




“TeV on a Chip”: A New Perspective of Wakefield Acceleration

Toshiki Tajima
University of California at Irvine

Collaboration: X. M. Zhang, G. Mourou, V. Shiltsev, P. Taborek, K. Nakajima, F. Zimmermann, T. Ebisuzaki, X. Yan, B. Barish, Y.M. Shin, K. Abazajian, S. Barwick, J. Wheeler, W. J. Sha, S. Nicks, S. Hakimi, D. Roa, D. Strickland, D. Farinella, F. Tamanoi, G. Szabo, A. Sahai, R. Sydora

1. New compression of **laser**
 2. Nanometric wakefield accelerator driven by **X-ray laser** = “**TeV on a Chip**”
 3. Betatron oscillations and **X-rays** in nanotube
 4. Astrophysical wakefields
 5. Nanotube wakefield **cancer therapy**
- 

Motivation:

1. Invention of **Thin Film Compression** (TFC, 2013) opened up **Laser Wakefield Acceleration** (LWFA, 1979) in **X-ray** regime,

$$E_{TD} = m\omega_{pe} c / e; \quad \Delta\varepsilon = 2mc^2 a_0^2 (n_{cr} / n)$$

compactifying further by 10^3 over the gas plasma LWFA

2. X-ray frequency exceeds the nanomaterial's plasma frequency ω_{pe}

→ **carbon-nanotubes**

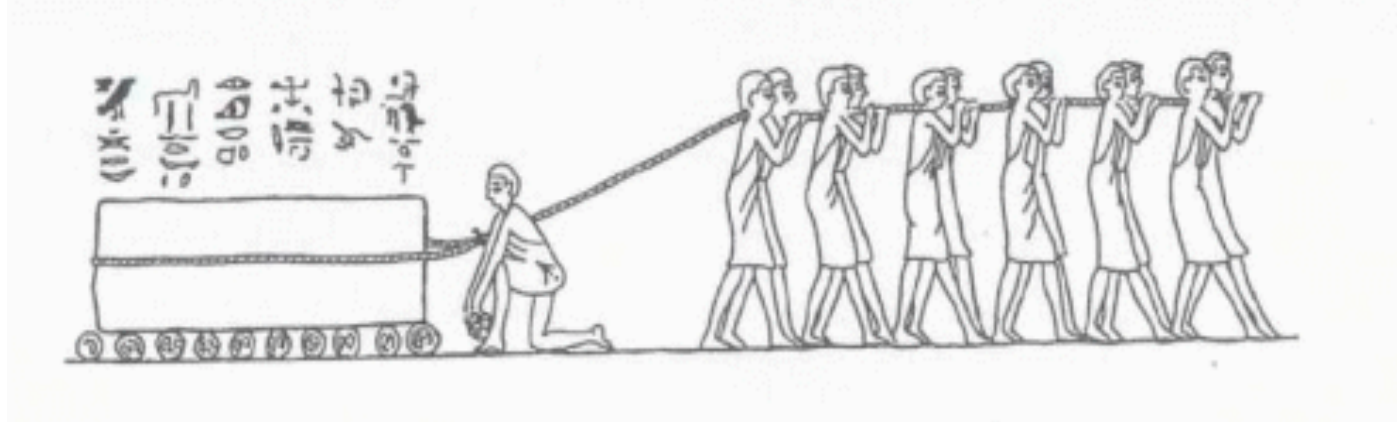
higher than 10TV/m wakefield (2014)

→ Explore **X-ray** wakefield accelerator in nanotube = “TeV on a Chip”

Plasma (nanomaterial) accelerator driven by **laser** pulse

Collective force $\sim N^2$ (nonlinear \leftarrow linear force $\sim N$)

Coherent and smooth structure (not stochastic)

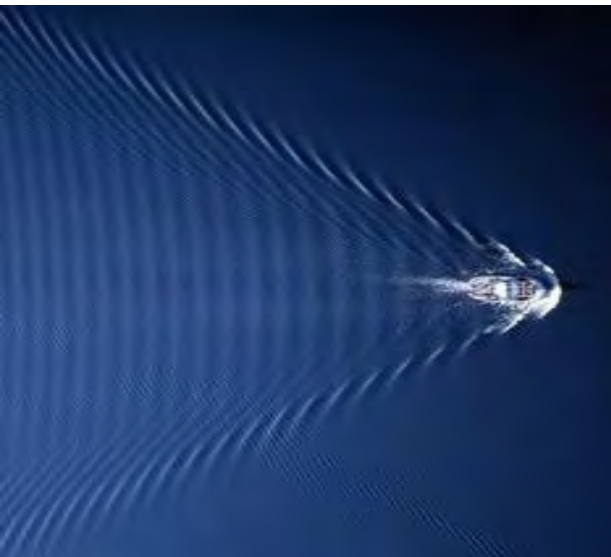


Plasma (nanomatter) accelerator driven by **laser** (coherent photons)

compactification by $10^3 - 10^4$ (now even by 10^6) \gg conventional accelerators
enabled by **laser** technology (laser compression (Mourou et al.1985))

Laser Wakefield (LWFA):

Wake phase velocity \gg water movement speed
maintains **coherent** and **smooth** structure



Tsunami phase velocity becomes ~ 0 ,
causes **wavebreak** and **turbulence**

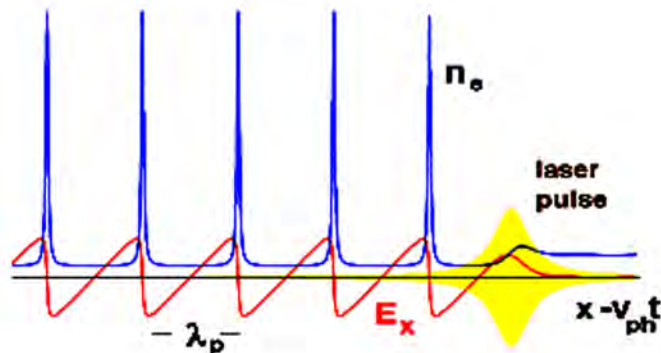


VS

Strong beam (of **laser** / particles) drives plasma waves to saturation amplitude: $E = m\omega v_{ph} / e$

No wave breaks and wake **peaks** at $v \approx c$

Wave **breaks** at $v < c$



← relativity
regularizes
(*relativistic coherence*)



Relativistic coherence enhances beyond the Tajima-Dawson field $E = m\omega_p c / e$ (\sim GeV/cm)

The late Prof. Abdus Salam



At ICTP Summer School (1981), Prof. Salam summoned me and discussed about **laser wakefield** acceleration.

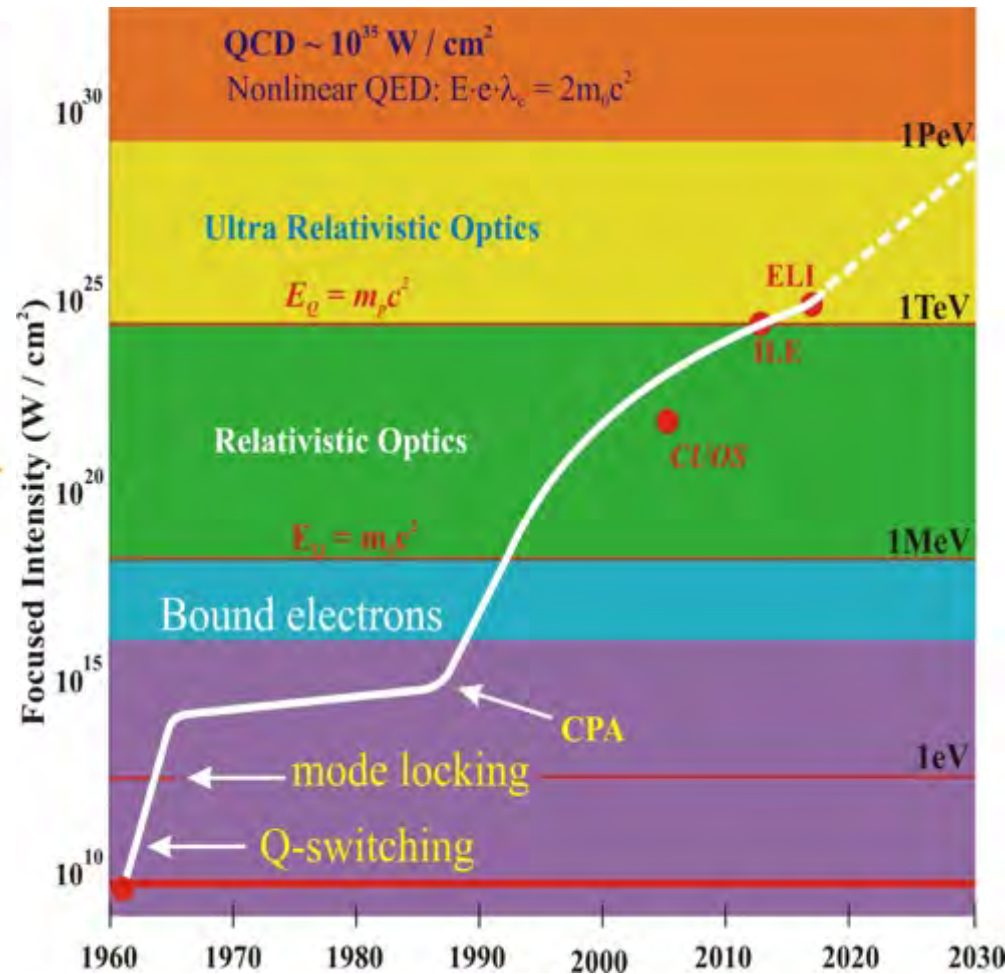
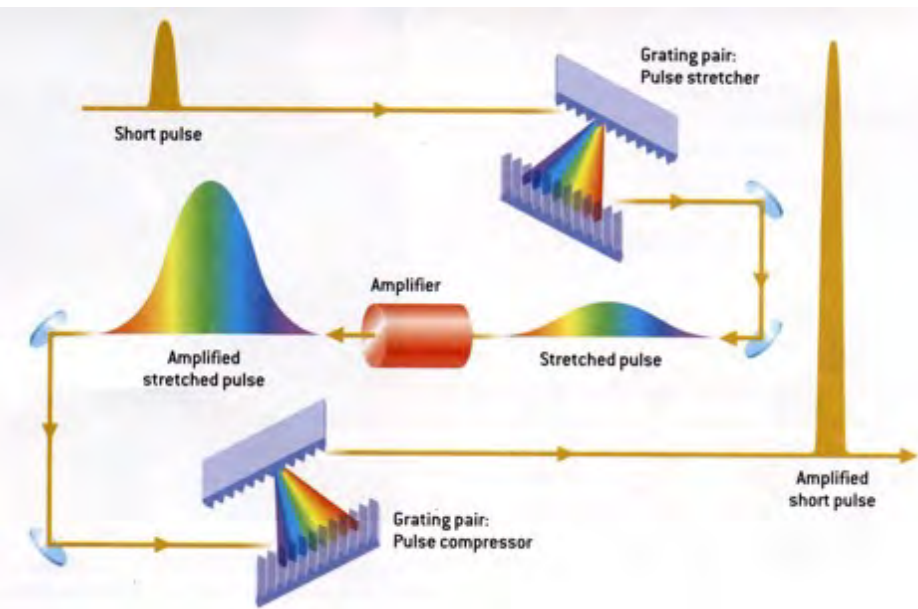
Salam: *'Scientists like me began feeling that we had less means to test our theory. However, with your laser acceleration, I am encouraged'*. (1981)

He organized the Oxford Workshop on **laser wakefield** accelerator in 1982.

