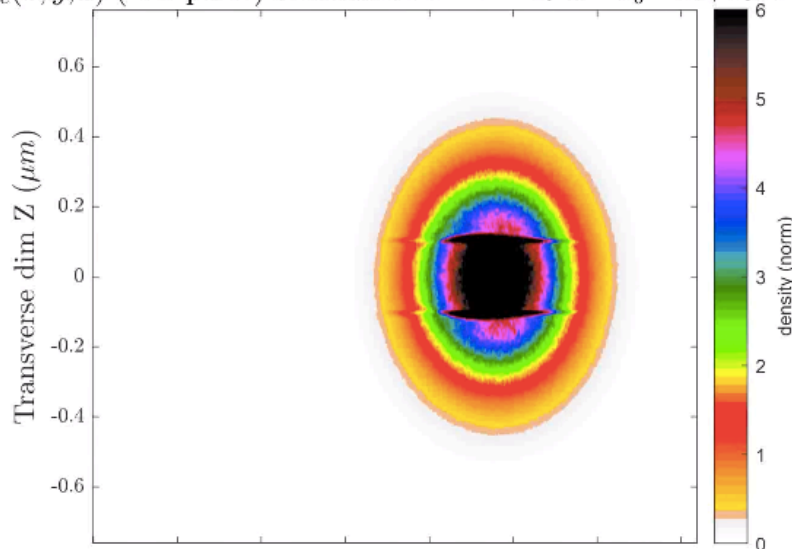
early



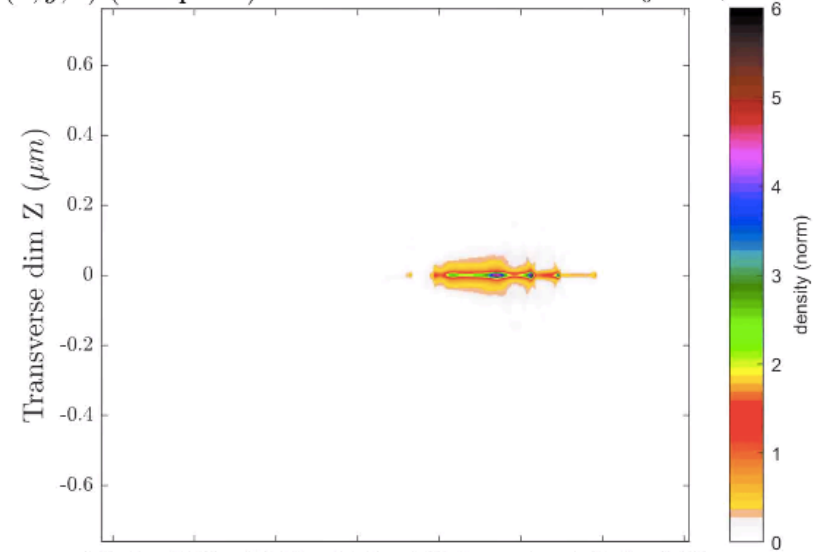
later



$n_e(x, y, z)$  (X-Z plane) centered in Y - t = 15 fs -  $n_0 = 2e+28m^{-3}$



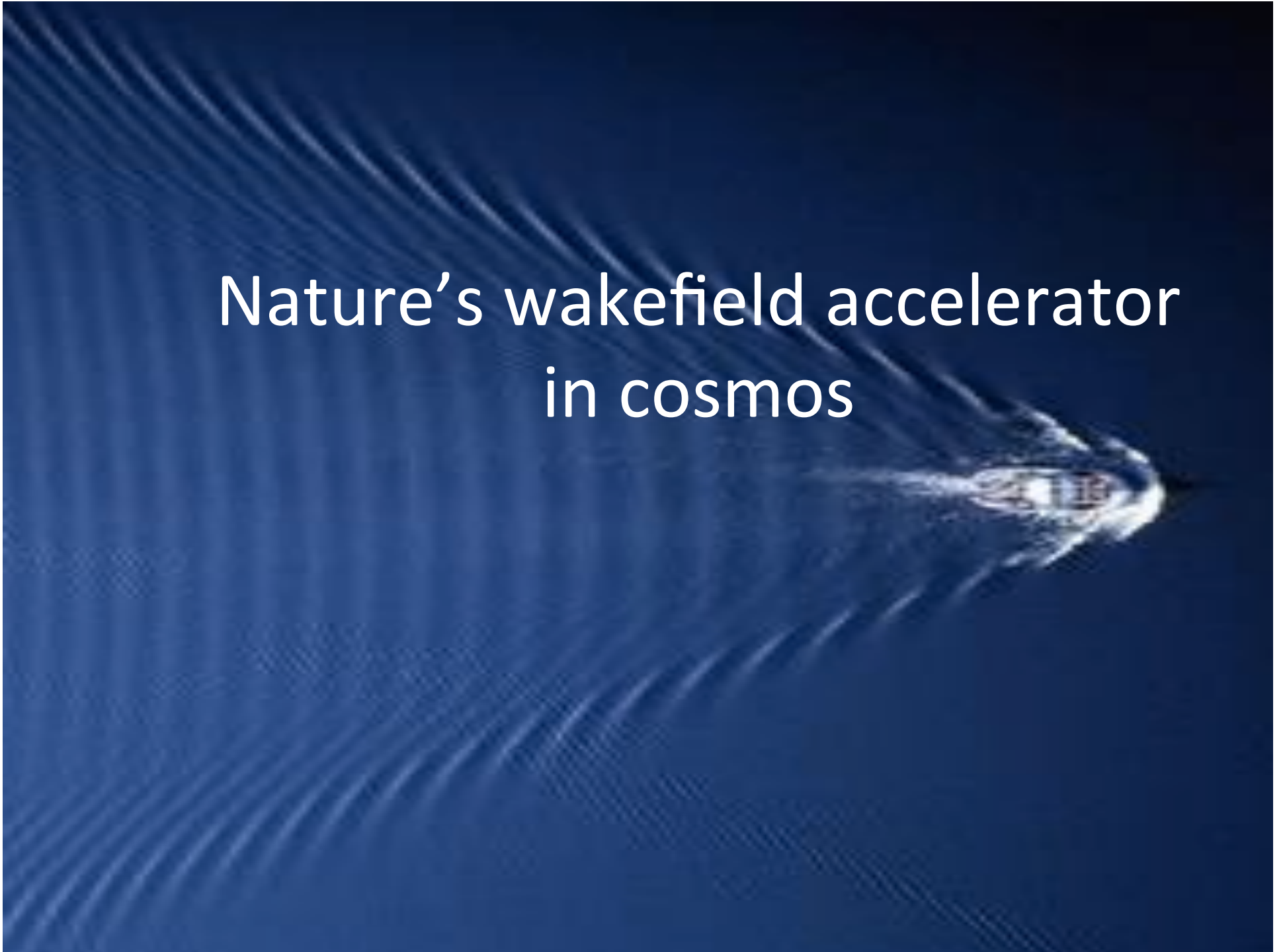
$(x, y, z)$  (X-Z plane) centered in Y - t = 335 fs -  $n_0 = 2e+28m^{-3}$



Highly compressed



# Nature's wakefield accelerator in cosmos



# Ultrahigh Energy Cosmic Rays (UHECR)

Fermi mechanism runs out of steam  
beyond  $10^{19}$  eV

due to *synchrotron radiation*

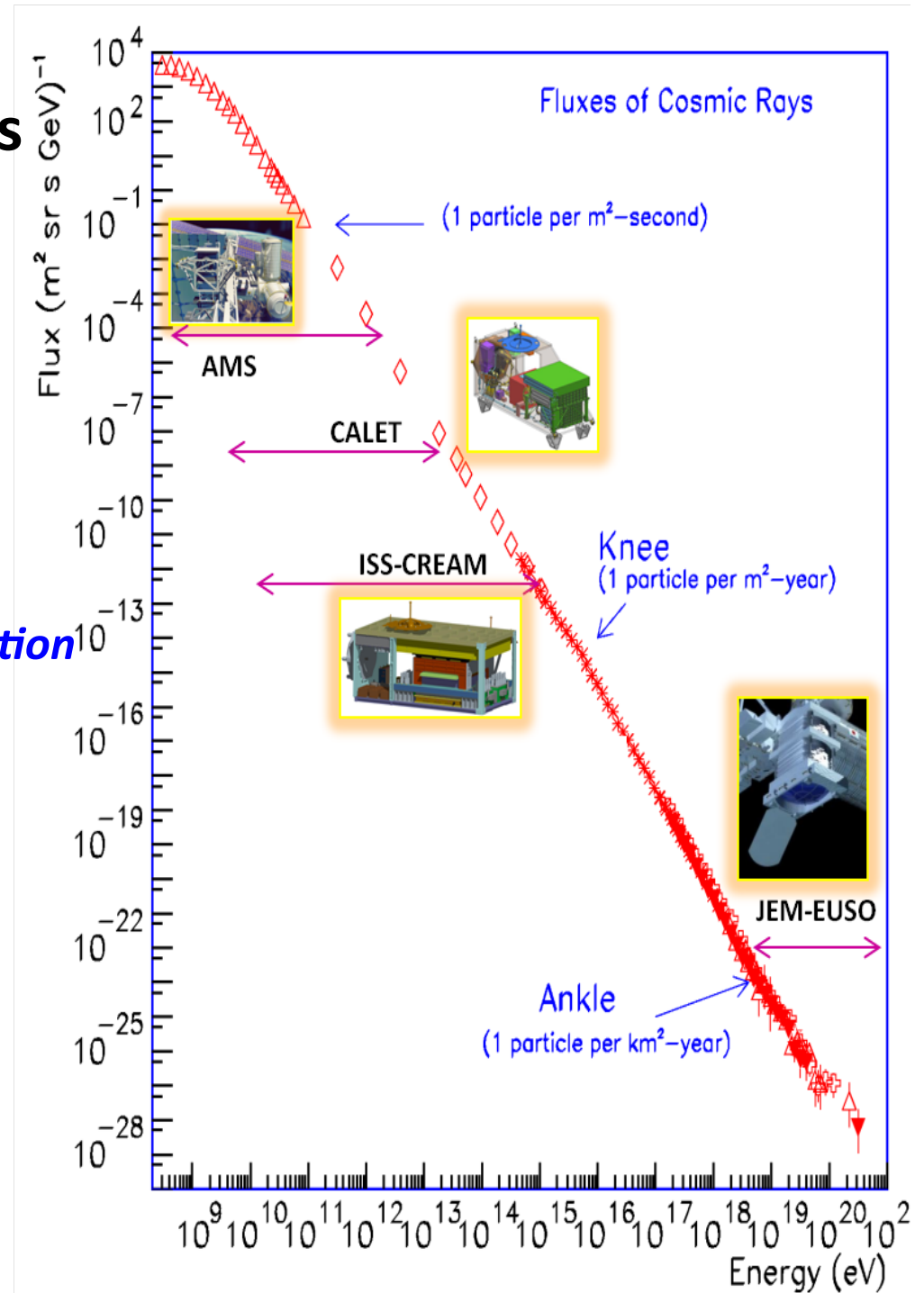
Wakefield acceleration

comes in rescue

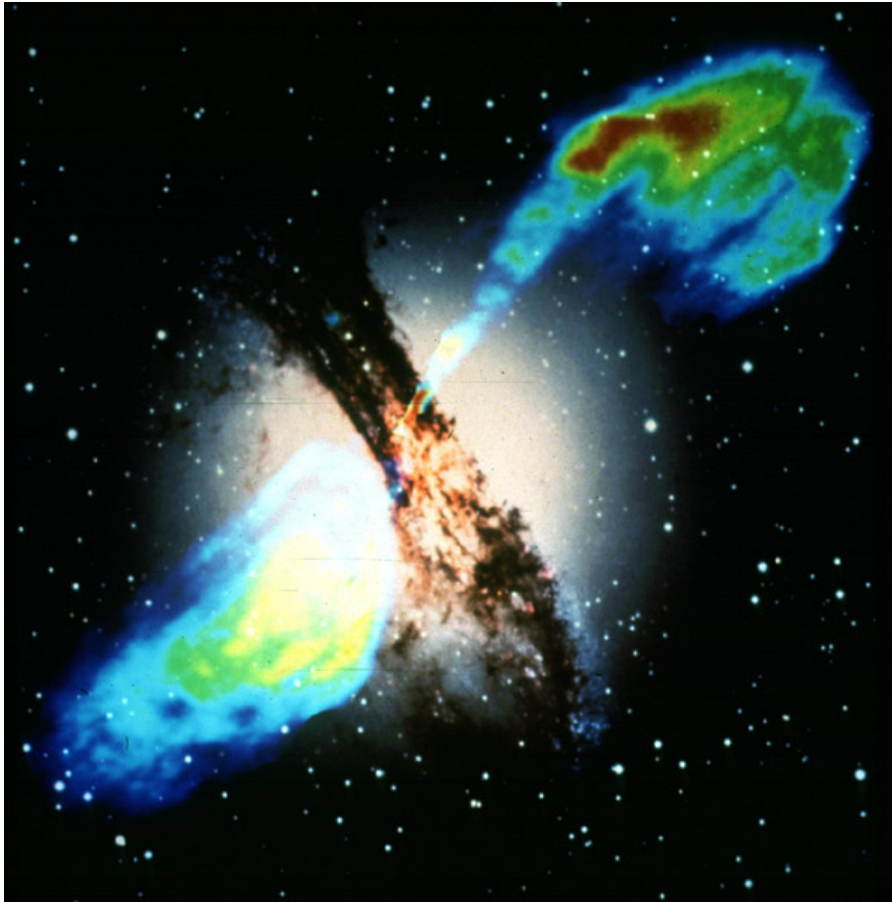
prompt, intense, *linear acceleration*

small synchrotron radiation

radiation damping effects?