Effort: many scientists over many years to realize his vision / dream
High field science: spawned

(NB: Prof. C. Rubbia et al.
discovered his bosons at CERN, 1983)

Enabling technology: **laser** revolution



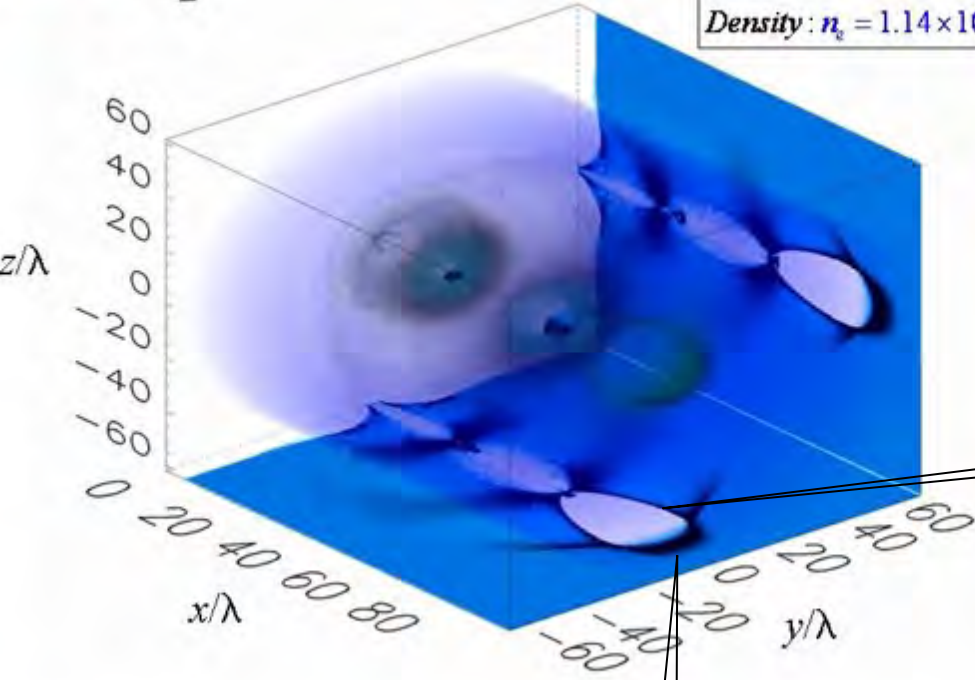
G. Mourou invented **Chirped Pulse Amplification** (1985)

Laser intensity exponentiated since,

to match the required intensity for Tajima-Dawson's **LWFA** (1979)

Laser-driven Bow and Wake

Density: $n_e = 1.14 \times 10^{18} \text{ cm}^{-3}$



Wakefield acceleration

Wake Wave



Bow Wave

Ponderomotive acceleration

(Bulanov, Esirkepov)

Theory of **wakefield** toward extreme energy

$$\Delta E \approx 2m_0c^2 a_0^2 \gamma_{ph}^2 = 2m_0c^2 a_0^2 \left(\frac{n_{cr}}{n_e} \right), \quad (\text{when 1D theory applies})$$

In order to avoid wavebreak,

$$a_0 < \gamma_{ph}^{1/2},$$

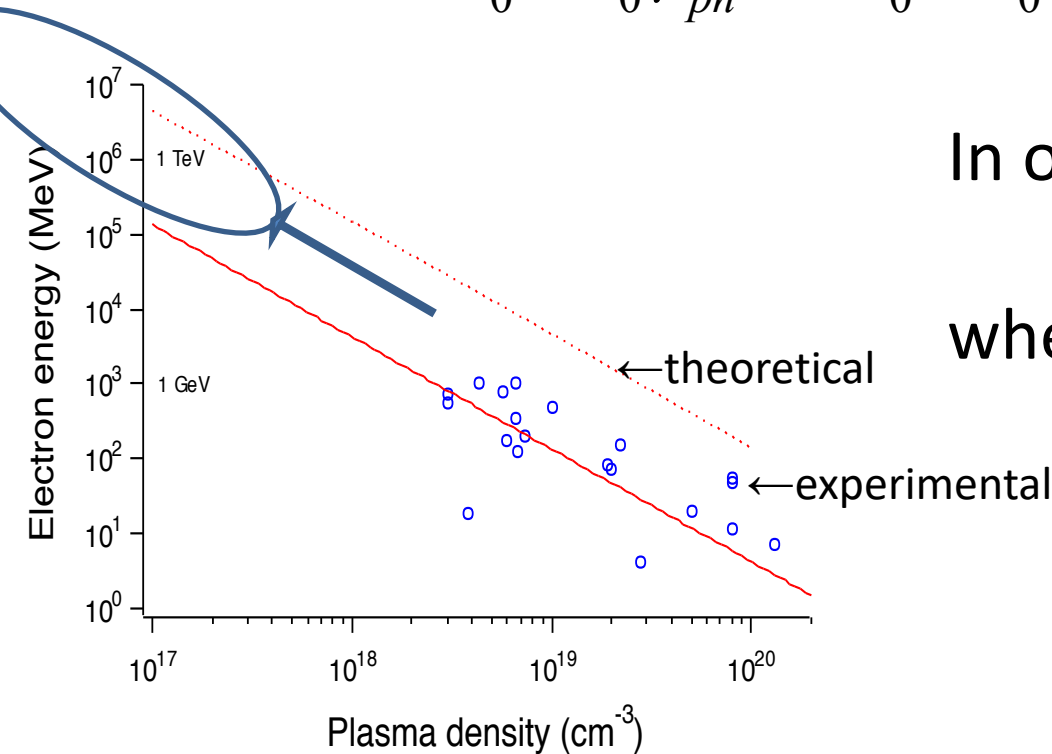
where

$$\gamma_{ph} = [n_{cr}(\omega) / n_e]^{1/2}$$

$$n_{cr} = 10^{21} / \text{cc} \text{ (1eV photon)}$$

$$\rightarrow 10^{29} \text{ (10keV photon)}$$

$$n_e = 10^{16} \text{ (gas)} \rightarrow 10^{23} / \text{cc} \text{ (solid)}$$



$$L_d = \frac{2}{\pi} \lambda_p a_0^2 \left(\frac{n_{cr}}{n_e} \right), \quad L_p = \frac{1}{3\pi} \lambda_p a_0 \left(\frac{n_{cr}}{n_e} \right),$$

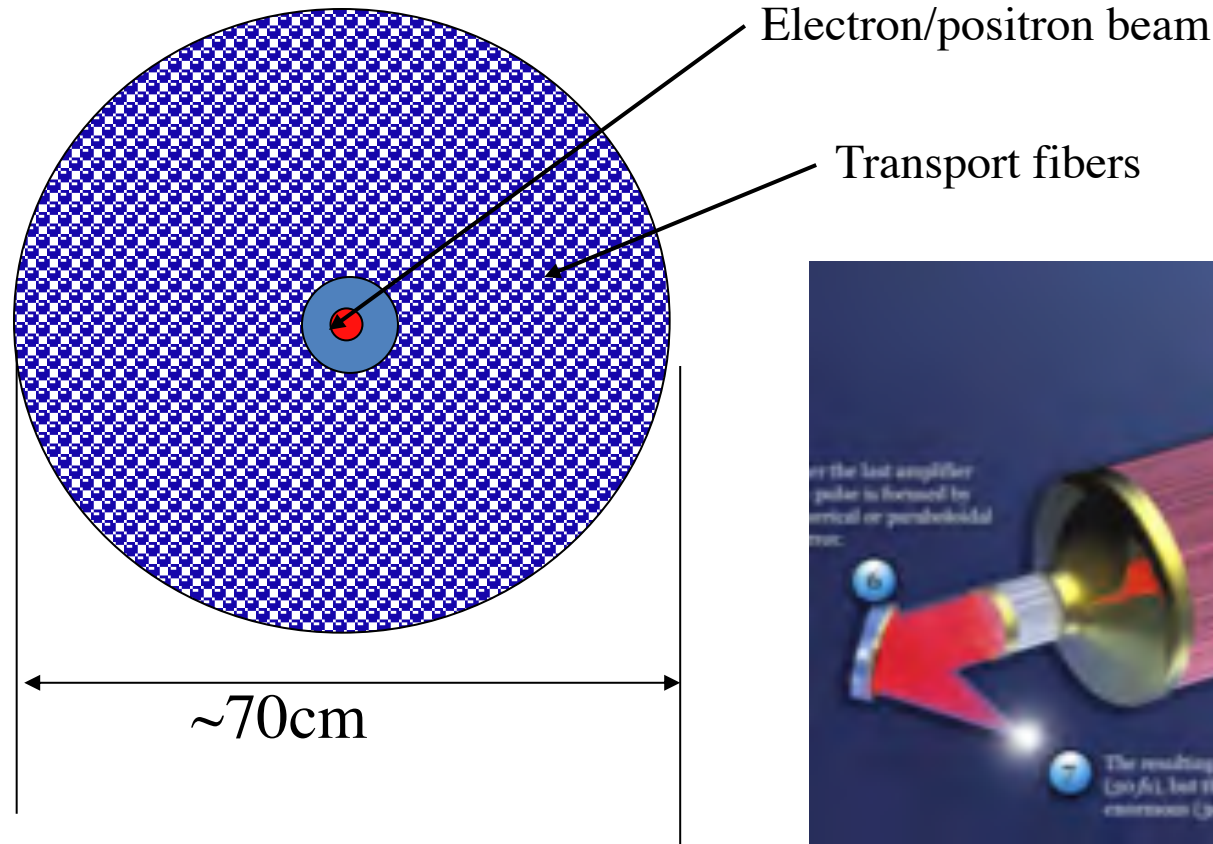
dephasing length

pump depletion length

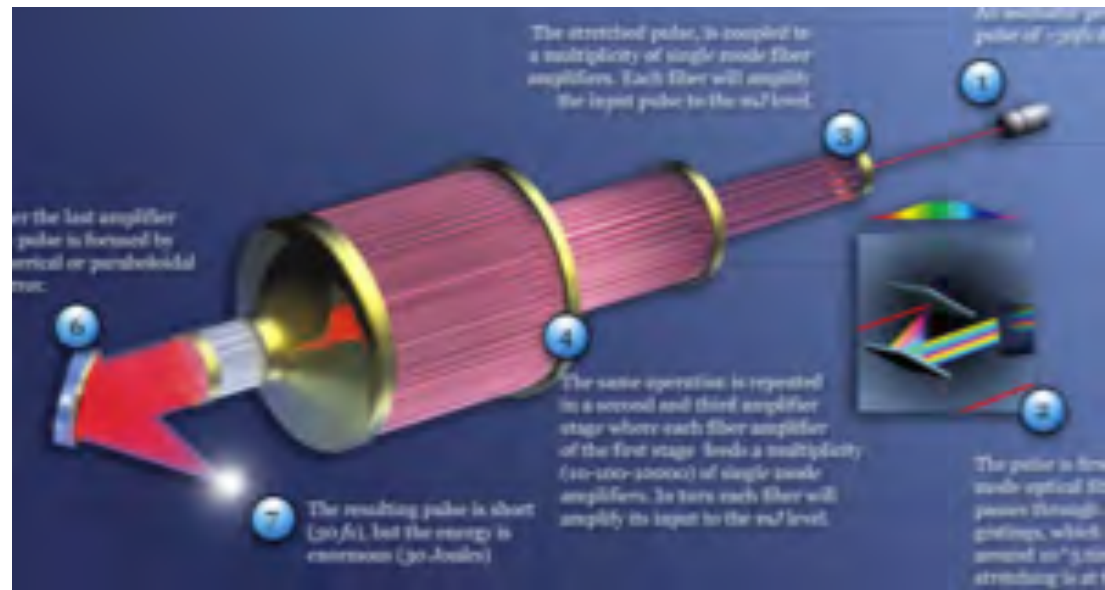
CAN Laser:

Need to Phase

32 J/1mJ/fiber ~ 3×10^4 Phased Fibers!



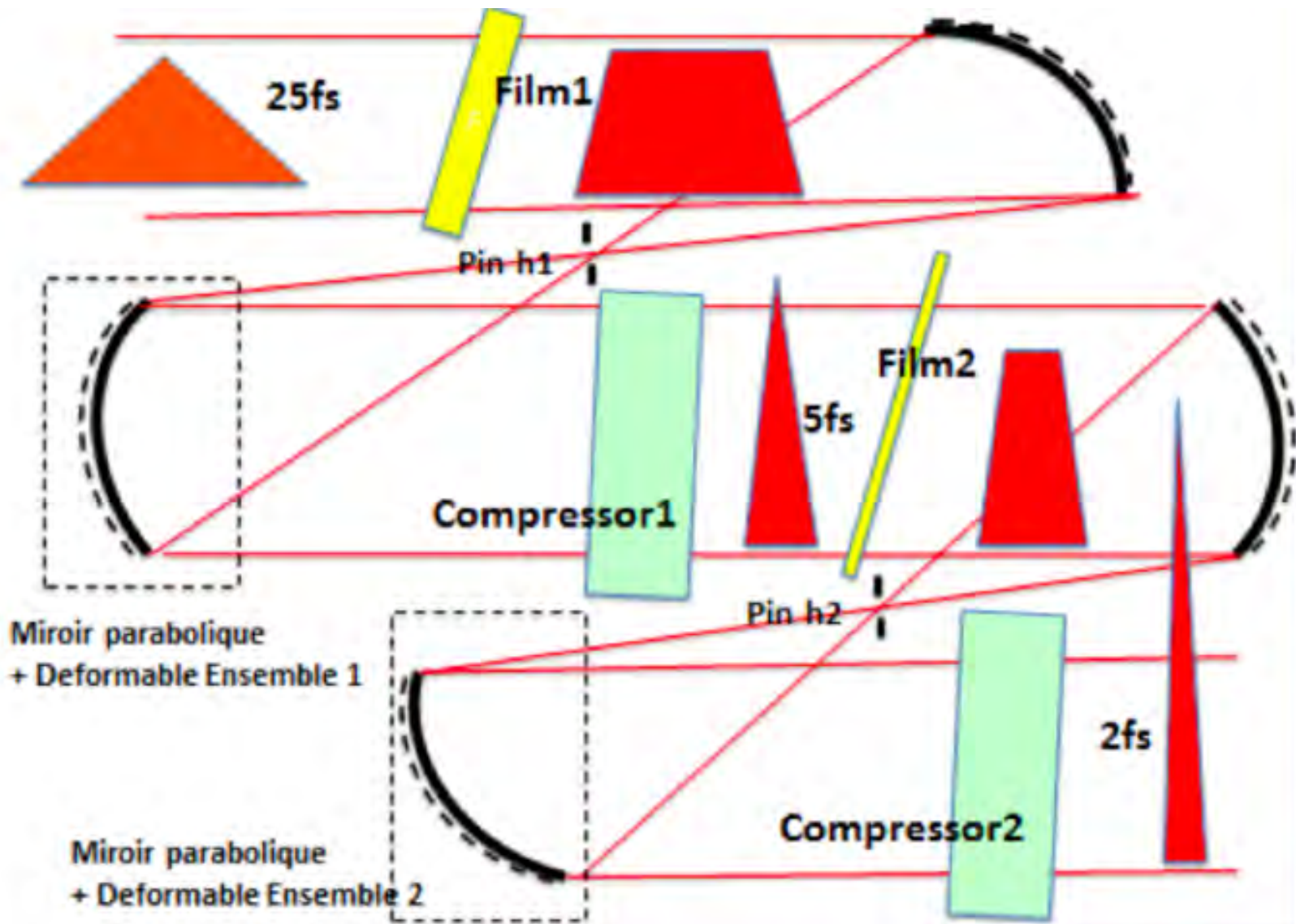
Mourou, Brookesby, Tajima, Limpert (2013)