# Cen A

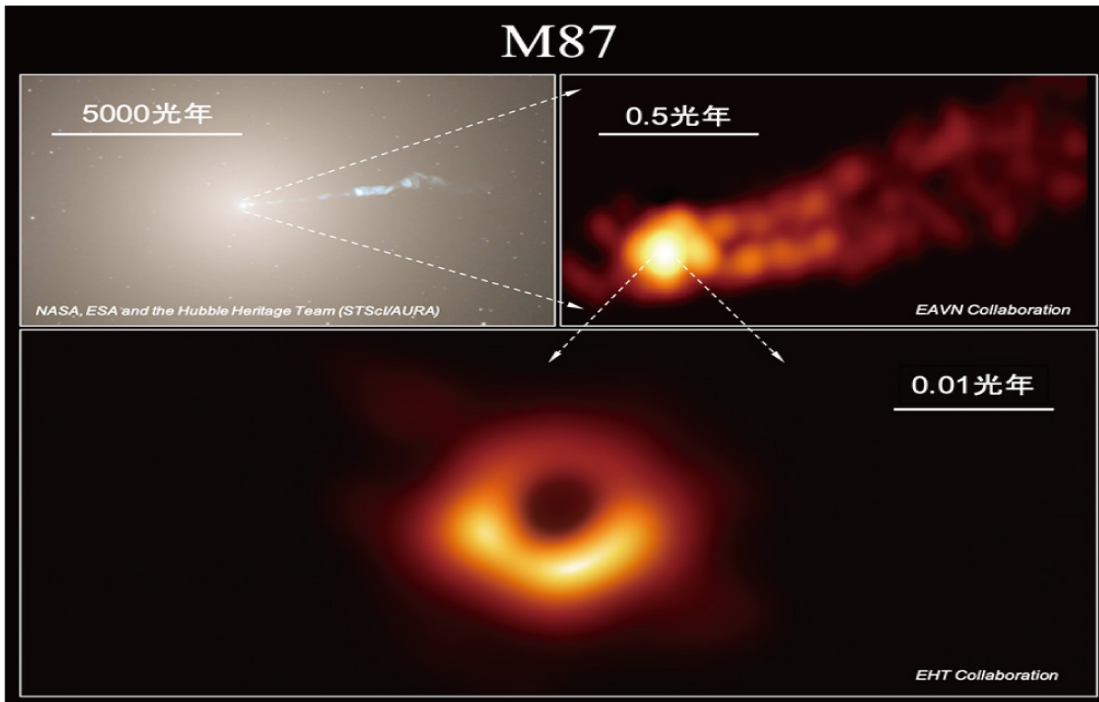


- Distance : 3.4Mpc
- Radio Galaxy
  - Nearest
  - Brightest radio source
- Elliptical Galaxy
- Black hole at the center w/  
relativistic jets

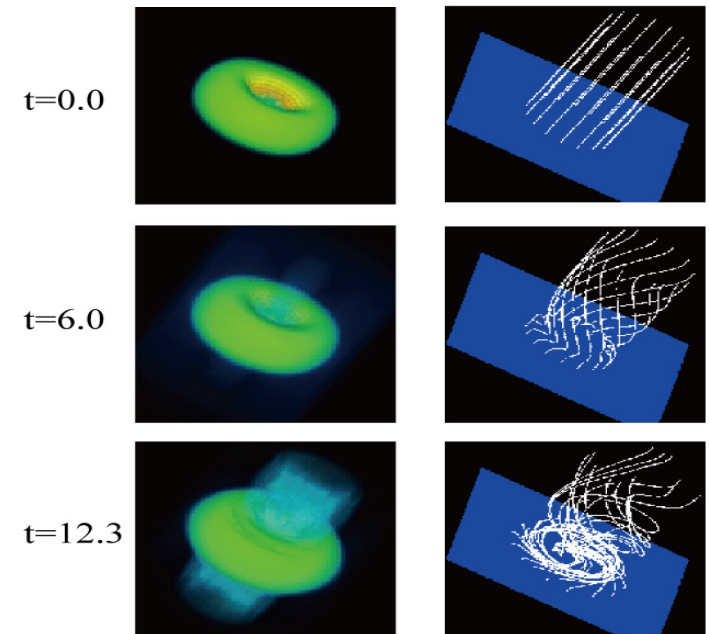
# Discovery of Blackhole and Prediction

M87 blackhole: by **Event Horizon Telescope (2019)**

Prediction: **Tajima and Shibata**  
“**Plasma Astrophysics**” (1997)