Length of a fiber ~2m

Total fiber length ~ 5×10^4 km

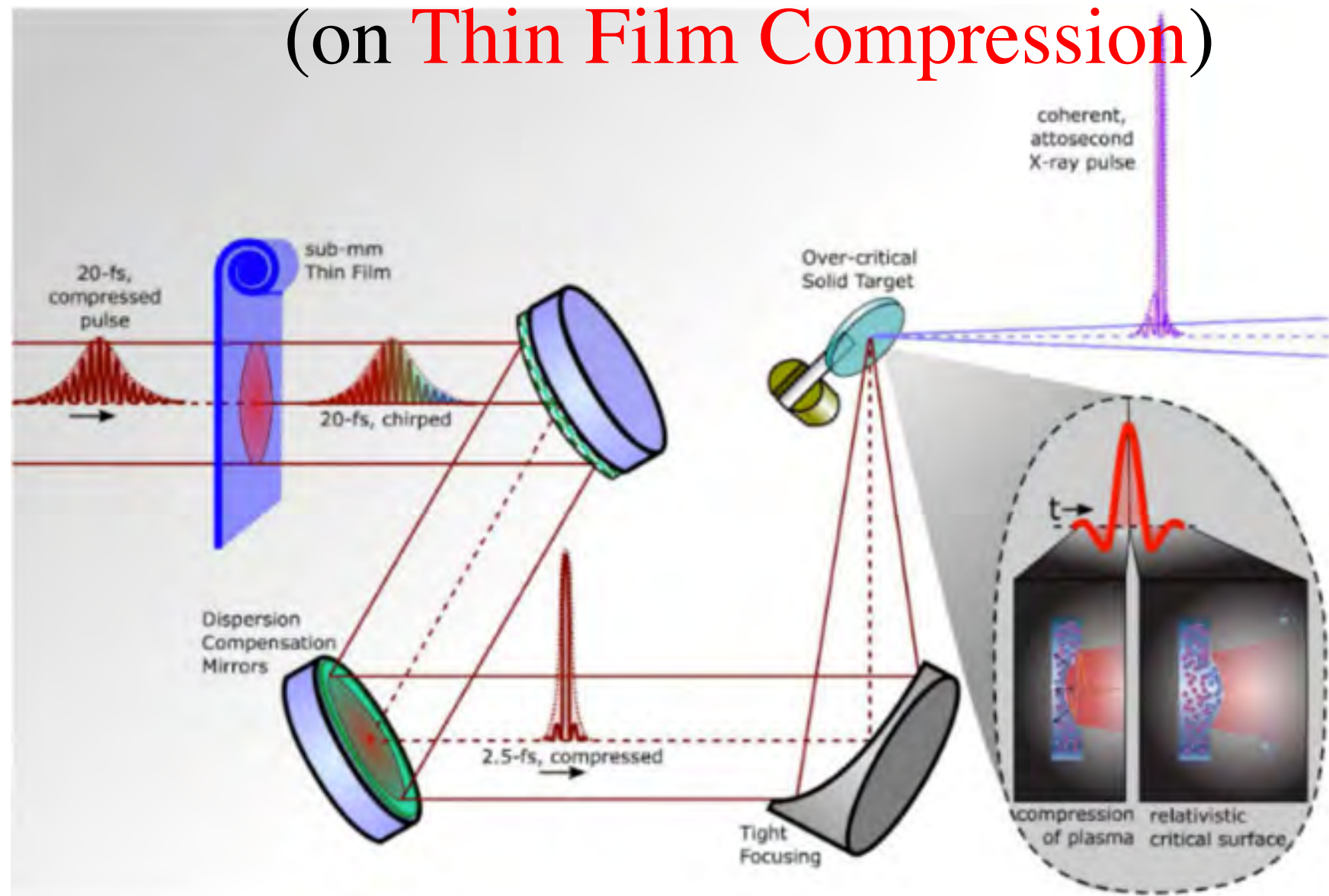
Thin Film Compression



Single-cycled **laser** and “TeV on a chip”



Next Generation X-ray Lasers (on Thin Film Compression)



Earlier works of X-ray crystal acceleration

- X-ray optics and fields (Tajima et al. ,1987)
- Nanocrystal hole for particle propagation (Newberger, Tajima, et al. 1989)
- particle transport in the crystal (Tajima et al. 1990)

APPLICATION OF NOVEL MATERIAL IN CRYSTAL ACCELERATOR CONCEPTS

B. Newberger, T. Tajima, The University of Texas at Austin, Austin, Texas 78712
 F. R. Huson, W. Mackay, Texas Accelerator Center, The Woodlands, Texas
 B. C. Covington, J. R. Payne, Z. G. Zou, Sam Houston State University, Huntsville, Texas
 N. K. Mahale, S. Ohnuma, University of Houston, Houston, Texas 77004

which incorporate regular macroscopic features on the underlying crystal lattice are of potential application to crystal accelerators and coherent sources. We have recently begun an investigation of material, porous Si, in which pores of radii up to a lattice spacings are etched through finite volumes of crystal. The potential reduction of losses to particle transport in crystal accelerators for relativistic, positively charged particles in this context will be presented. The consequences of particle transport will be discussed.

and $k = v_0/mrc^2$, v_0 , is the "spring constant of the channel well. Its specific form depends on the material. To construct the continuum potential of a string of atoms for purposes it suffices to take a typical value of 2×10^4 eV is the multiple scattering velocity space "diffusion" We have used¹⁰

$$D = z\pi r_e^2 N Z_{val} \left(\frac{m_e}{m_I}\right)^2 L_R,$$

where r_E is the classical electron radius, Z_{val} is the number of valence electrons, and N is the number density of atoms per unit volume. Logarithmic dependencies on particle energy are neglected throughout: L_R is a constant with a typical

Particle Accelerators, 1990, Vol. 32, pp. 235-240
 Reprints available directly from the publisher
 Photocopying permitted by license only

© 1990 Gordon and Breach, Science Publishers, Inc.
 Printed in the United States of America

BEAM TRANSPORT IN THE CRYSTAL X-RAY ACCELERATOR

T. TAJIMA, B. S. NEWBERGER
 University of Texas-Austin, Austin TX 78712 U.S.A.
 F. R. HUSON, W. W. MACKAY
 Texas Accelerator Center, The Woodlands, TX 77381 U.S.A.
 B. C. COVINGTON, J. PAYNE
 Sam Houston State University, Huntsville, TX 77341 U.S.A.
 N. K. MAHALE, S. OHNUMA
 University of Houston, Houston, TX 77204 U.S.A.

Abstract A Fokker-Planck model of charged particle transport in crystal channels which includes the effect of strong accelerating gradients has been developed¹ for application to

VOLUME 59, NUMBER 13

PHYSICAL REVIEW LETTERS

28 SEPTEMBER 1987

Crystal X-Ray Accelerator

T. Tajima

Department of Physics and Institute for Fusion Studies, The University of Texas, Austin, Texas 78712

and

M. Cavenago

Department of Physics, University of California, Irvine, California 92717

(Received 18 November 1986)

An ultimate linac structure is realized by an appropriate crystal lattice (superlattice) that serves as a "soft" irised waveguide for x rays. High-energy (≈ 40 keV) x rays are injected into the crystal at the Bragg angle to cause Bornmann anomalous transmission, yielding slow-wave accelerating fields. Particles (e.g., muons) are channeled along the crystal axis.

PACS numbers: 52.75.Dr, 41.80.-y, 61.80.Mk

An approach to the attainment of ever higher energies by extrapolating the linac to higher accelerating fields, higher frequencies, and finer structures is prompted by several considerations, including the luminosity requirement which demands the radius of the colliding-beam spot be proportionately small at high energies: $a_0 \approx \pi^{-1/2} h c (f/N)^{-1/2} P e^{-2}$, where f , N , P , and e are the duty cycle, total number of events, beam power, and beam energy, respectively. This approach, however, encounters a physical barrier when the photon energy becomes of the order $h\omega \approx h\omega_p \approx mc^2 a^2 \approx 30$ eV (a = the fine-structure constant), corresponding to wavelength (scale length) $\lambda \approx 500$ Å. The metallic wall begins to absorb the photon strongly, where ω_p is the plasma frequency corresponding to the crystal electron density. In addition, since the wall becomes not perfectly conducting for $h\omega \approx mc^2 a^2$, the longitudinal component of fields becomes small and the photon goes almost straight into the wall (a soft-wall regime). As the photon energy $h\omega$ much exceeds $mc^2 a^2$ and becomes $\approx mc^2 a$, however, the metal now ceases to be opaque. The mean free path of the photon is given by Bethe-Bloch theory as $l = (3/2^3 \pi) \times a_B^2 a^{-1} n^{-1} (h\omega/Z_{eff}^2 R)^{3/2}$, where a_B is the Bohr radius, n the electron density, Z_{eff} the effective charge of the lattice ion, and R the Rydberg energy.

In the present concept the photon energy is taken at the hard x-ray range of $h\omega \approx mc^2 a$ and the linac structure is replaced by a crystal structure, e.g., silicon or GaAs-AlAs. (A similar bold endeavor was apparently undertaken by Hofstadter already in 1968.¹) Here the crystal axis provides the channel through which accelerated particles propagate with minimum scattering (channeling²) and the x rays are transmitted via the Bornmann effect (anomalous transmission^{3,4}) when the x rays (wavelength λ) are injected into the xz plane with a

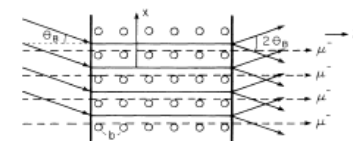
where b is the transverse lattice constant and later a the longitudinal lattice constant ($a \approx b$) (see Fig. 1). The row of lattice ions (perhaps with inner-shell electrons) constitutes the "waveguide" wall for x rays, while they also act as periodic irises to generate slow waves. A superlattice⁵ such as Ge₂Si_{1-x}S₂ (in which the relative concentration c ranges from 0 to 1 over 100 Å or longer in the longitudinal z direction) brings in an additional freedom in the crystal structure and provides a small Brillouin wave number $k_z = 2\pi/s$ with s being the periodicity length. We demand that the x-ray light in the crystal channel walls becomes a slow wave and satisfies the high-energy acceleration condition

$$\omega/(k_z + k_x) = c, \quad (2)$$

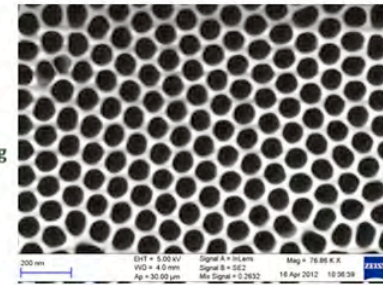
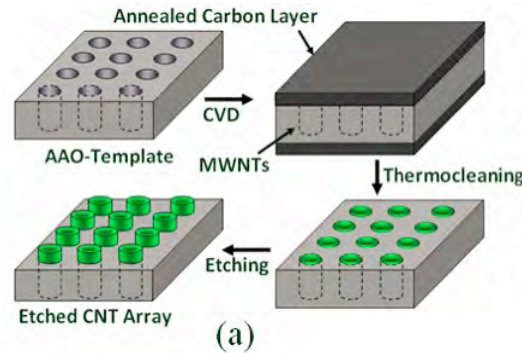
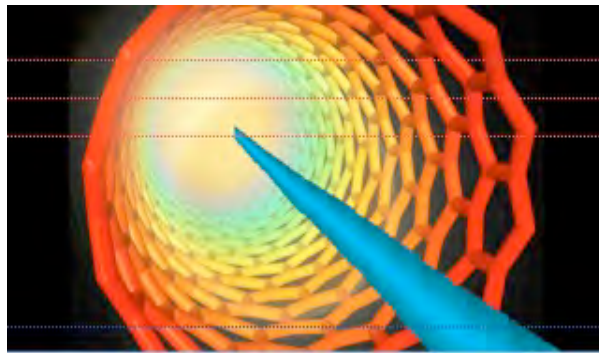
where ω and k_z are the light frequency and longitudinal wave number.

The energy loss of moving particles in matter is due to ionization, bremsstrahlung, and nuclear collisions. We can show⁶ that a channeled high-energy particle moving fast in the z direction oscillates in the xy plane according to the Hamiltonian

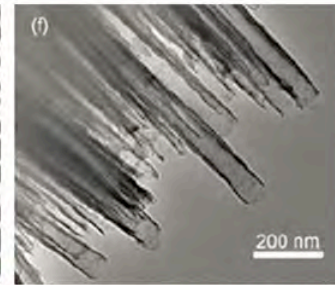
$$H = \frac{1}{2m} (p_x^2 + p_y^2) + V(x, y), \quad (3)$$



Why Nanotubes



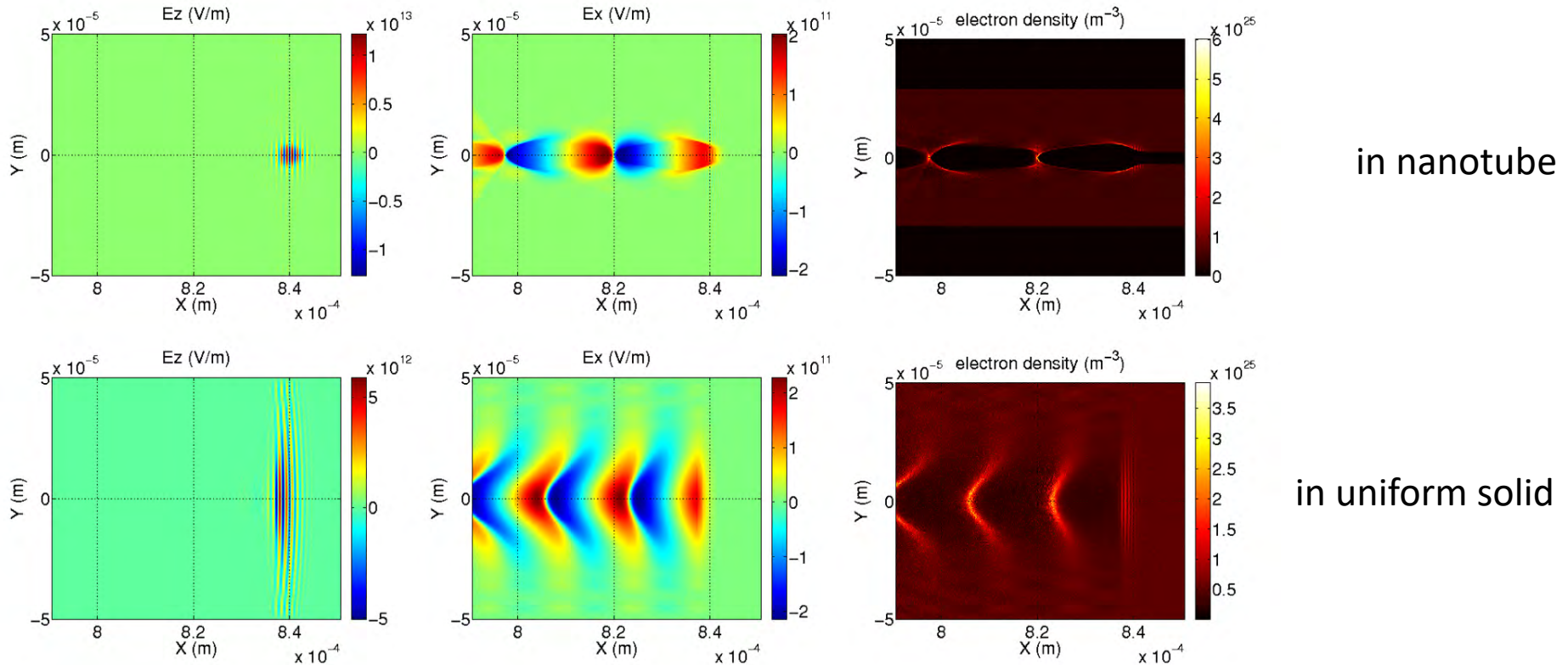
(b)



(c)

- High density ↔ Higher acceleration gradient ($\sim \text{TeV} / \text{cm}$)
- Provides external structure to guide laser and electron beam
- No slowdown of electrons by collisions
- Intact for time of ionization (fs)
- More coherent electrons and betatron radiation

X-ray LWFA in a tube vs. uniform solid



A few-cycled 1keV X-ray pulse ($a_0 \sim O(1)$), causing 10TeV/m wakefield in the tube
more strongly confined in the tube
cf: uniform solid

Comparison of flat plasma vs. nanotube



Flat snow slalom



Half-pipe snow slalom

Tajima and Dawson, PRL, 1979: wakefields
Tajima, M. Cavenago, PRL, 1987: crystal acceleration
S. Iijima, Nature 1991: CNT
Tajima workshop invited Iijima, 1992

Mourou, 2014: Thin Film Compression
Tajima, 2014: nanotube acceleration with X-ray
Zhang, 2016: self-focusing in nanotube
Shiltsev, Tajima, 2019: Fermilab workshop

X-ray in nanotube \leftrightarrow

optical laser in mm plasma guide

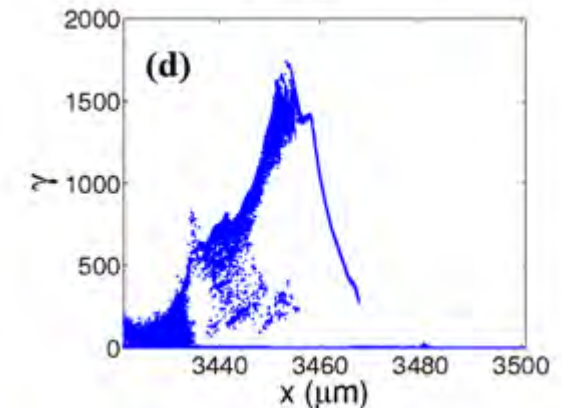
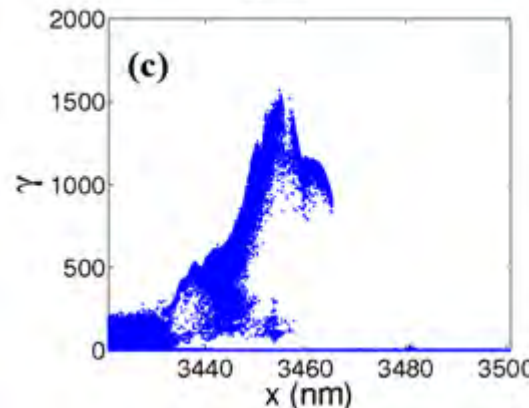
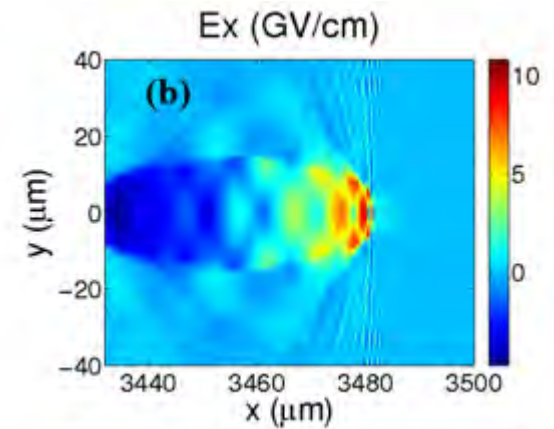
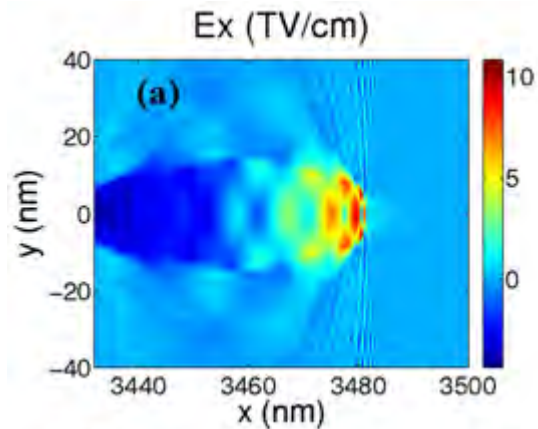
Acceleration process are self-similar:

Xray in micron (short), while optical laser in mm (longer)

But beam emittance and betatron radiation: quite different (not self-similar)

X-ray laser

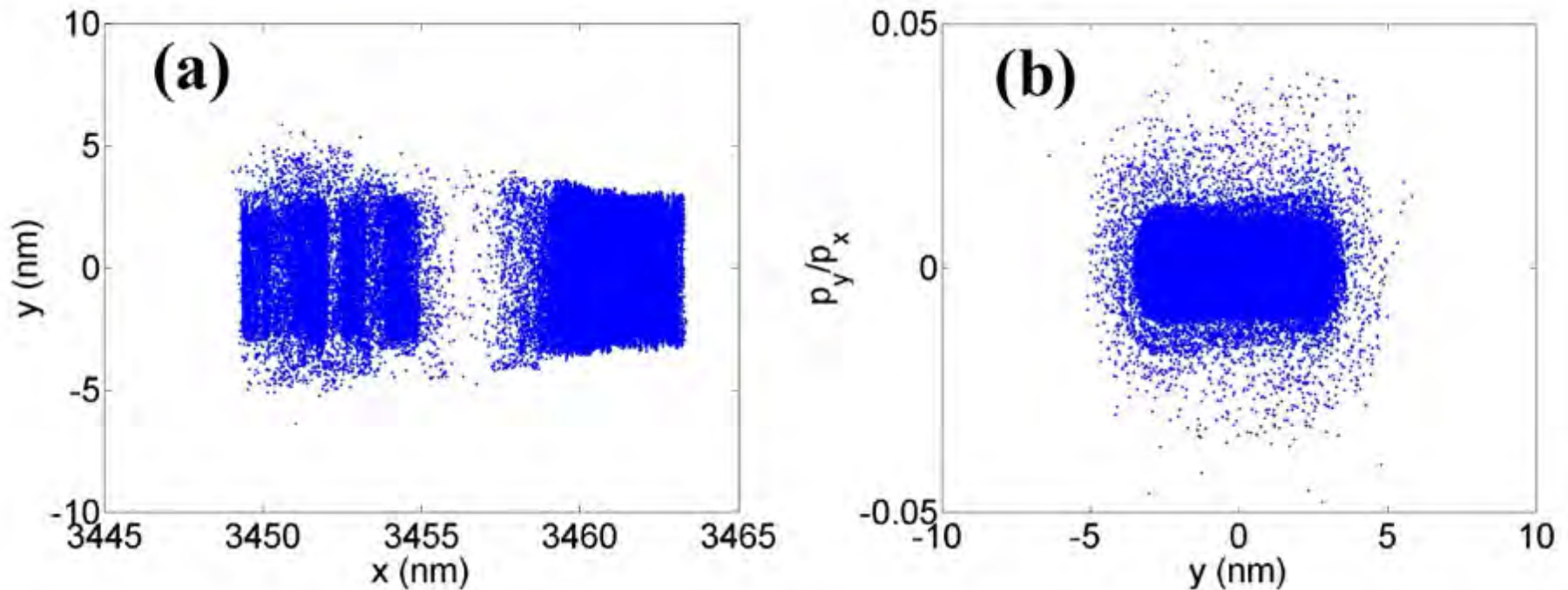
Optical laser



Distributions of (a)(b) **wakefield** and (c)(d) electron energy induced by (a)(c) the **X-ray laser** pulse and (b)(d) **optical laser** in a tube when $a_0=10$

Beam emittance reduction

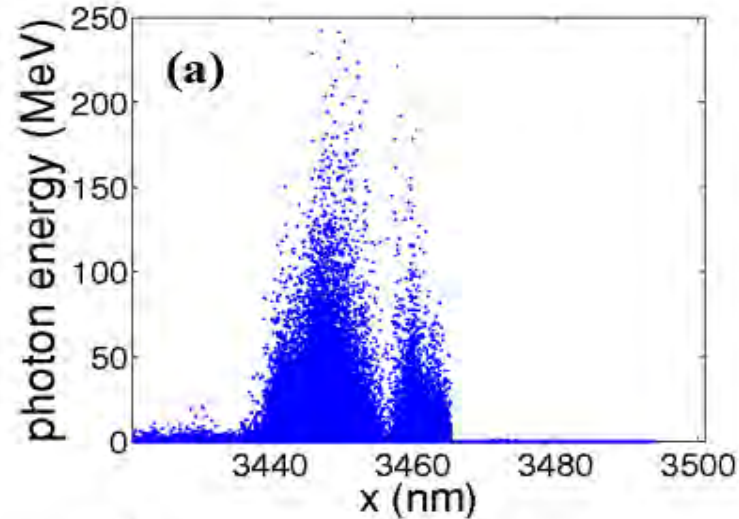
X-ray laser driven wakefield
emittance reduction (much smaller transverse dimension)