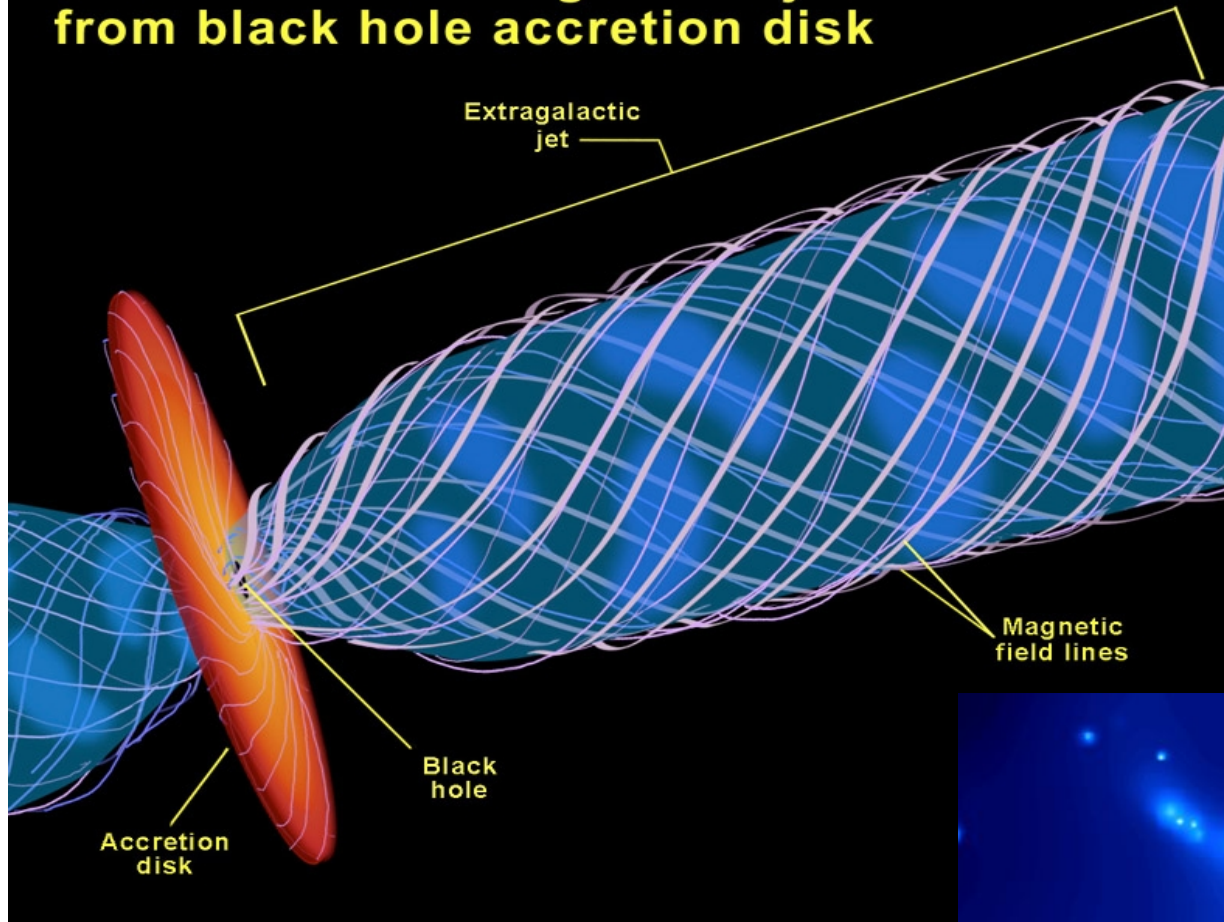


3D Structure of Disk and Jet





## Formation of extragalactic jets from black hole accretion disk



Fermi's 'Stochastic Acceleration'  
(large synchrotron radiation loss)



Coherent **wakefield** acceleration  
(no limitation of the energy)

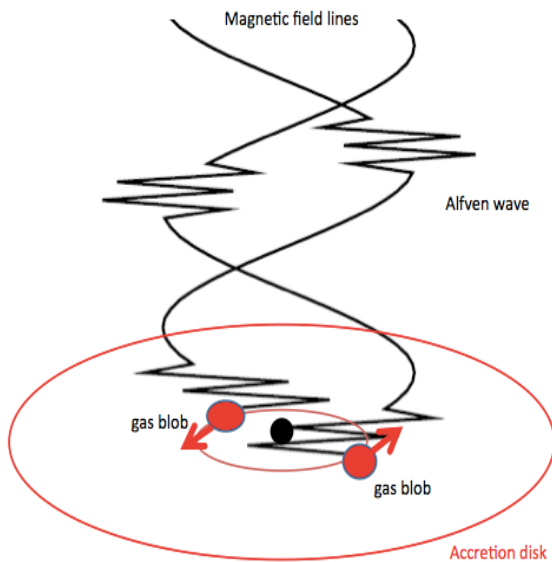


### Nature's **LWFA** : Blazar jets

extreme high energy cosmic rays ( $\sim 10^{21}$  eV)  
episodic  $\gamma$ -ray bursts observed  
consistent with **LWFA** theory



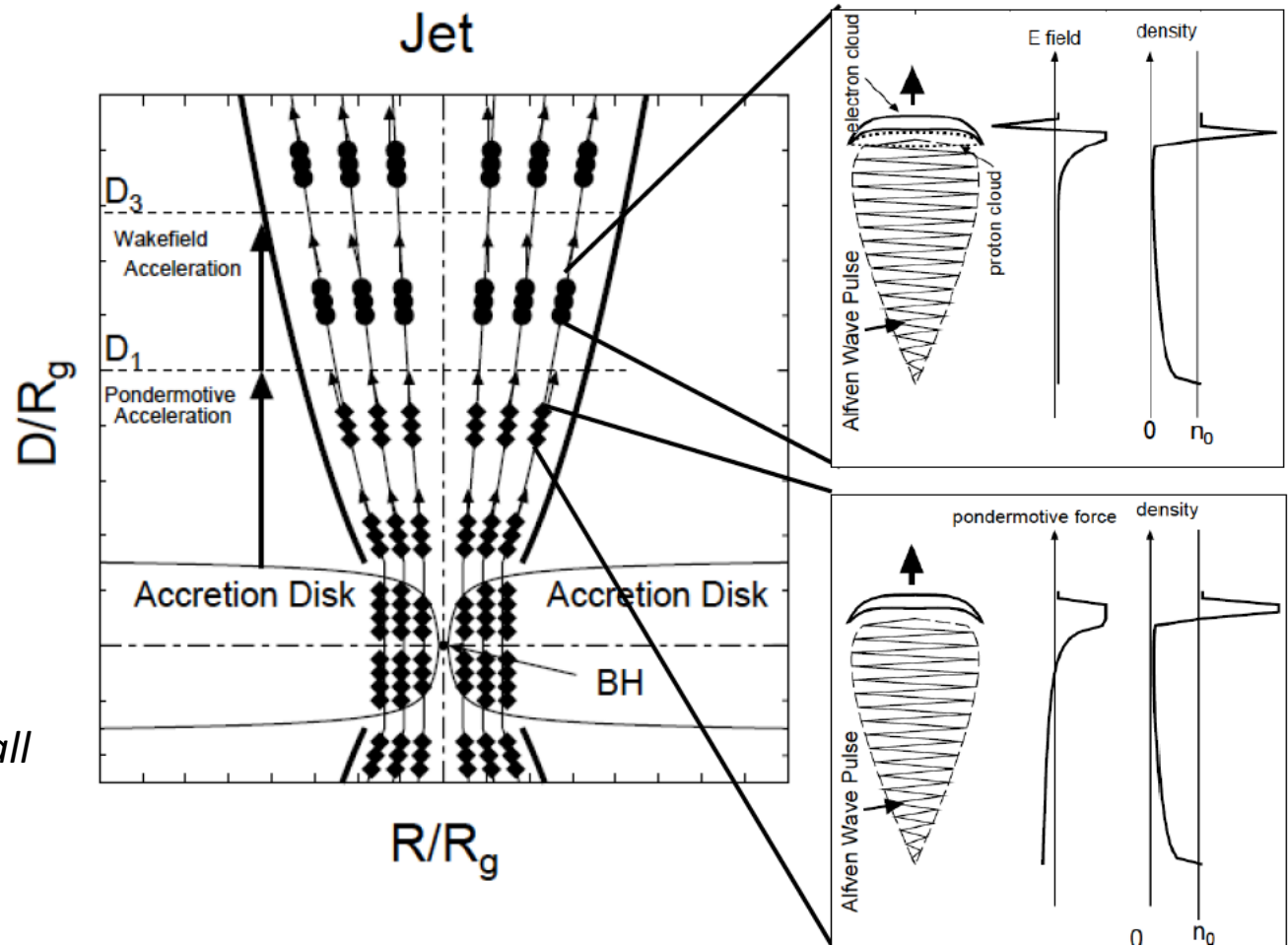
# Astrophysical **wakefield** acceleration: Superintense **Alfven Shock** in the Blackhole Accretion Disk toward ZeV Cosmic Rays ( $a_0 \sim 10^6 - 10^{10}$ , large spatial scale)



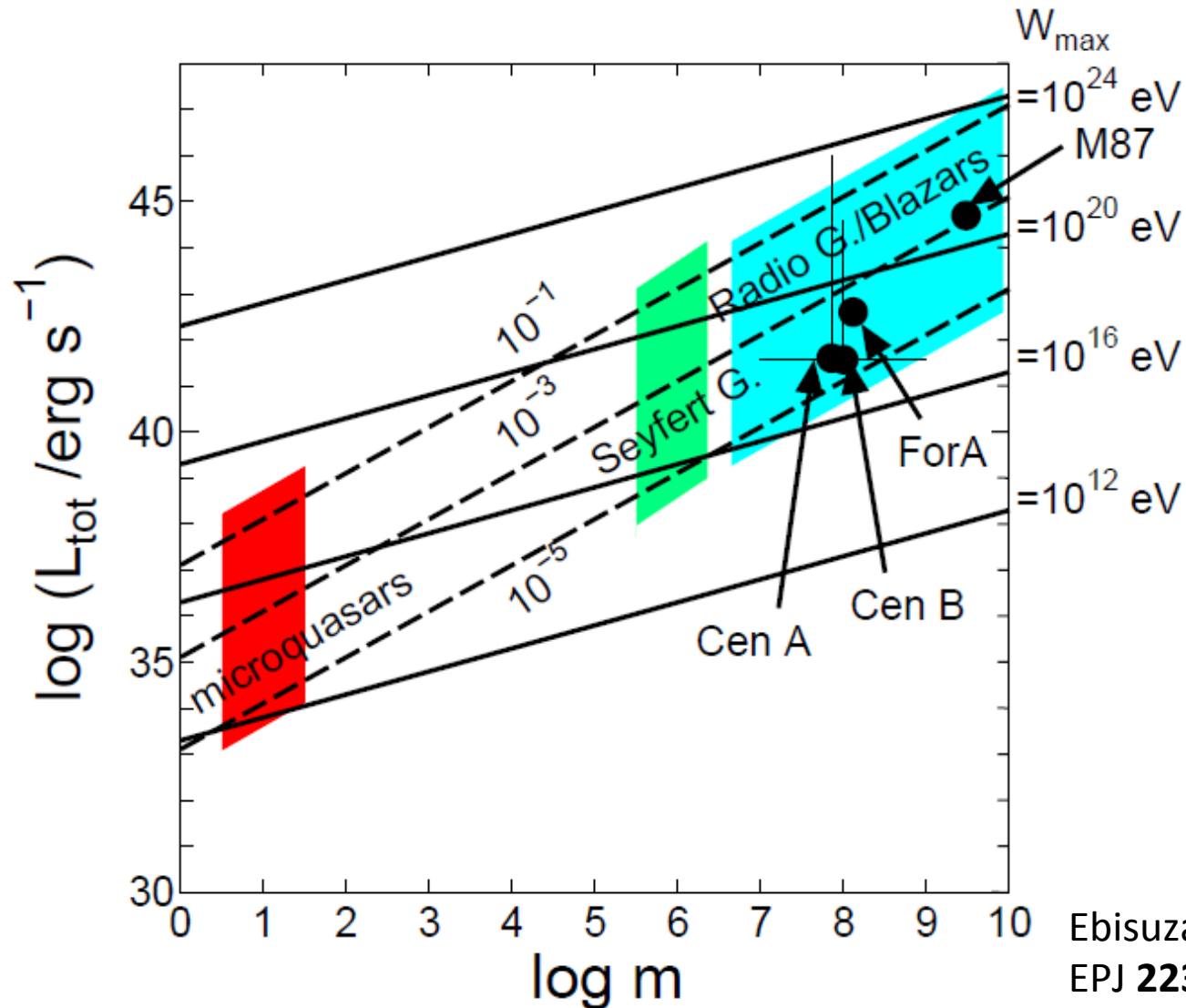
$$a_0 = eE_0 / mc\omega_0 \gg 1$$

$E_0$ : modest

$\omega_0$ : extremely small



# Comic ray acceleration and $\gamma$ -ray emission: Summary



# Blazar shows anti-correlation between $\gamma$ burst flux and spectral index

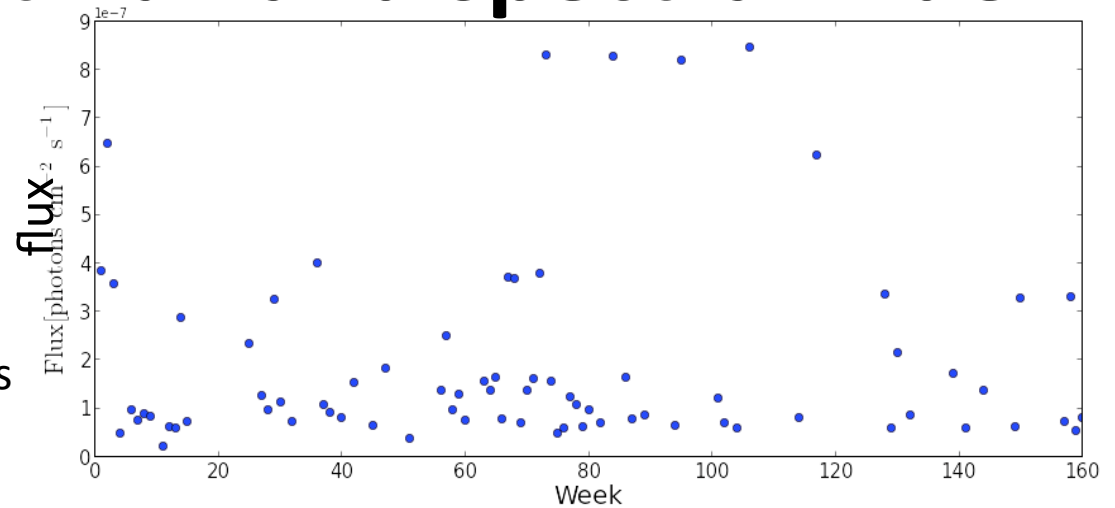