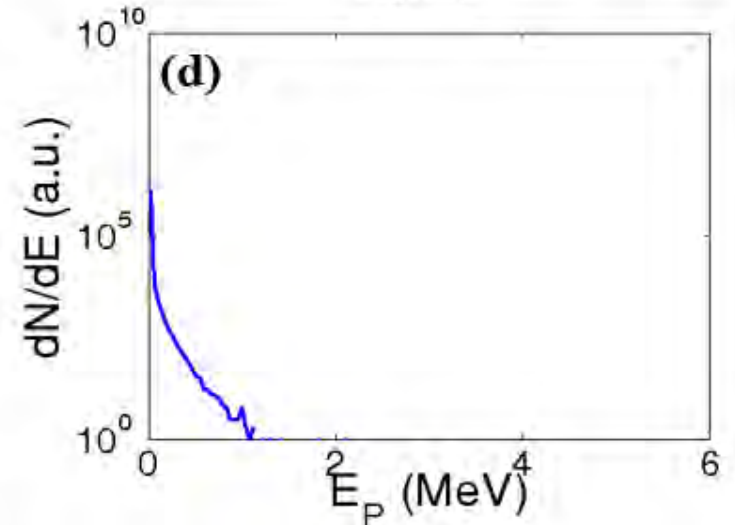
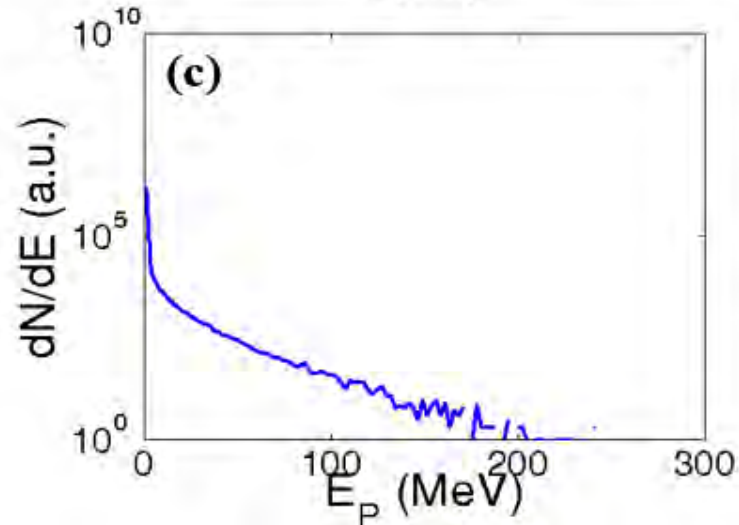
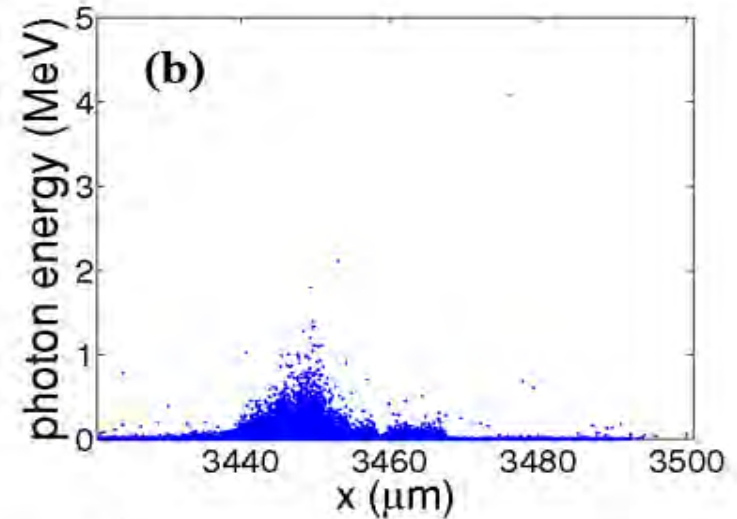
(a) The space distribution (x, y) and (b) the transverse phase space ($y, p_y/p_x$)

Betatron radiation

X-ray laser



Optical laser



(a)(b) Photon energy distributions and (c)(d) photon energy spectrum in the (a)(c)X-ray driven case and (b)(d) 1eV optical laser driven case in a tube.

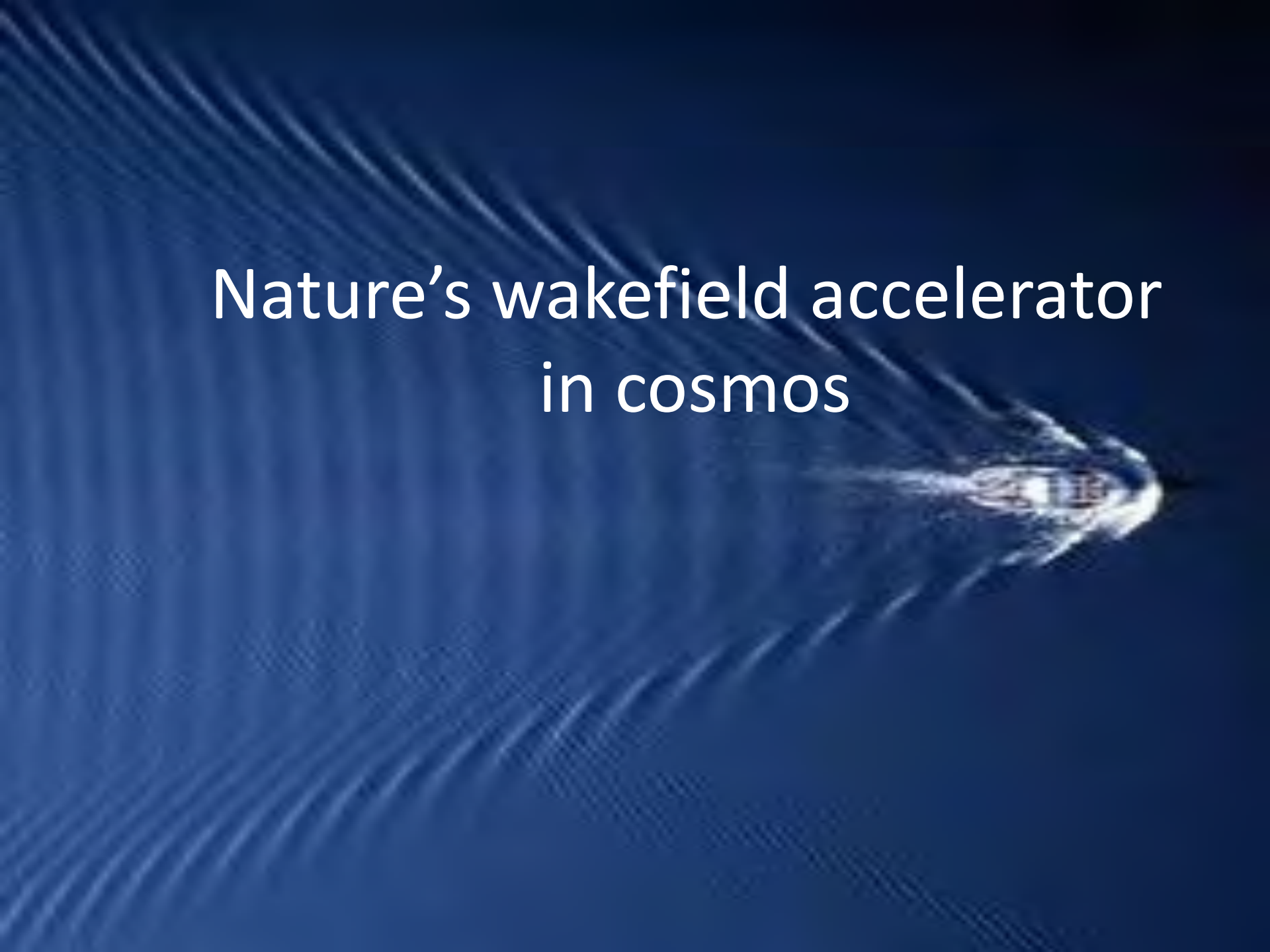
$$\alpha = \frac{\hbar^2}{e c}$$

Fermi's PeV Accelerator

Now

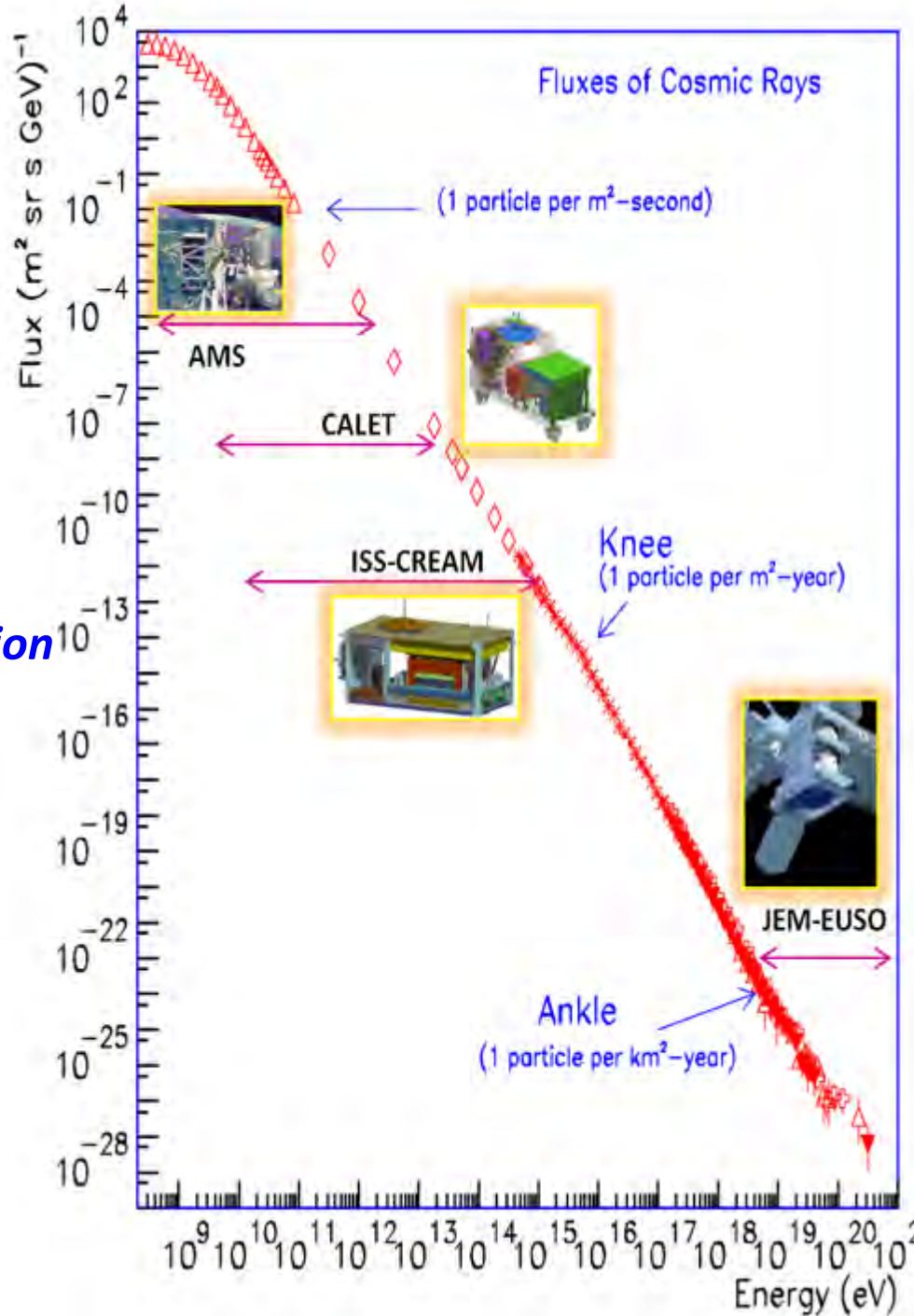
TeV on a chip \rightarrow PeV over 10m \rightarrow check superstring theory?

Nature's wakefield accelerator in cosmos

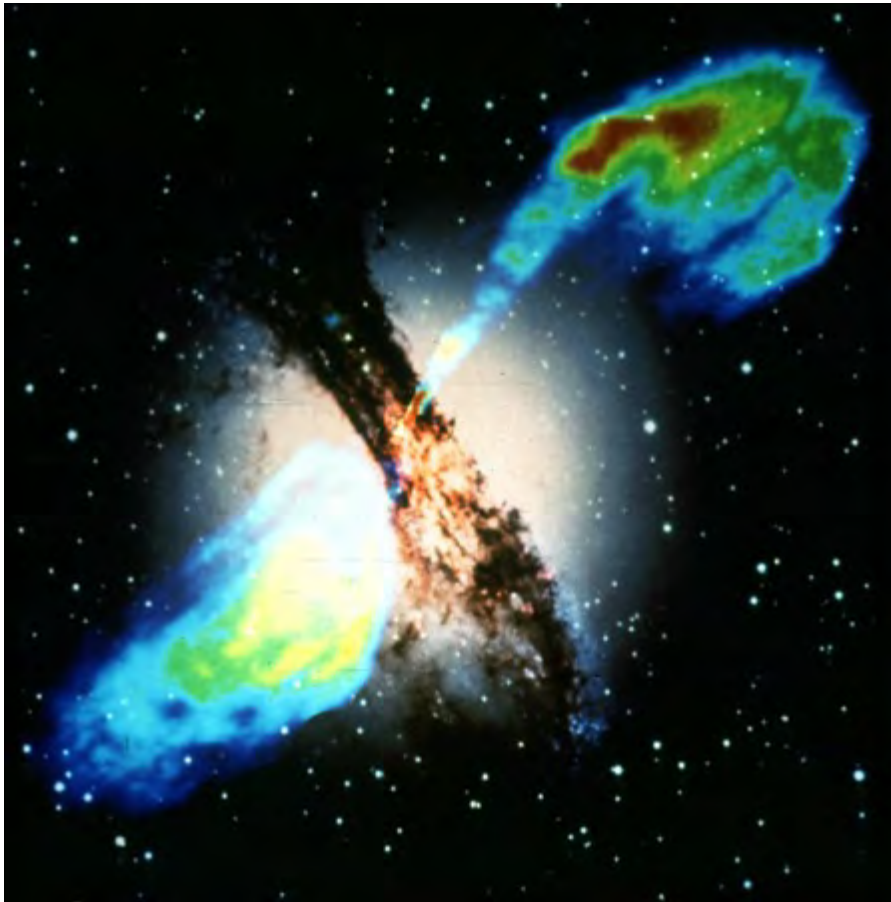


Ultrahigh Energy Cosmic Rays (UHECR)

Fermi mechanism runs out of steam
beyond 10^{19} eV
due to *synchrotron radiation*
Wakefield acceleration
comes in rescue
prompt, intense, *linear acceleration*
small synchrotron radiation
radiation damping effects?