Blazar: AO0235+164

$M \sim 10^8 M_{\text{Sun}}$

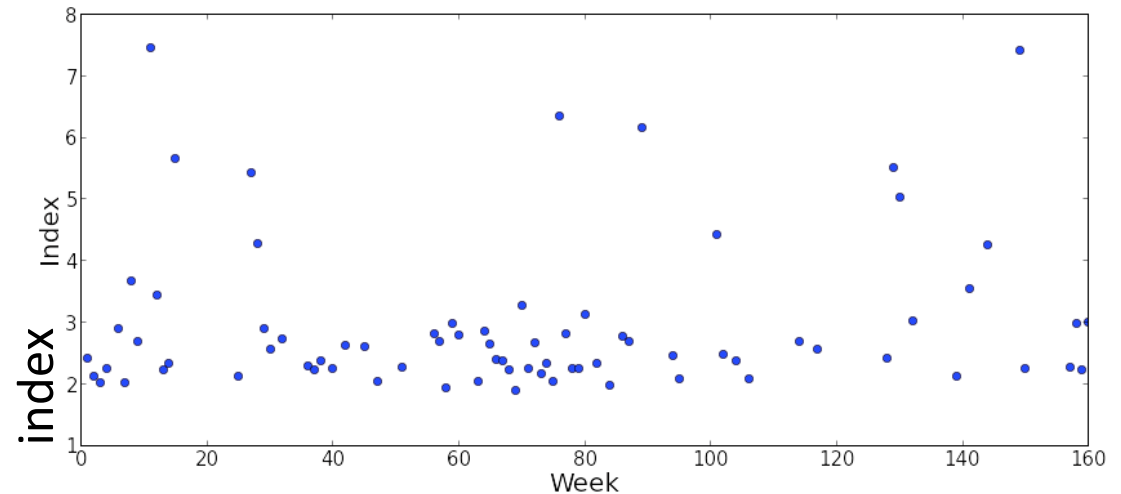
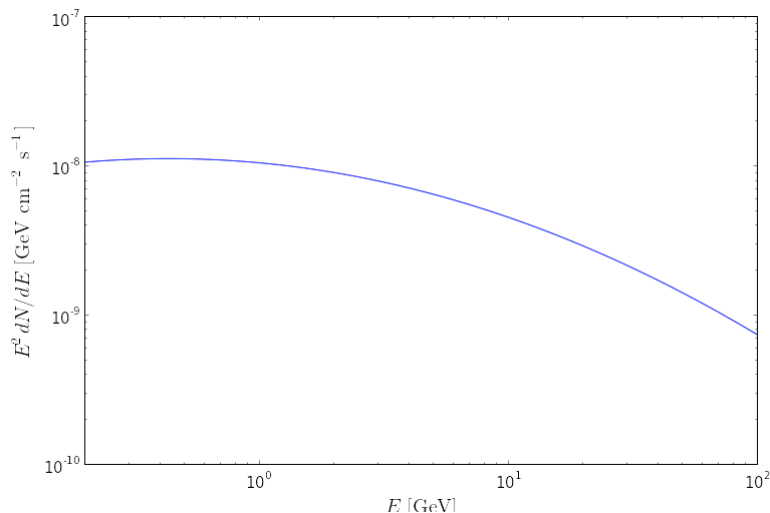
Rise time < week (less than a unit),  
Period between bursts  $\sim > 10$  weeks

Spectral index  $\Rightarrow 2$

( $\sim$  Ebisuzaki/Tajima theory)