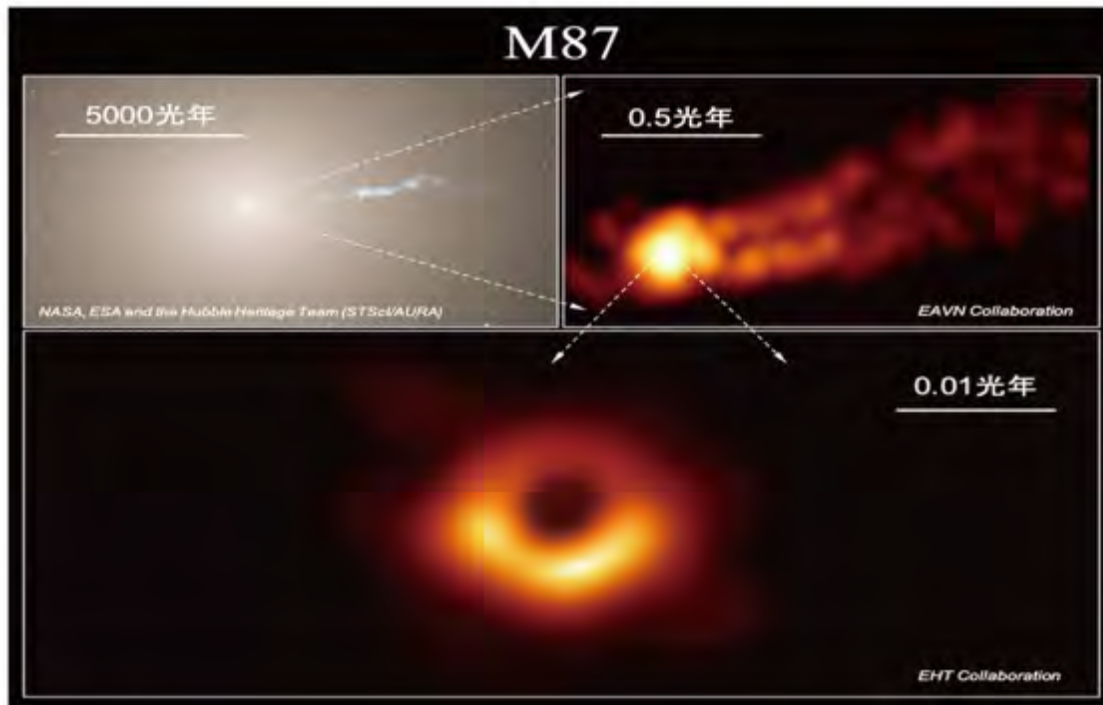
Cen A



- Distance : 3.4Mpc
- Radio Galaxy
 - Nearest
 - Brightest radio source
- Elliptical Galaxy
- Black hole at the center w/
relativistic jets

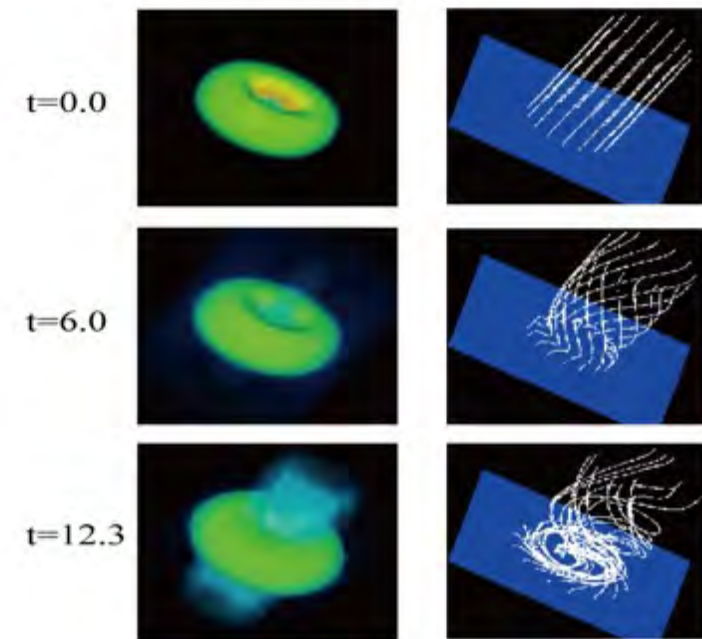
Discovery of Blackhole and Prediction

M87 blackhole: by [Event Horizon Telescope \(2019\)](#)

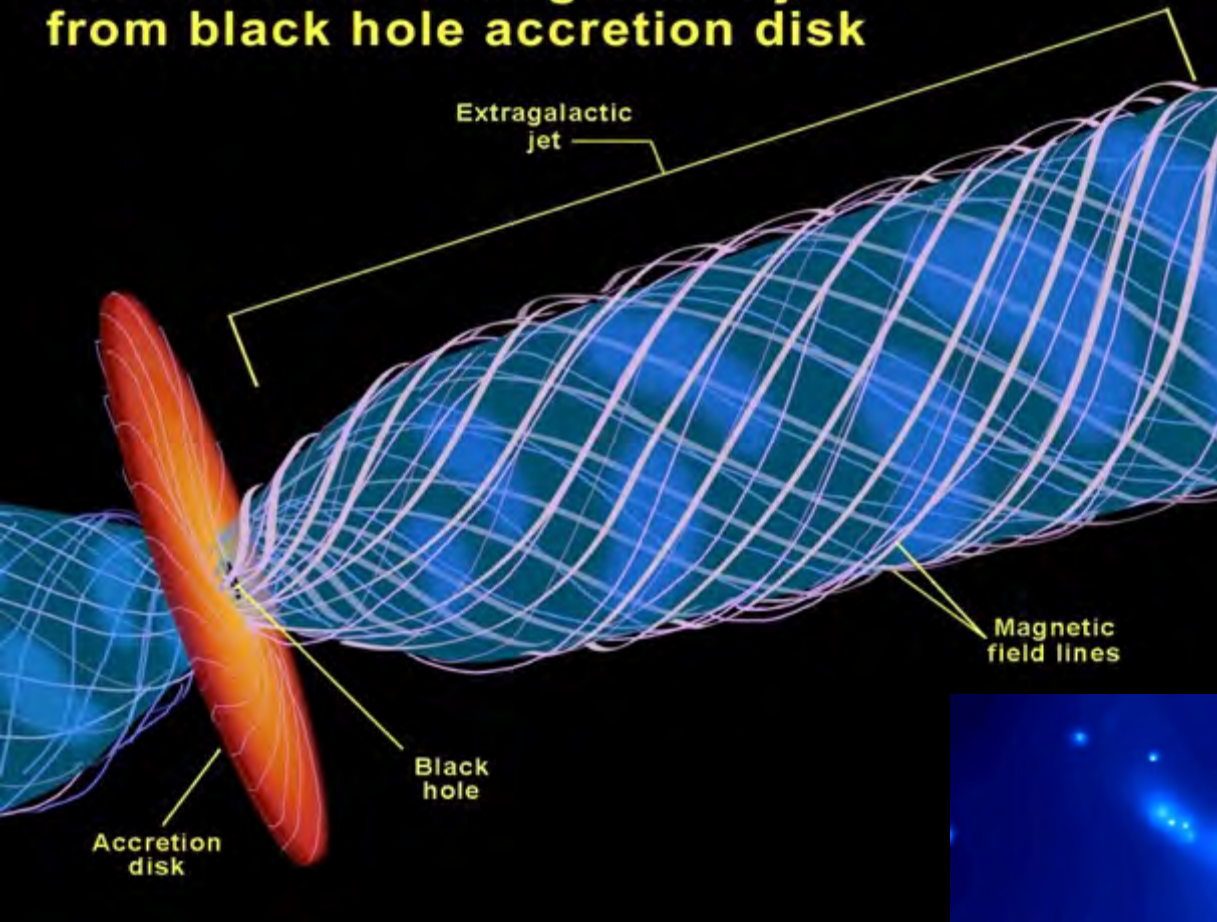


Prediction: [Tajima and Shibata](#)
"Plasma Astrophysics" (1997)

3D Structure of Disk and Jet



Formation of extragalactic jets from black hole accretion disk



Fermi's 'Stochastic Acceleration'
(large synchrotron radiation loss)



Coherent **wakefield** acceleration
(no limitation of the energy)



Nature's **LWFA** : Blazar jets

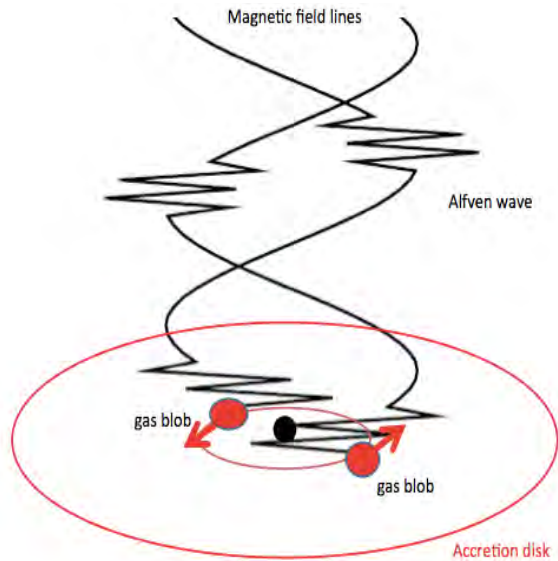
extreme high energy cosmic rays ($\sim 10^{21}$ eV)

episodic γ -ray bursts observed

consistent with **LWFA** theory

Astrophysical **wakefield** acceleration:

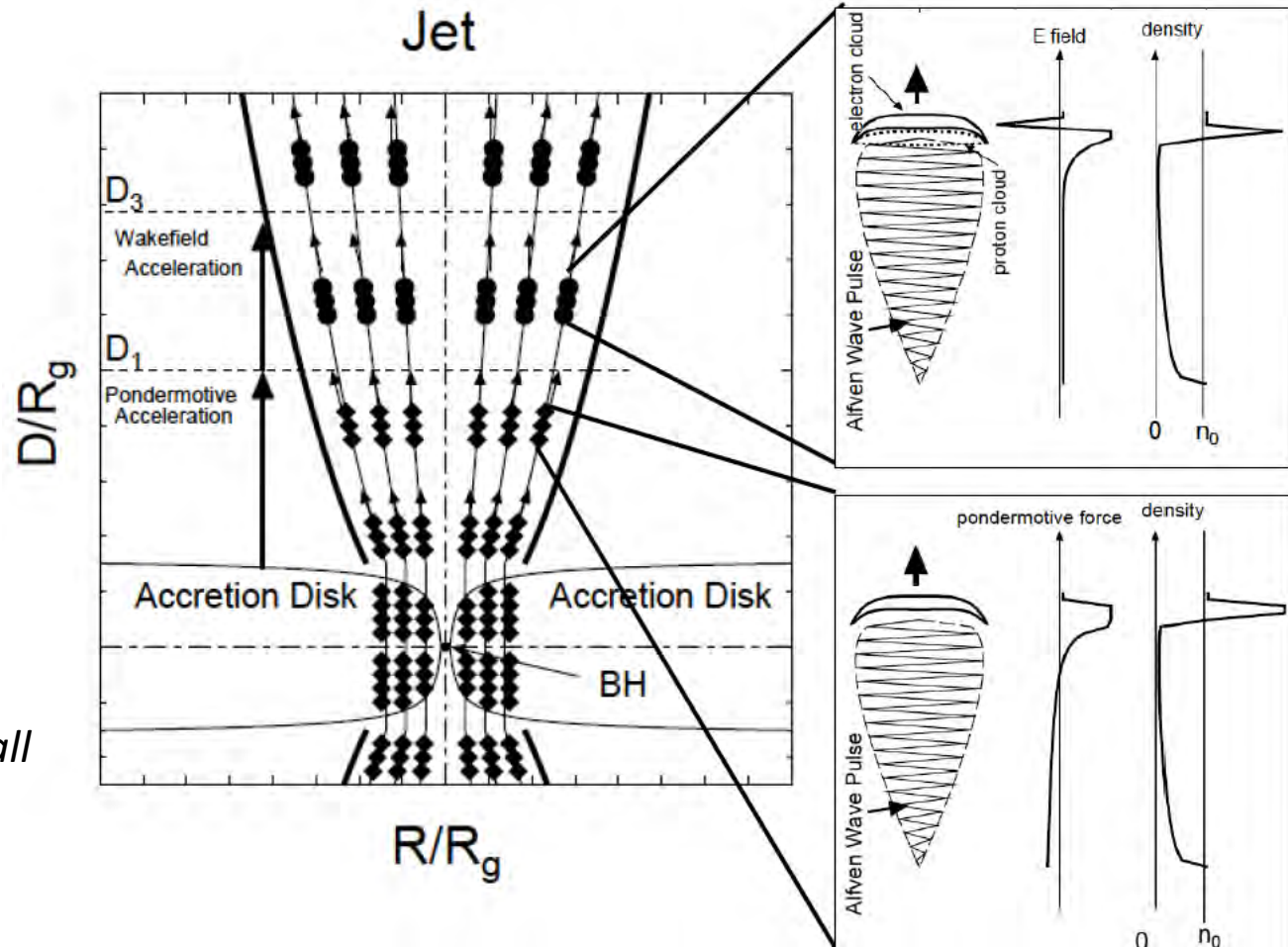
Superintense **Alfven Shock** in the Blackhole Accretion Disk toward ZeV Cosmic Rays ($a_0 \sim 10^6 - 10^{10}$, large spatial scale)