$\rightarrow$  all quantitatively consistent with Wakefield theory



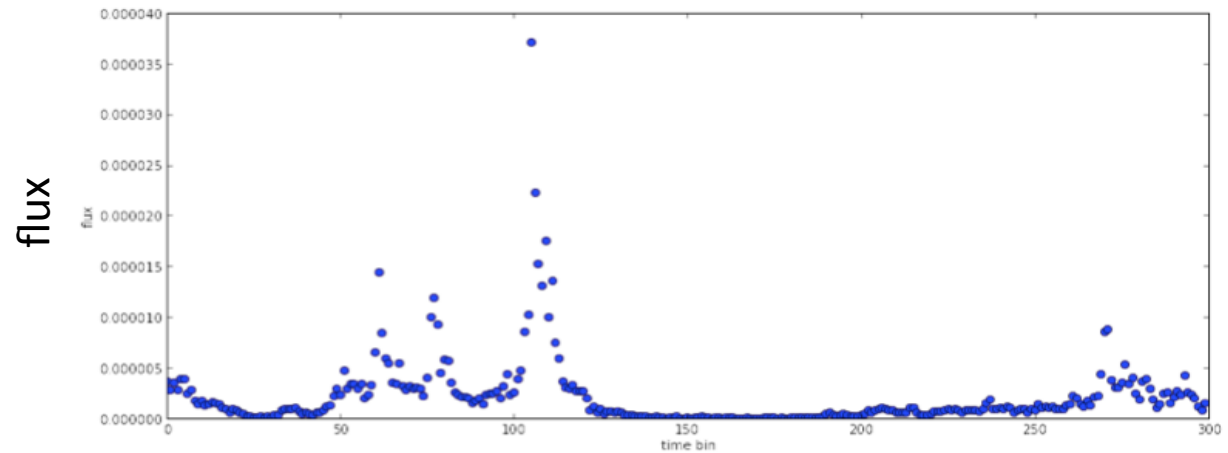
time

N. Canac, K. Abazajian (2019)

# Again, Anti-correlation even in a bigger blazar

Blazar: 3C454.3

$M \sim 10^9 M_{\text{Sun}}$



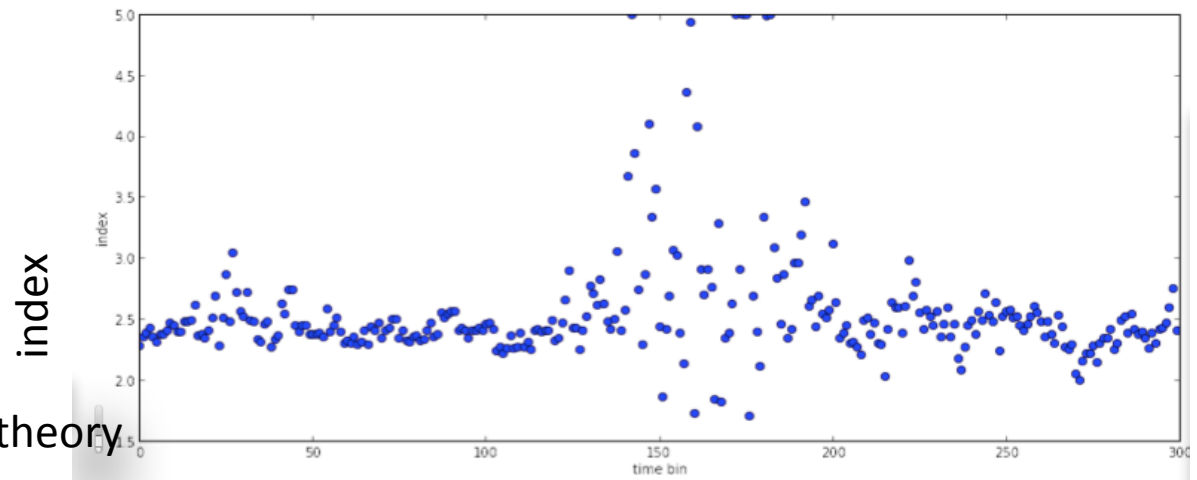
Same anti-correlation as  
AO0235+164

The rise time and burst periods  
a lot longer (by an order of  
magnitude)

Quantitative agreement and  
**correct scaling** with Blazar mass  
with (broader sense of) **Wakefield** theory

(Ebisuzaki/Tajima)

period  $\sim M$  ; luminosity  $\sim M$



time

N. Canac, K. Abazajian (2019)

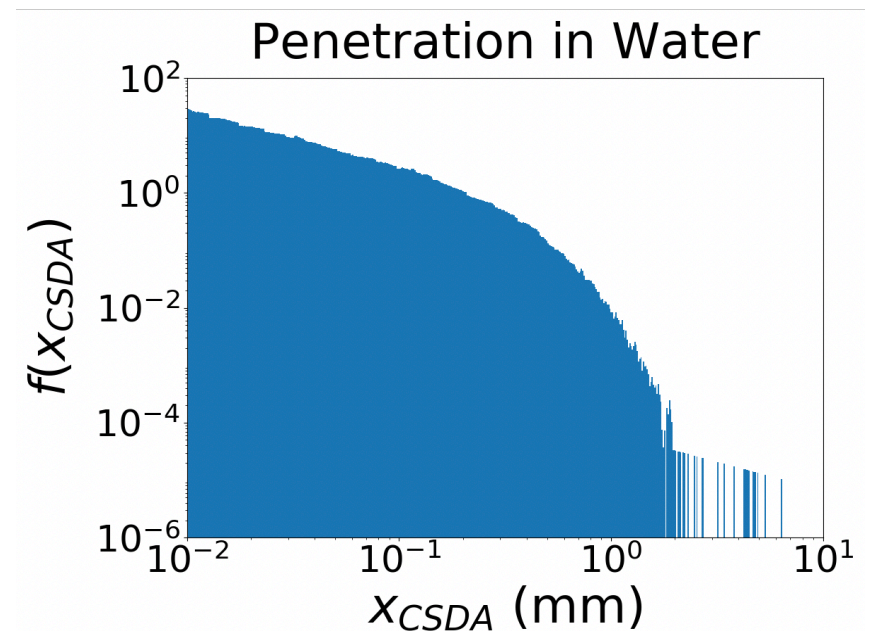
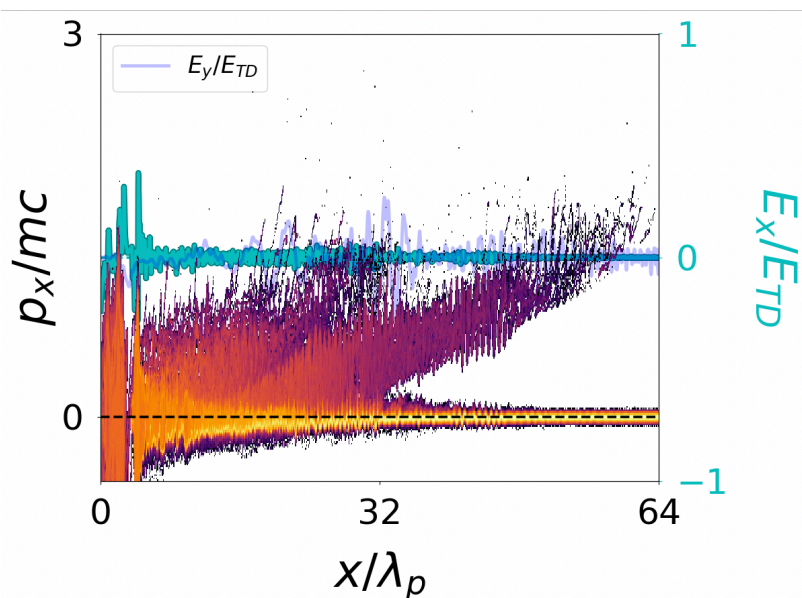
# Nanotube cancer therapy





# High density wakefields for medicine

- **Micron** accelerator (in body?) by **optical laser**
- **Nanomaterials** target: density  $\sim 10^{21} \text{ cm}^{-3}$