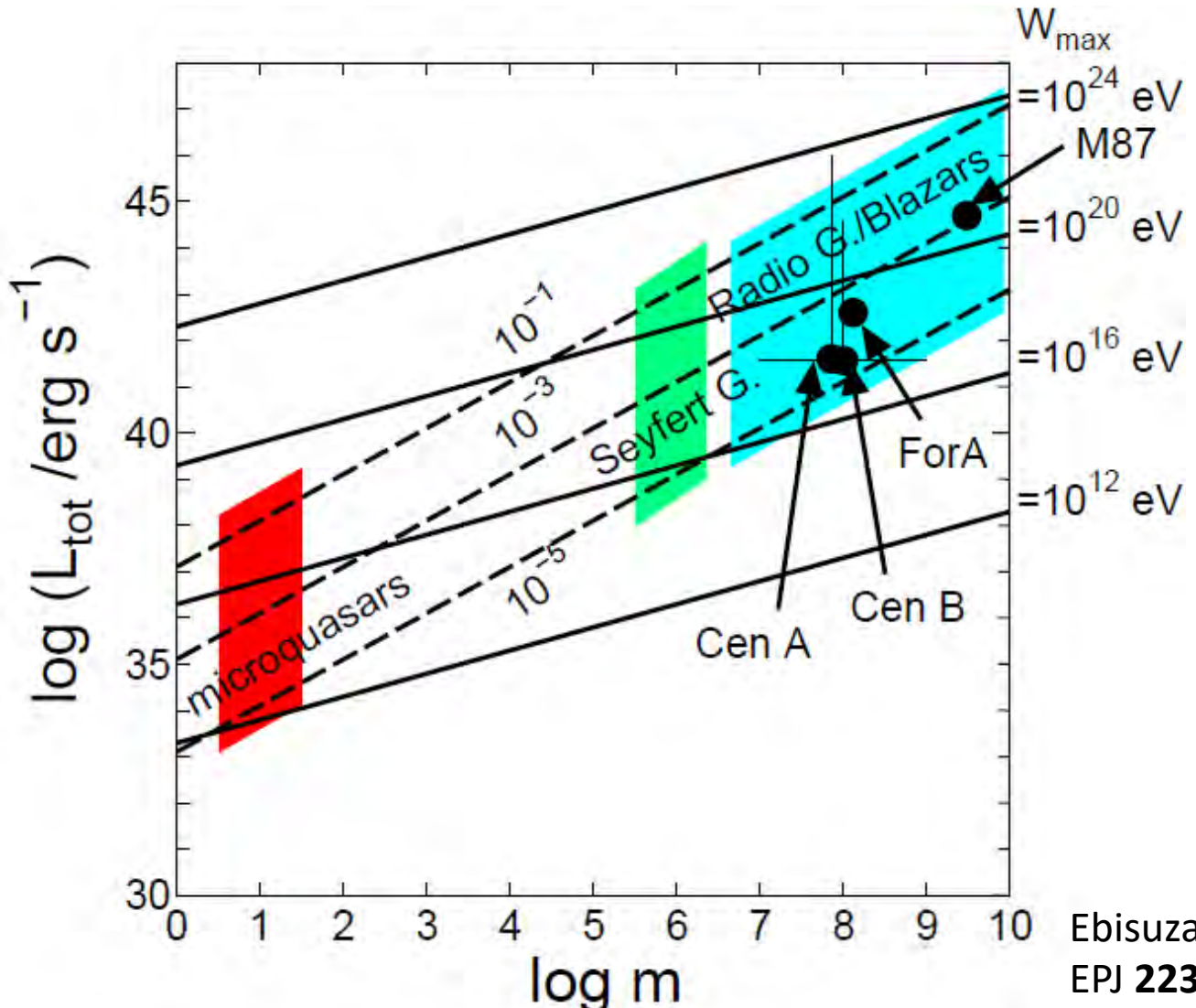
$$a_0 = eE_0 / mc\omega_0 \gg 1$$

E_0 : modest

ω_0 : extremely small



Comic ray acceleration and γ -ray emission: Summary



Blazar shows anti-correlation between γ burst flux and spectral index

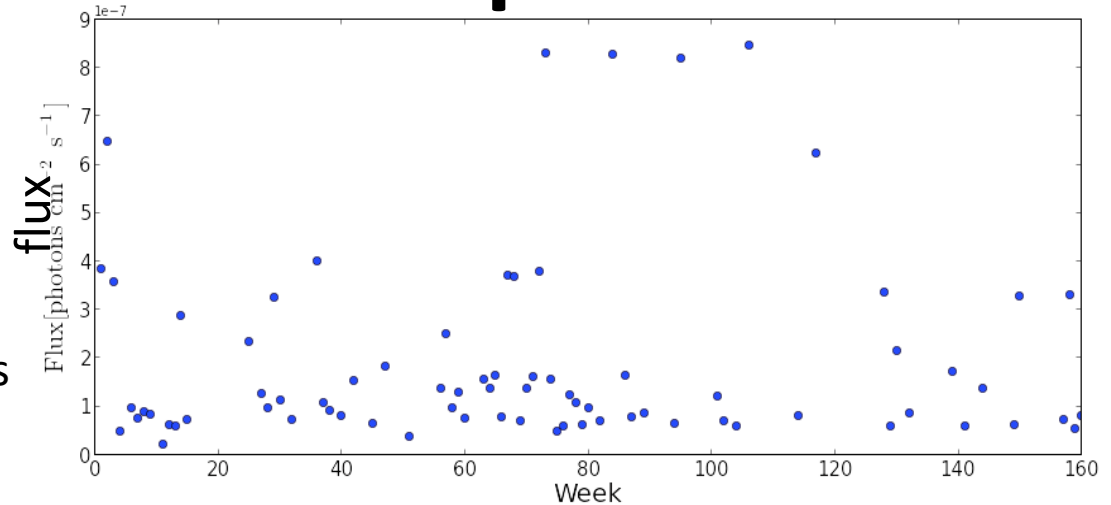
Blazar: AO0235+164

$M \sim 10^8 M_{\text{Sun}}$

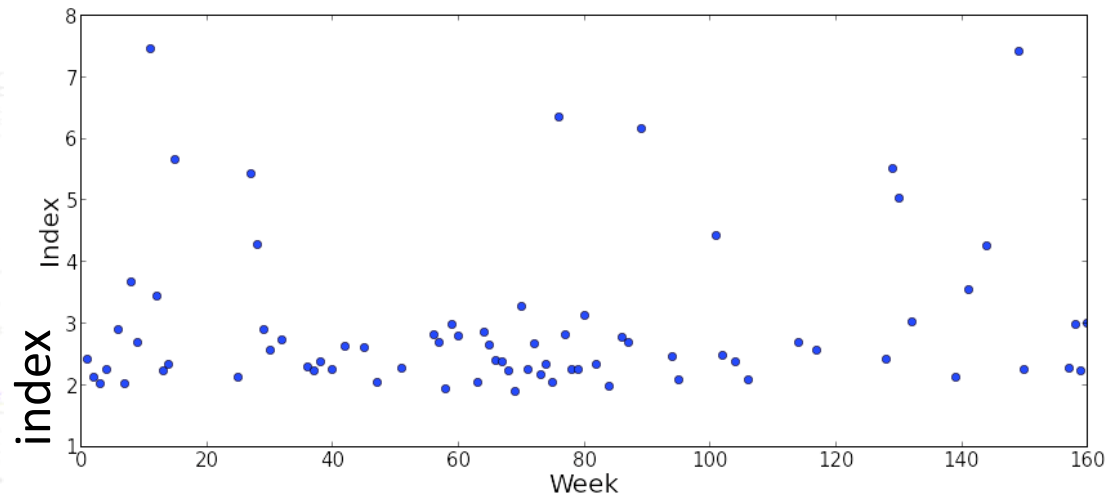
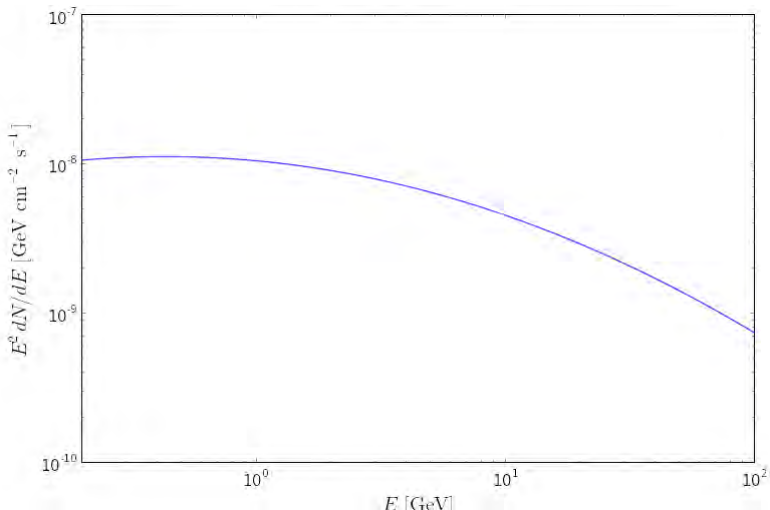
Rise time < week (less than a unit),
Period between bursts $\sim > 10$ weeks

Spectral index $\Rightarrow 2$

(\sim Ebisuzaki/Tajima theory)



\rightarrow all quantitatively consistent with **Wakefield** theory



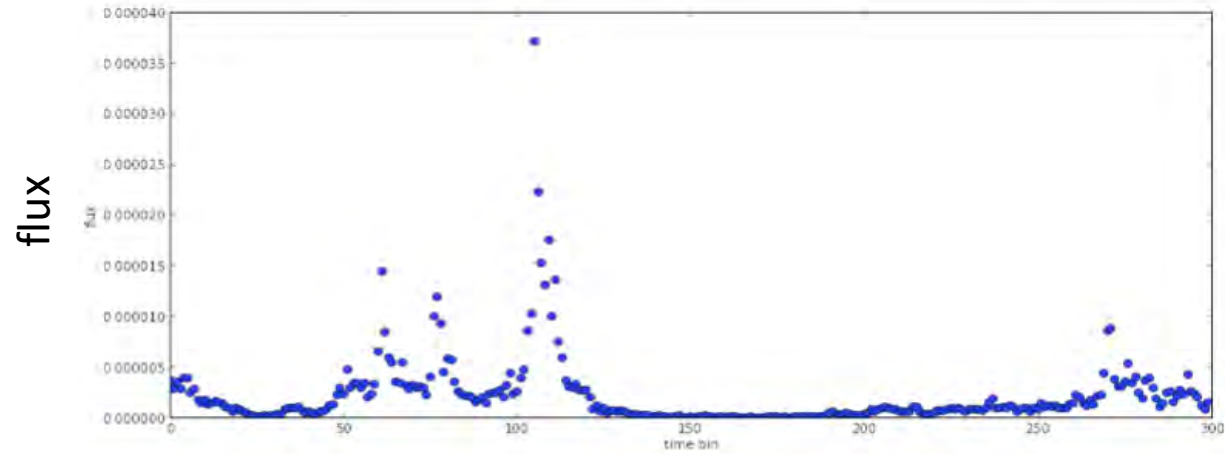
time

N. Canac, K. Abazajian (2019)

Again, Anti-correlation even in a bigger blazar

Blazar: 3C454.3

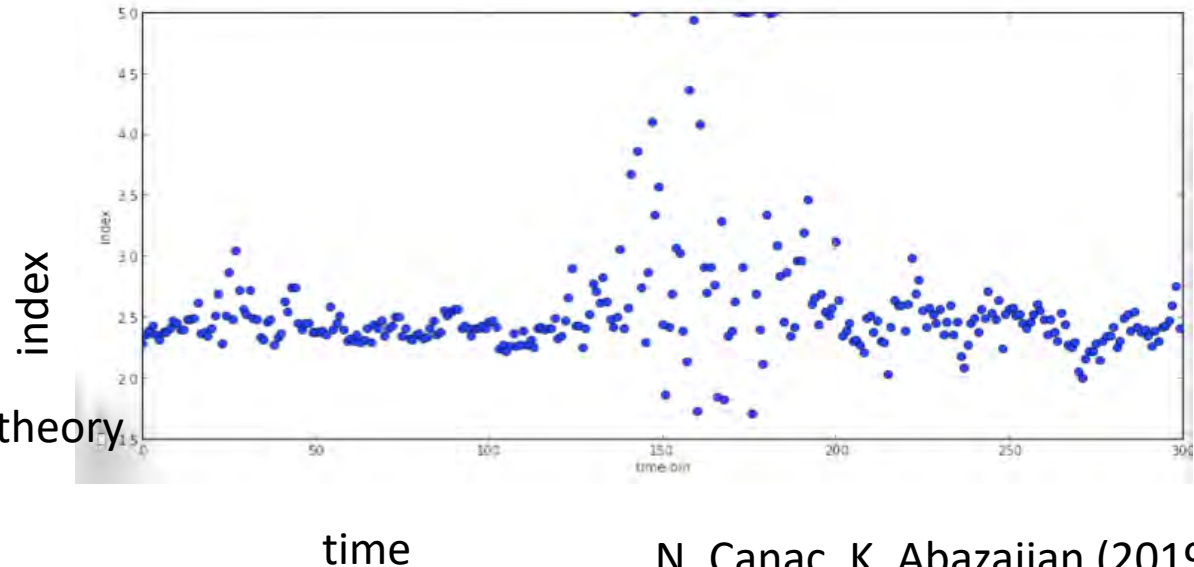
$M \sim 10^9 M_{\text{Sun}}$



Same anti-correlation as
AO0235+164

The rise time and burst periods
a lot longer (by an order of
magnitude)

Quantitative agreement and
correct scaling with Blazar mass
with (broader sense of) **Wakefield** theory
(Ebisuzaki/Tajima)
period $\sim M$; luminosity $\sim M$

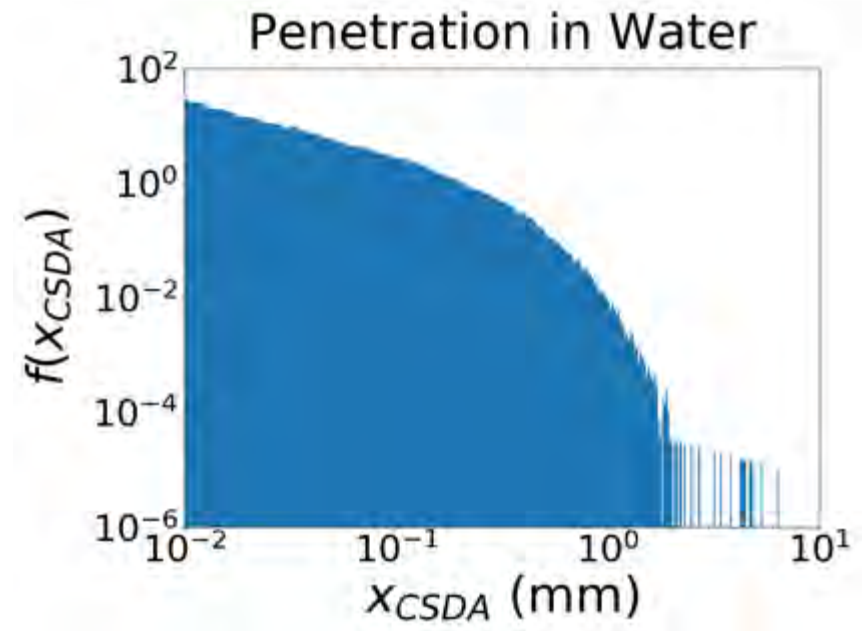
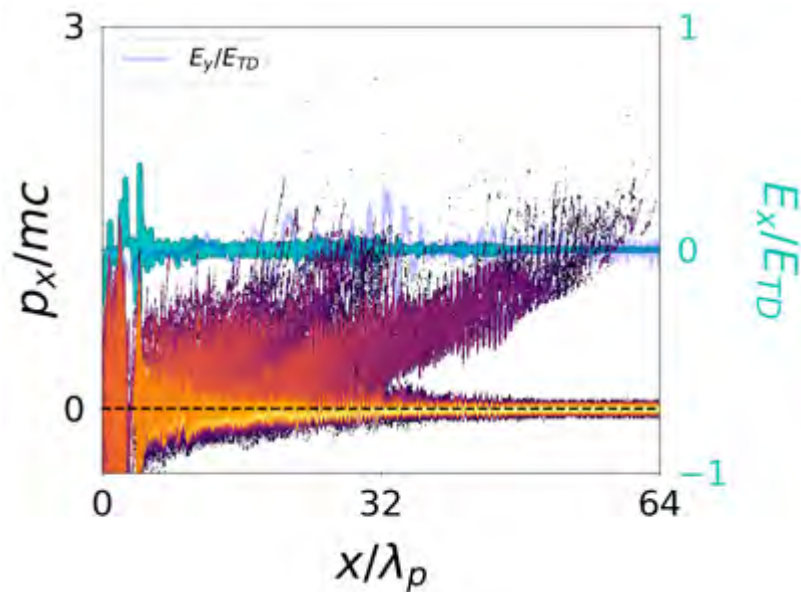


Nanotube cancer therapy



High density wakefields for medicine

- **Micron** accelerator (in body?) by **optical laser**
- **Nanomaterials** target: density $\sim 10^{21} \text{ cm}^{-3}$

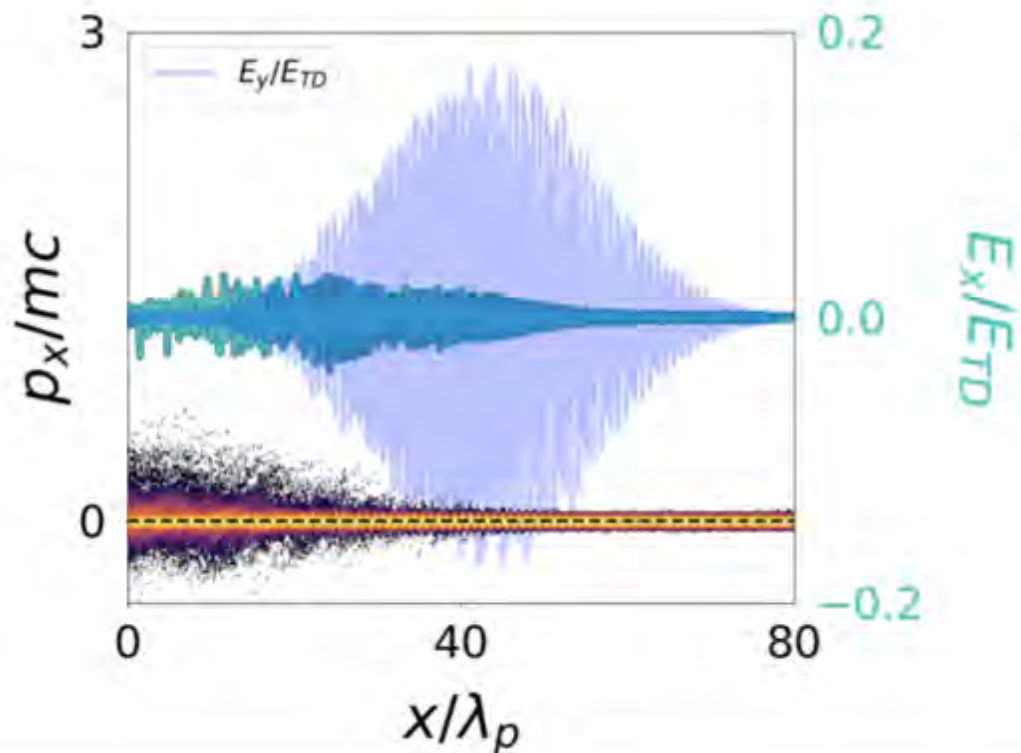
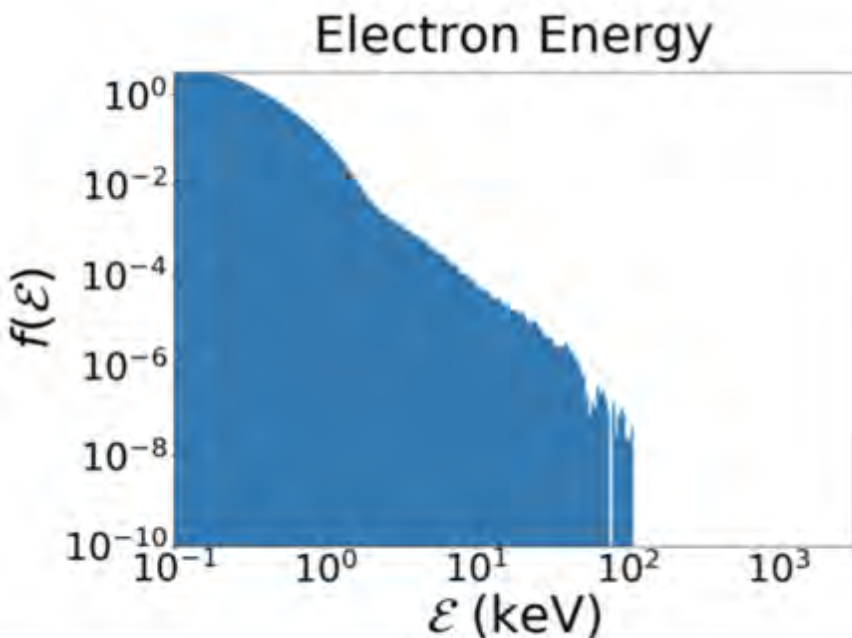


Critical density wakefield acceleration (< MeV) : e.g. skin cancer

Beatwave wakefield acceleration of electron acceleration in low intensity **laser**

- Two laser pulses, each @ $a_0 = 0.03$
- $a_0 = 0.03 \rightarrow 1.2 \times 10^{15} \text{ W/cm}^2$
- Wavelength: $\lambda_0 = 1 \mu\text{m}$
- $\omega_1 = \omega_0 + \omega_p/2, \omega_2 = \omega_0 - \omega_p/2$
- Pulse length: $\approx 300 \text{ fs}$

← Tajima-Dawson (1979)



Conclusions

- 1994-**LWFA** Demonstrated: ultrafast pulses, coherent collective (robust) intense (GeV/cm) accelerators.
- TFC \rightarrow Single-cycled **laser** \rightarrow single-cycled **X-ray laser** (also high density e-bunch)
- **Wakefield in nanostructure** (TeV/cm):
TeV on a chip accessible*
- Toward PeV ($\sim 10\text{-}100\text{m}$)
- **Wakefields**: Nature's favored acceleration for **gamma ray** bursts, UHECR from Blazars
- Applications: tiny **LWFA** radiotherapy of cancer

* Book: "Beam Acceleration in Crystals and Nanostructures" (WSP, 2020)

Recent advancements in generation of intense X-ray laser ultrashort pulses open opportunities for particle acceleration in solid-state plasmas. Wakefield acceleration in crystals or carbon nanotubes shows promise of unmatched ultra-high accelerating gradients and possibility to shape the future of high energy physics colliders. This book summarizes the discussions of the “Workshop on Beam Acceleration in Crystals and Nanostructures” (Fermilab, June 24–25, 2019), presents next steps in theory and modeling and outlines major physics and technology challenges toward proof-of-principle demonstration experiments.

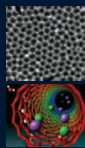
Thank you!

“Accelerator
Unprecedented and huge
Curious baby
Embraced by Mother Mountain
Where’s her beautiful white coat?”
(Toshiki, Geneva, Feb. 13, 2020)

World Scientific
www.worldscientific.com
11742 hc



Chattoopadhyay • Mourou
Shiltsev • Tajima



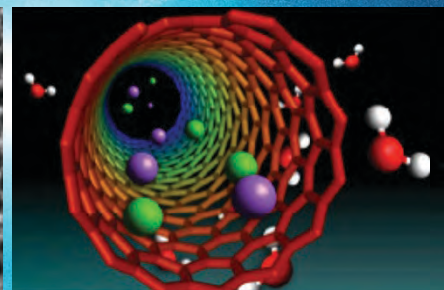
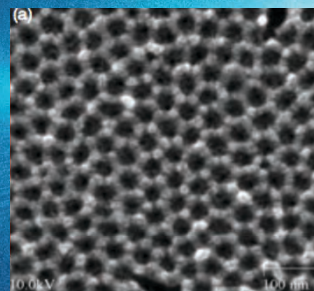
BEAM ACCELERATION IN
CRYSTALS AND NANOSTRUCTURES



BEAM ACCELERATION IN CRYSTALS AND NANOSTRUCTURES

Edited by

Swapan Chattopadhyay • Gérard Mourou
Vladimir D. Shiltsev • Toshiki Tajima



 World Scientific