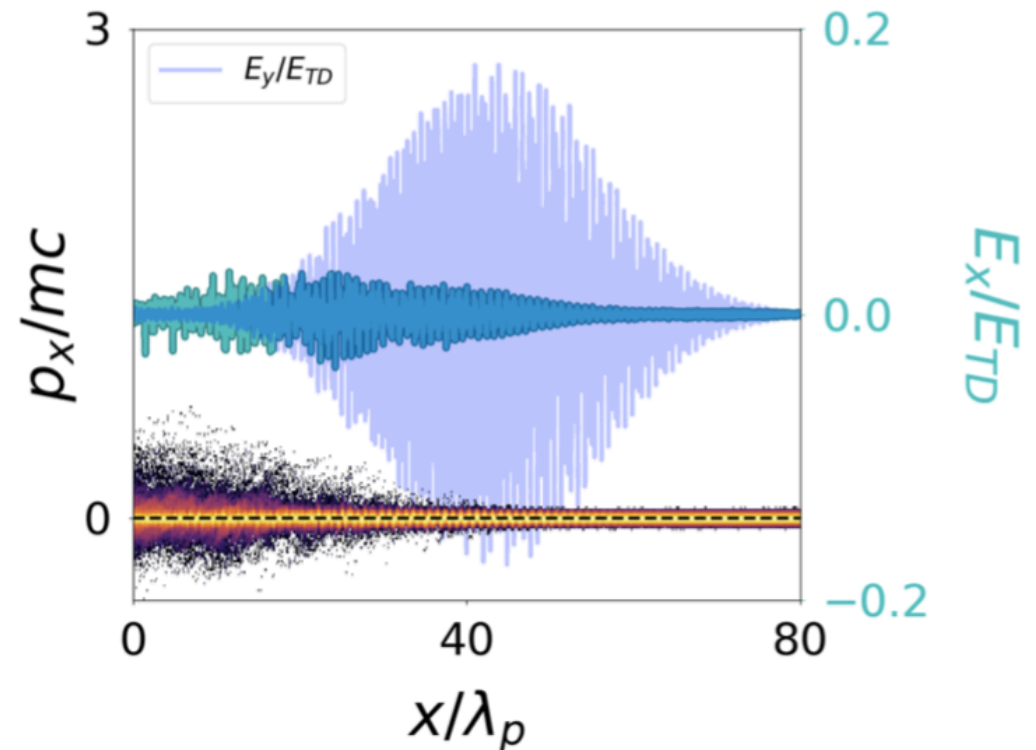
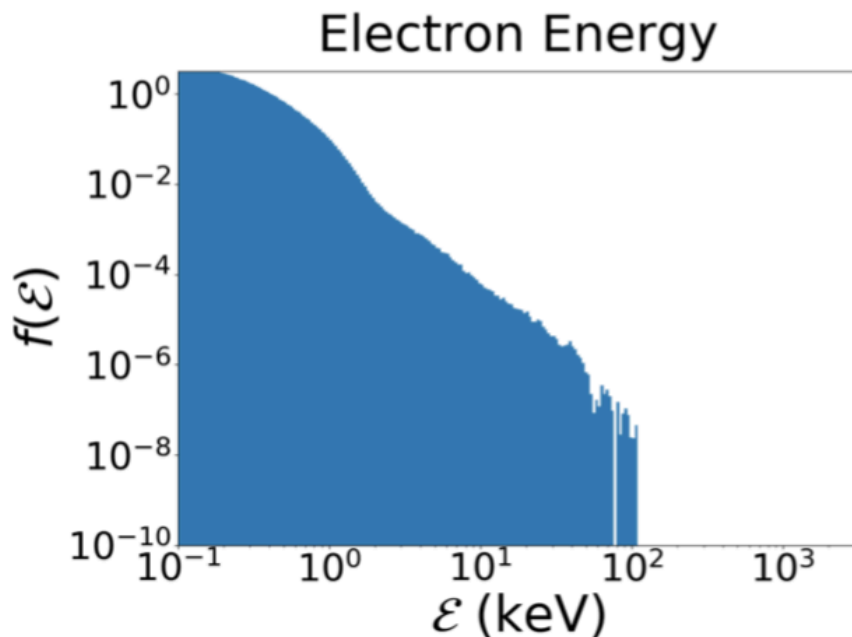
**Critical density wakefield acceleration** (< MeV) : e.g. skin cancer

Nicks et al. (2019)

# Beatwave wakefield acceleration of electron acceleration in low intensity **laser**

- Two laser pulses, each @  $a_0 = 0.03$
- $a_0 = 0.03 \rightarrow 1.2 \times 10^{15} \text{ W/cm}^2$
- Wavelength:  $\lambda_0 = 1 \mu\text{m}$
- $\omega_1 = \omega_0 + \omega_p/2, \omega_2 = \omega_0 - \omega_p/2$
- Pulse length:  $\approx 300 \text{ fs}$

← Tajima-Dawson (1979)



Very low intensity **laser** with **nanotubes** → no vacuum necessary

S. Nicks, et al. (2020)

# Conclusions

- 1994-LWFA Demonstrated: ultrafast pulses, coherent collective (robust) intense (GeV/cm) accelerators.
- TFC → Single-cycled **laser** → single-cycled **X-ray laser** (also high density e-bunch)
- **Wakefield in nanostructure (TeV/cm):**  
**TeV on a chip accessible\***
- Toward PeV (~10-100m)
- **Wakefields:** Nature's favored acceleration for UHECR, **gamma ray** bursts from Blazars
- Applications: tiny **LWFA** radiotherapy of cancer

\* Book: "Beam Acceleration in Crystals and Nanostructures" (WSP, 2020)

Recent advancements in generation of intense X-ray laser ultrashort pulses open opportunities for particle acceleration in solid-state plasmas. Wakefield acceleration in crystals or carbon nanotubes shows promise of unmatched ultra-high accelerating gradients and possibility to shape the future of high energy physics colliders. This book summarizes the discussions of the “Workshop on Beam Acceleration in Crystals and Nanostructures” (Fermilab, June 24–25, 2019), presents next steps in theory and modeling and outlines major physics and technology challenges toward proof-of-principle demonstration experiments.

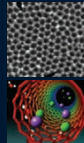
# Thank you!

“Accelerator  
Unprecedented and huge  
Curious baby  
Embraced by Mother Mountain  
Where’s her beautiful white coat?”  
(Toshiki, Geneva, Feb. 13, 2020)

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Shiltsev • Tajima



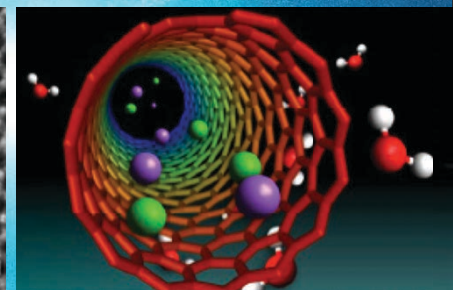
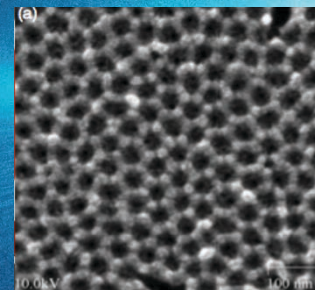
BEAM ACCELERATION IN  
CRYSTALS AND NANOSTRUCTURES



# BEAM ACCELERATION IN CRYSTALS AND NANOSTRUCTURES

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